

# Visualising Types of Uncertainty in Spatial Information

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National Academy of Sciences, 3-4 March 2005

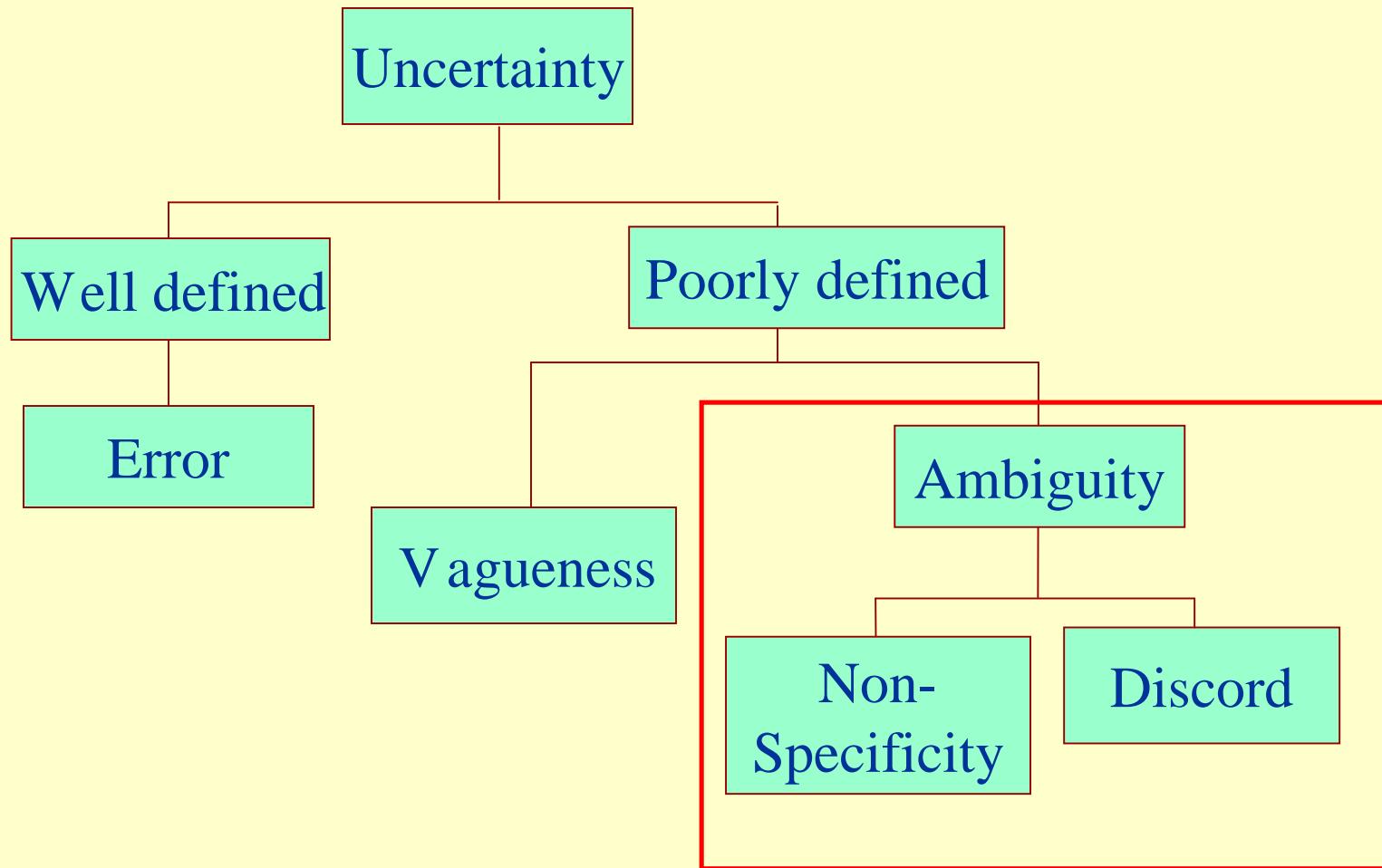
# Outline

- Issues
  - The Problem
  - The variety and levels of uncertainty
- Some solutions?
  - Monochrome or multihue maps
  - Static (error) animation
  - Sound
  - Linked windows
- But there are other dimensions to uncertainty
  - Here we will explore these other dimensions

# The Problem

- Uncertainty about mapped information
- The map fills the available display space
- BUT
- We know that the map is in error,
- or is uncertain, to some degree
- How can we display this *extra* information?

# A Taxonomy of Uncertainty

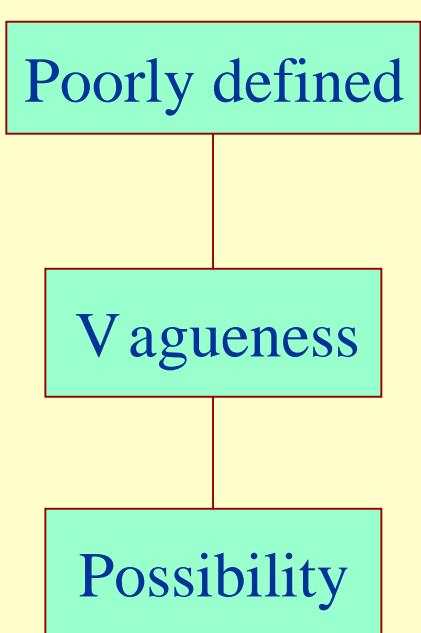


# Object level uncertainty

- Uncertainty can be at any level
  - The object mapped
  - The legend category within the theme
  - The theme
  - The map across themes
- We may need different methods for the different levels

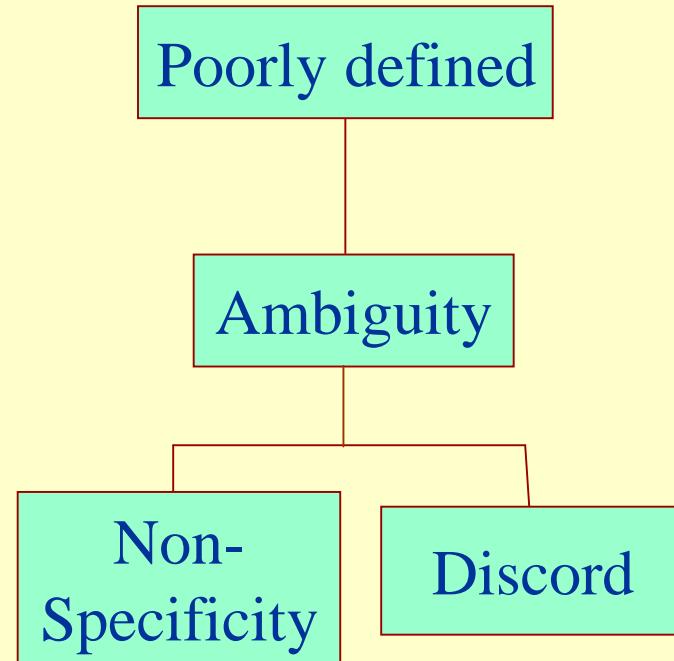
# Vagueness - Possibility

- Grounded in Philosophical Vagueness
- Sorites Paradox
- Semantic and epistemic vagueness *may* be addressed by Fuzzy Set theory
- Uses the same visualisation methods?
- Is this a good idea?



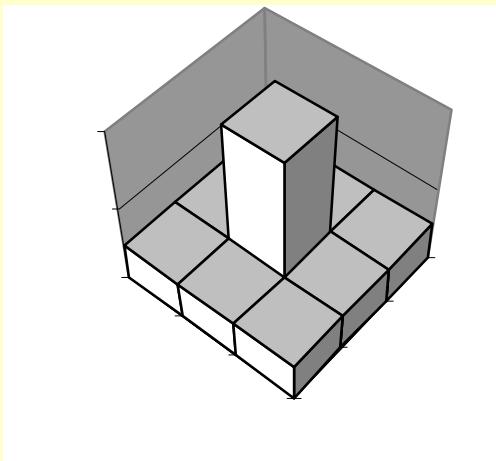
# Ambiguity

- Two, or more, different views of the same thing due to:
  - Non-Specificity
  - Discord

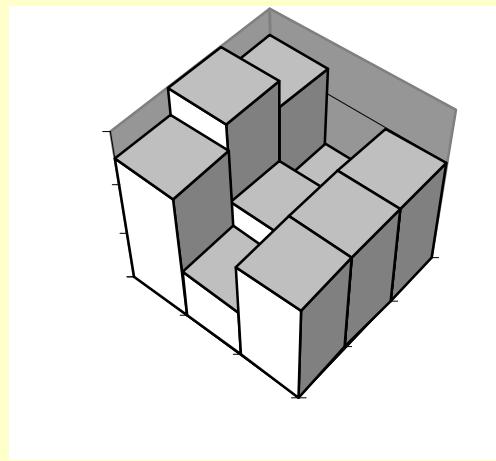


# Non-Specificity

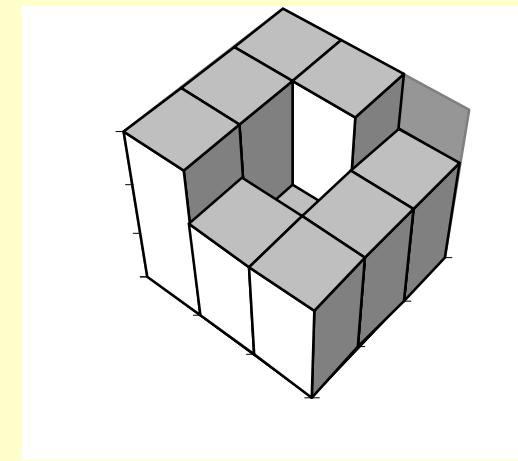
- The parameterisation is poorly specified
- An example
  - Landscape classification by morphometry
  - Morphometry
    - A specific algorithm
    - But how should be it measured?



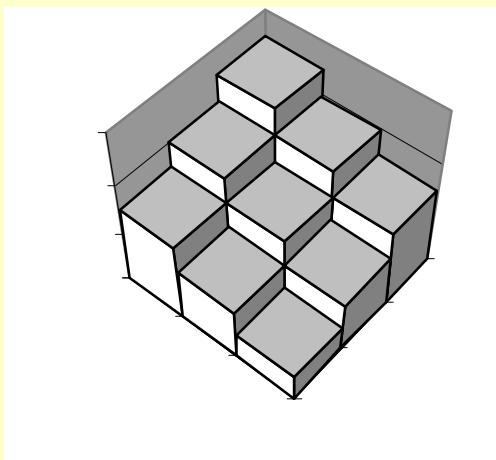
Peak



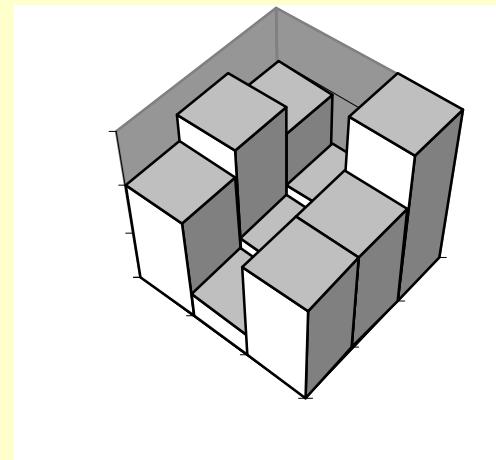
Pass



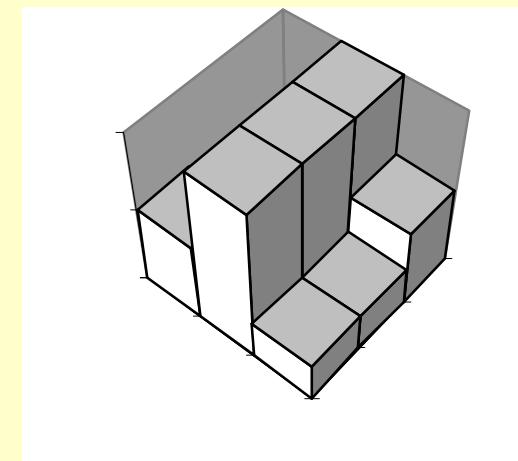
Pit



Planar



Channel



Ridge

## More formally

- The Landform,  $L$ , at any location,  $x$

$$L_x = [A]$$

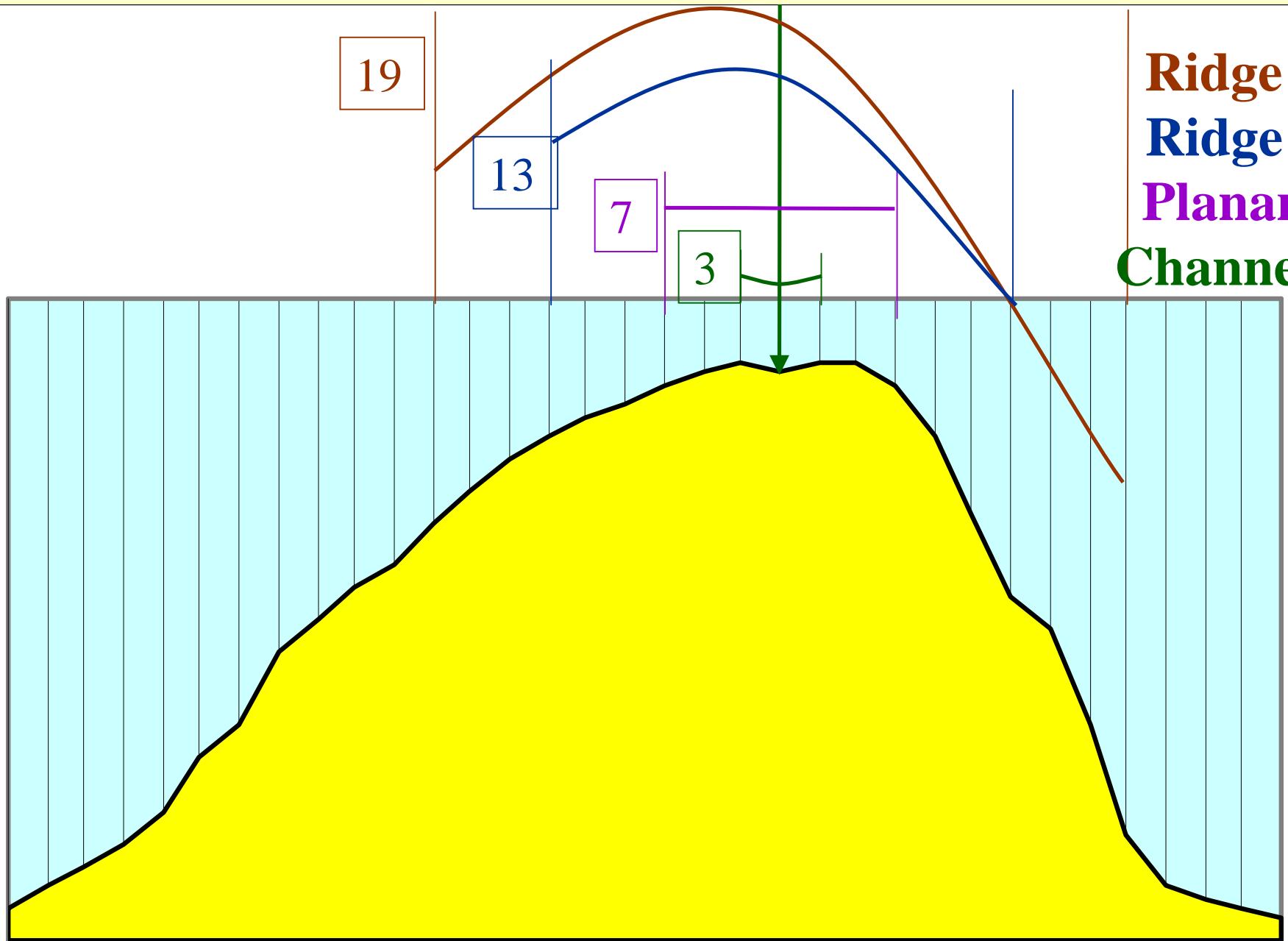
- where  $[A]$  is a set of Boolean morphometric classes

– [ridge, peak, pass, channel, pit, planar]

- And so for five  $A$   $m_{Ax} = [0]$

- And for only one  $A$   $m_{Ax} = [1]$

Ridge  
Ridge  
Planar  
Channel



# So resolution (scale) is important

- Many people have recognised the inconsistency of classification as ERROR
- BUT  $L_{xs_1} = L_{xs_2} \neq L_{xs_3} \dots$
- where s1, s2, etc indicate different scales of measurement
- Therefore for each A, the fuzzy membership of that morphometric class is

$$m_{Ax} = \frac{\sum_{i=1}^n m_{Axs_i}}{n}$$

# The Grey Corries

Stob Coire an Laoigh

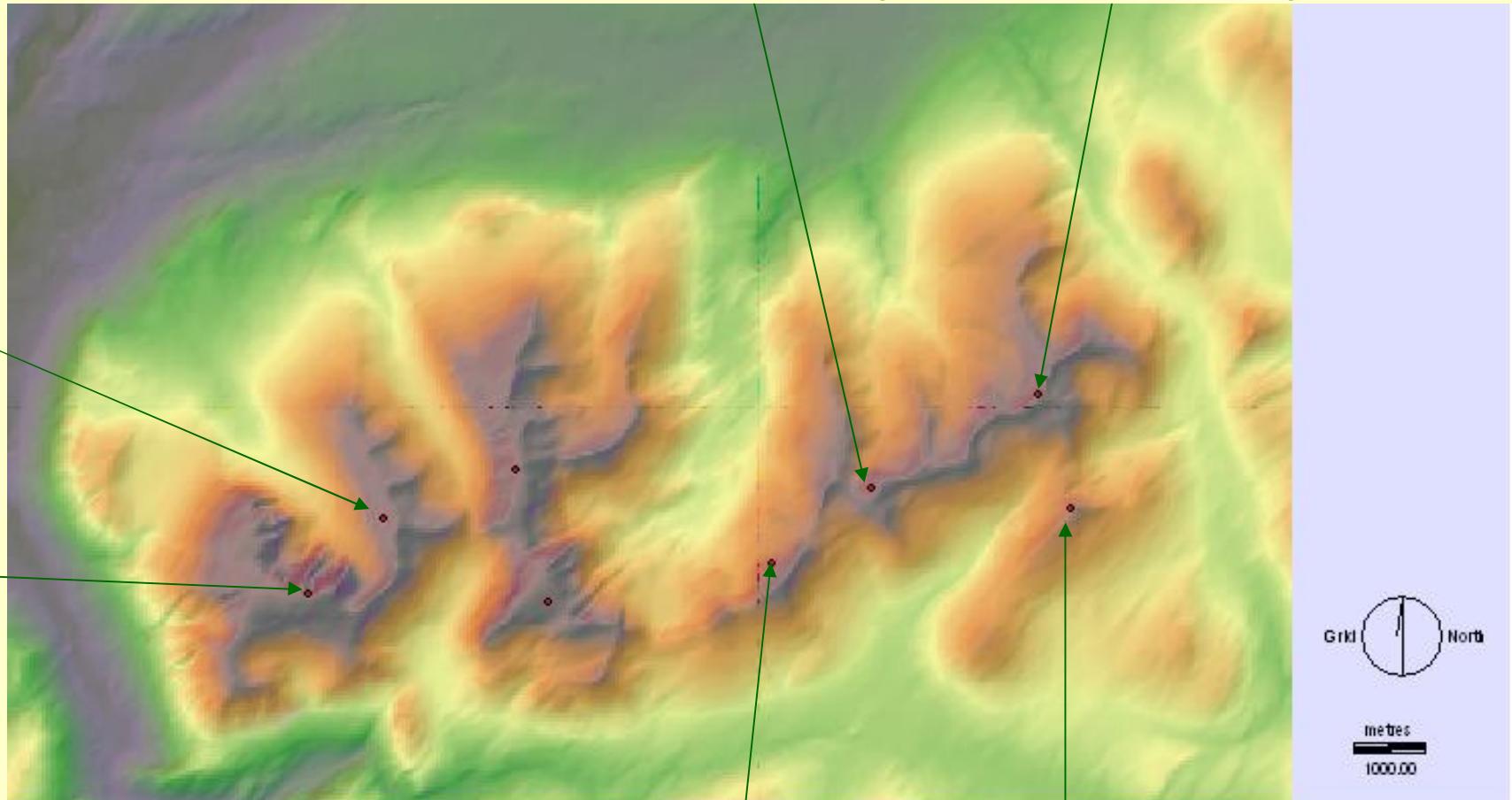
Stob Coire Claurigh

Carn  
Mor  
Dearg

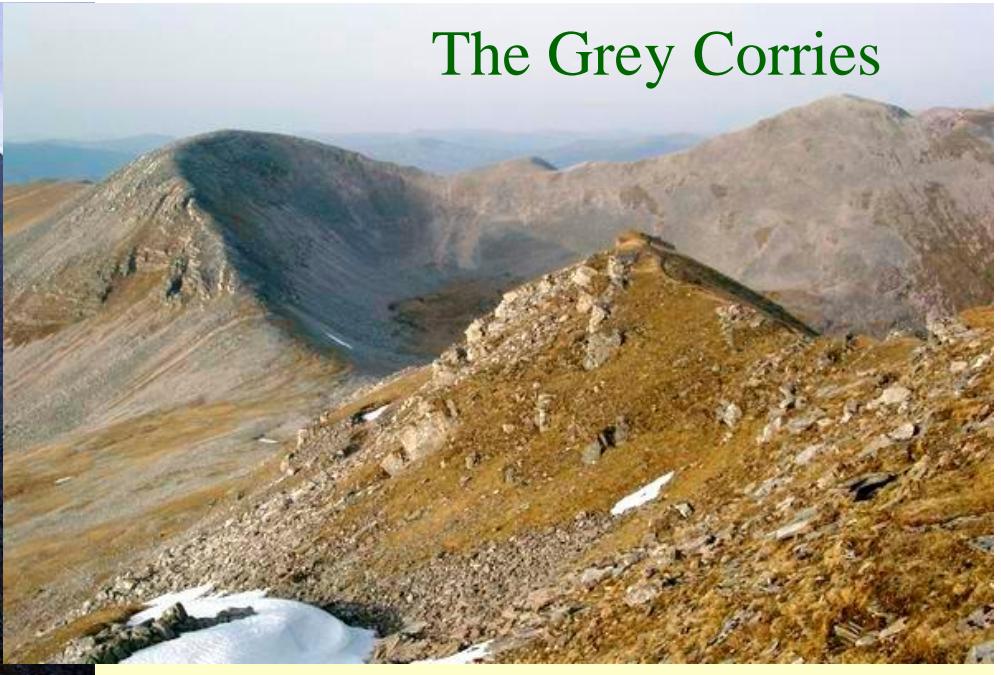
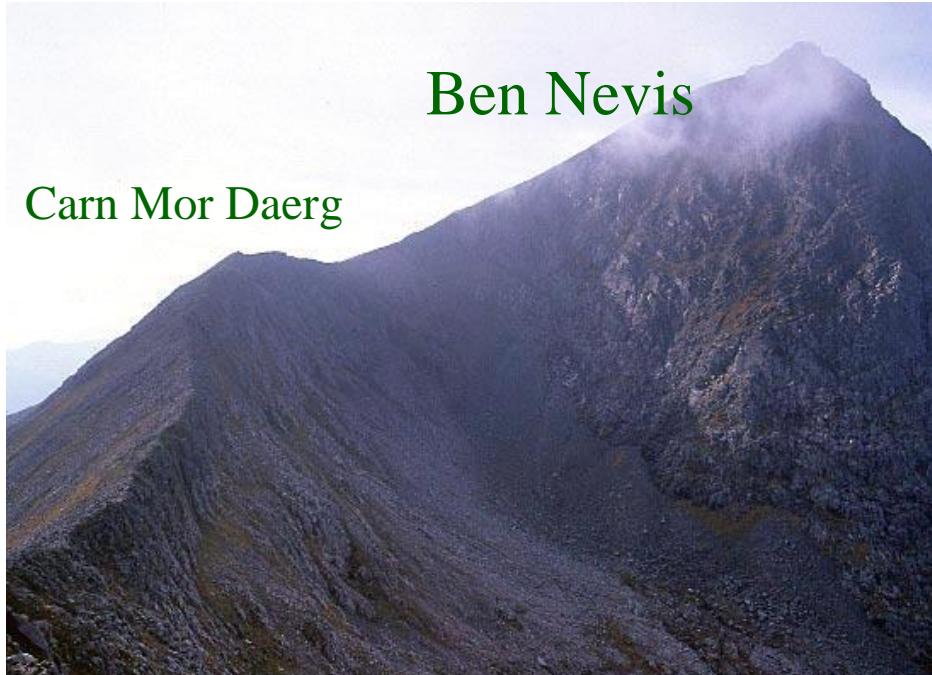
Ben  
Nevis

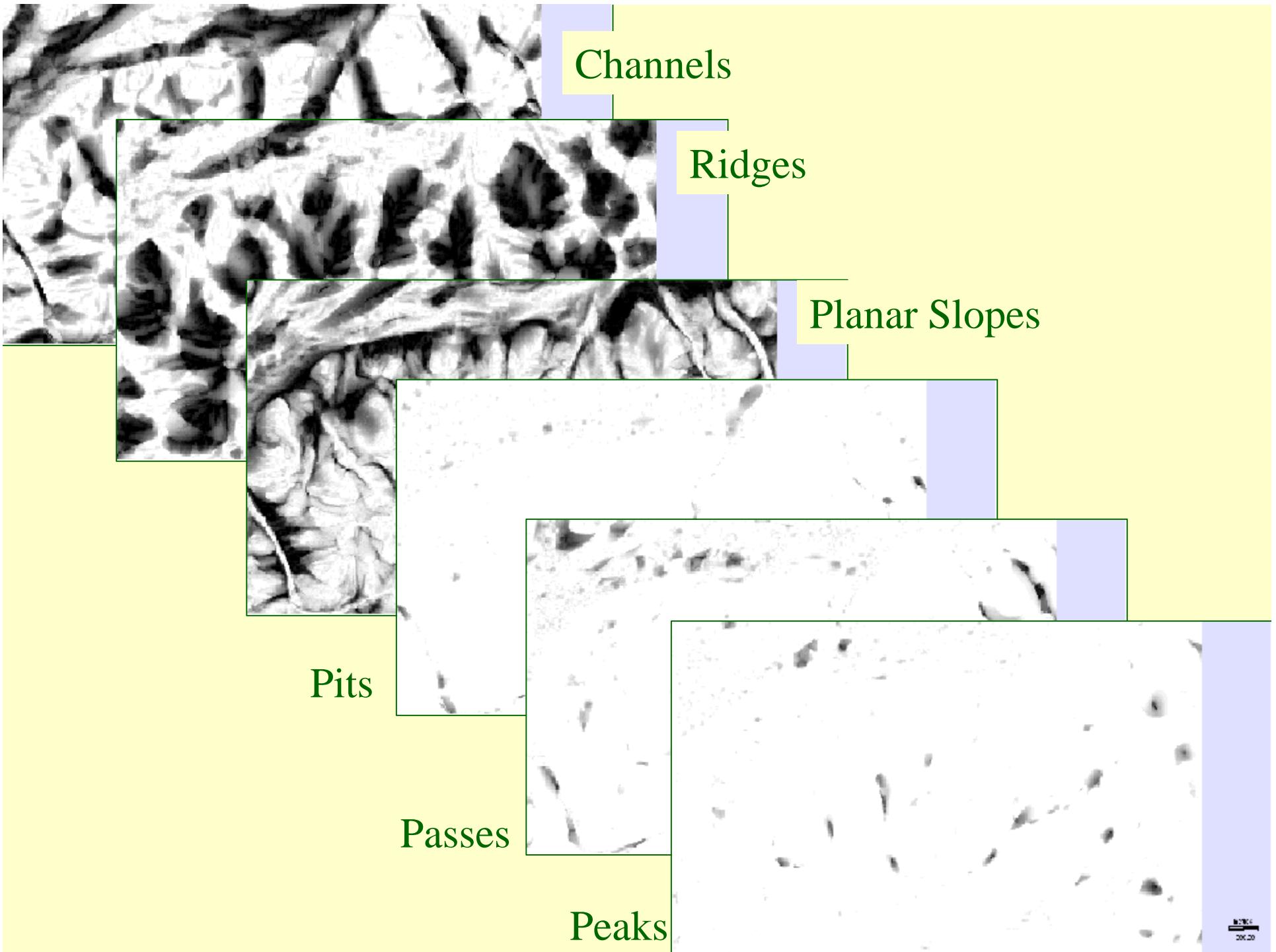
Sgurr Choinnich Mor

Stob Ban

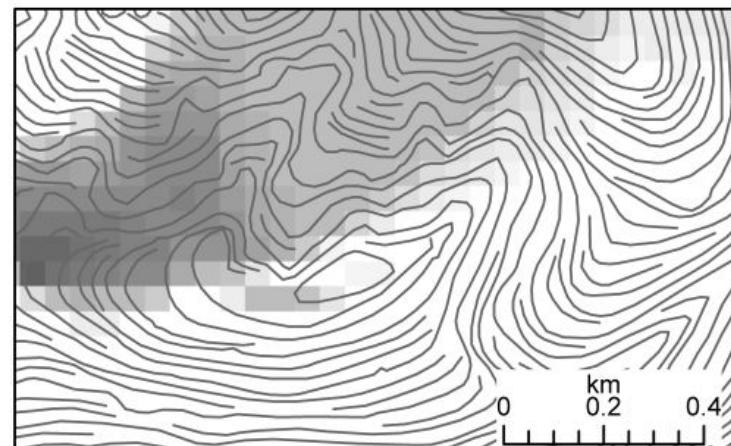
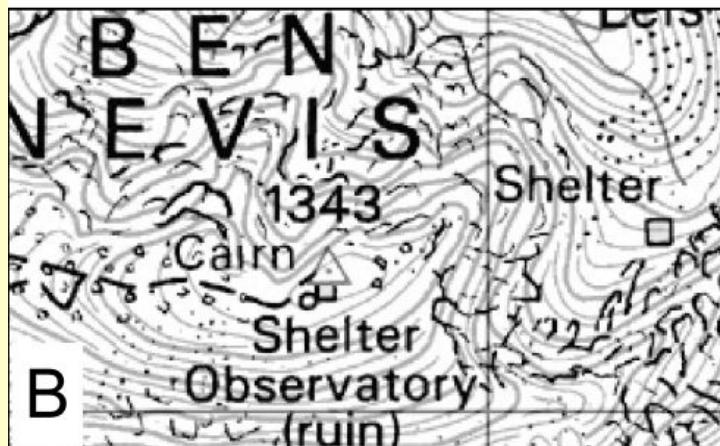
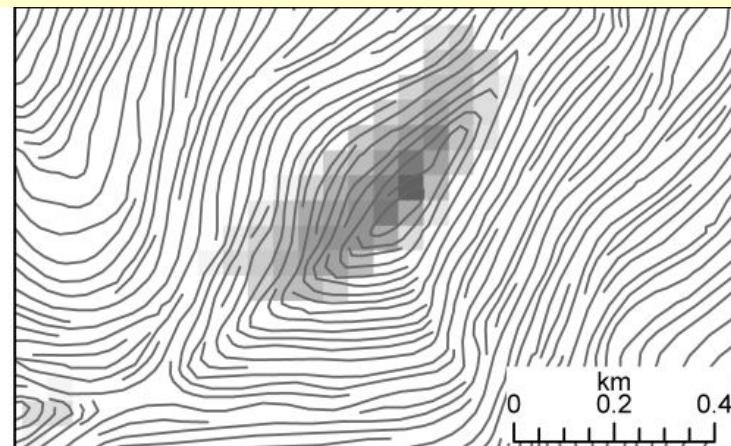
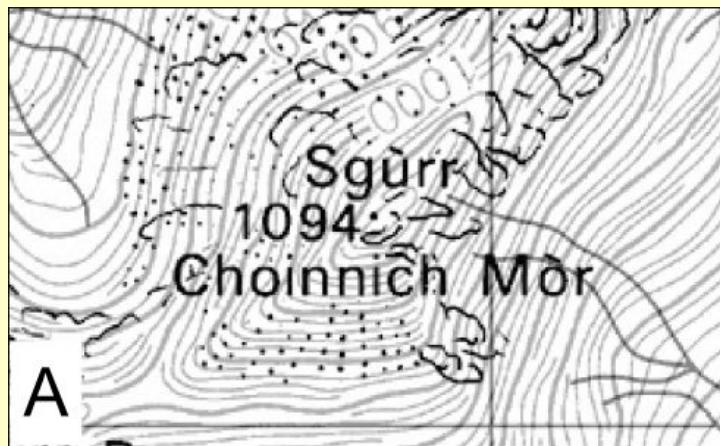


8 of the Scottish Munros (Peaks over 3000 ft)





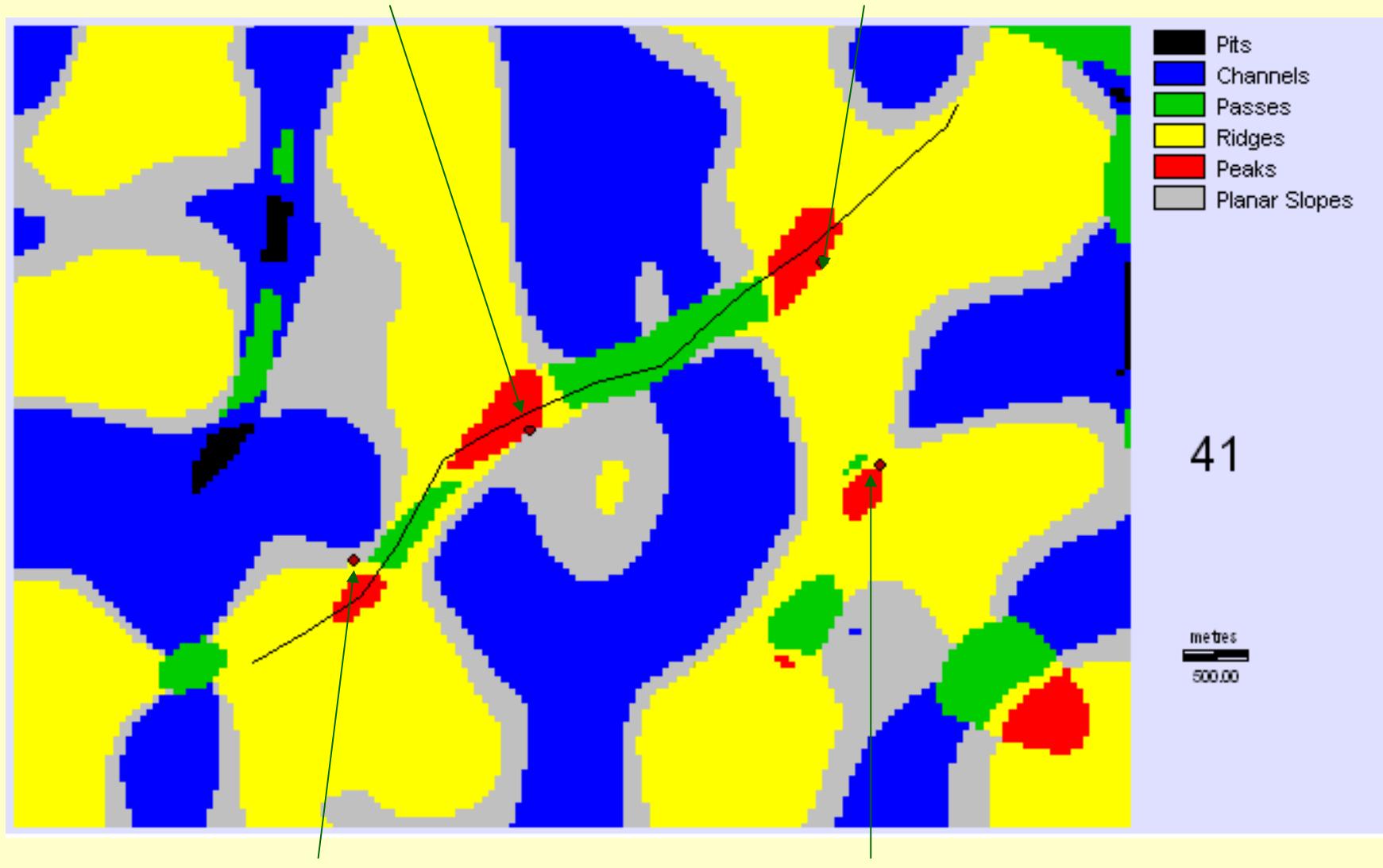
# Mountain Locations



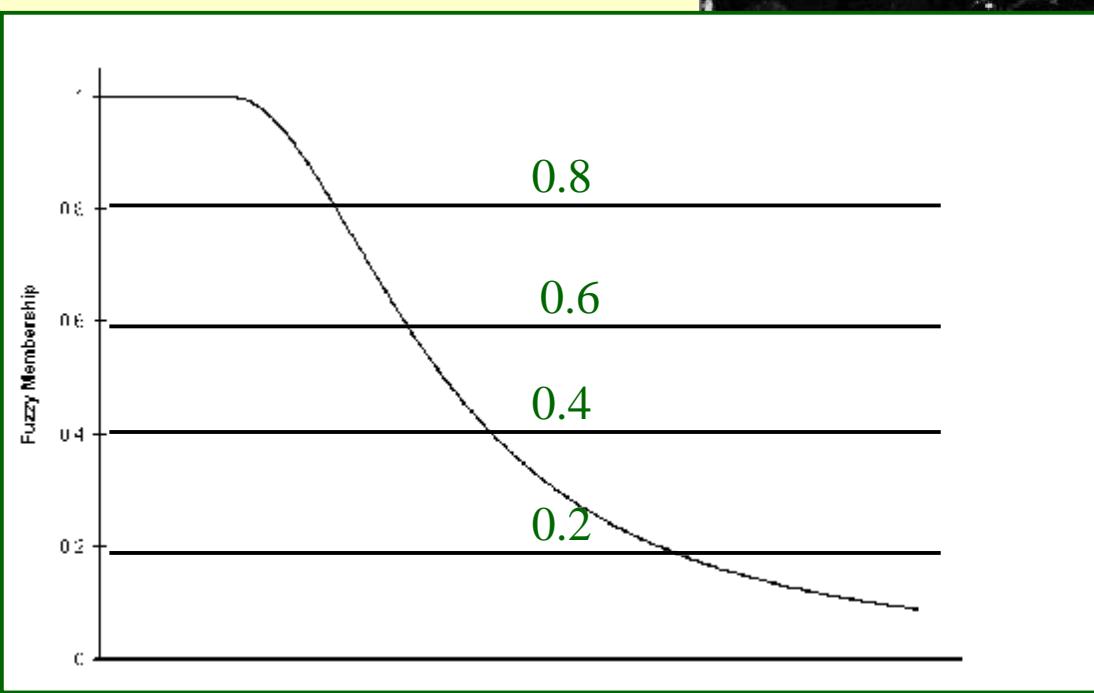
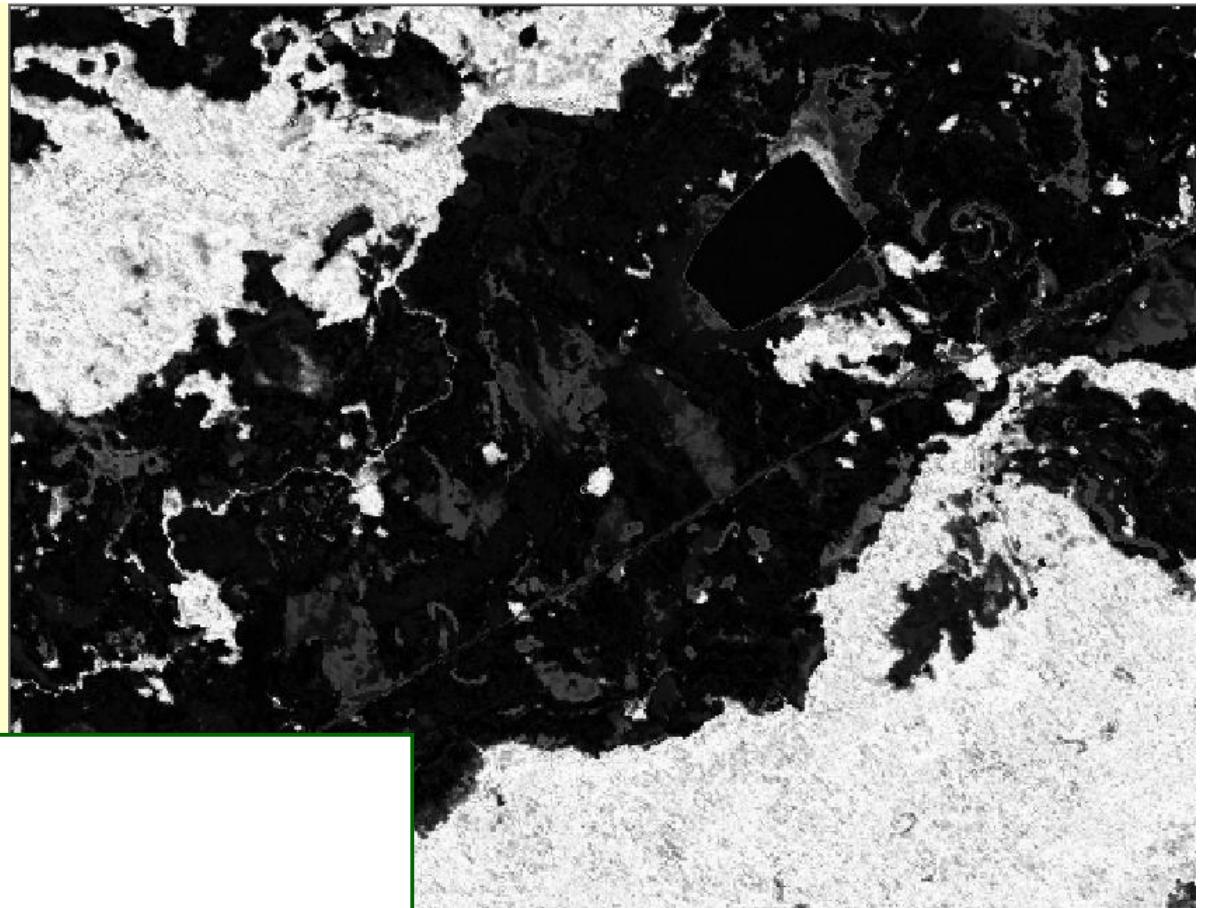
# Alternate Resolution Realisations of the Grey Corries

Stob Coire an Laoigh

Stob Coire Claurigh

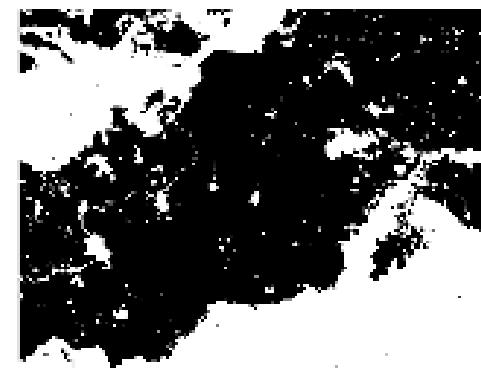
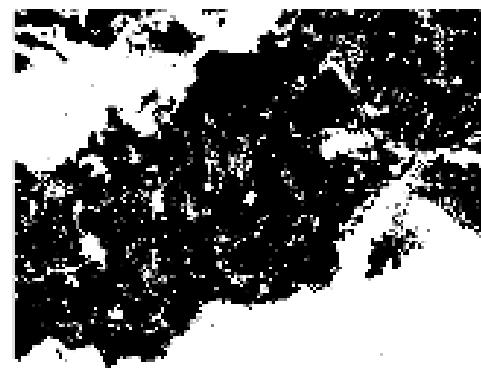


# Fuzzy Memberships as $\alpha$ cuts



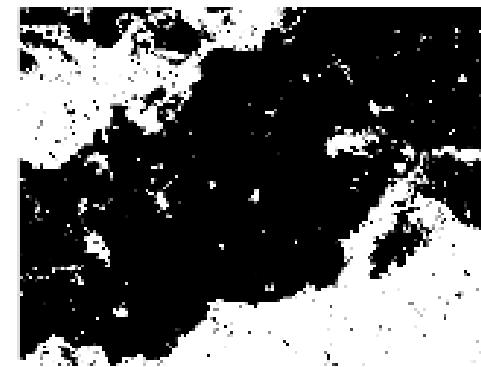
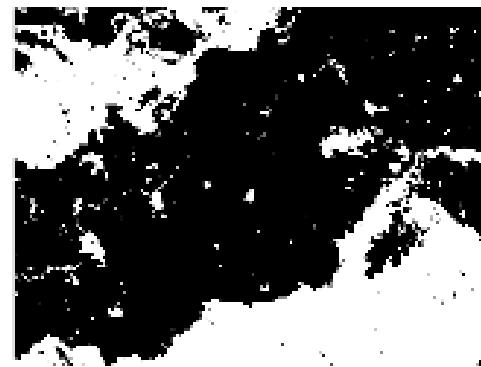
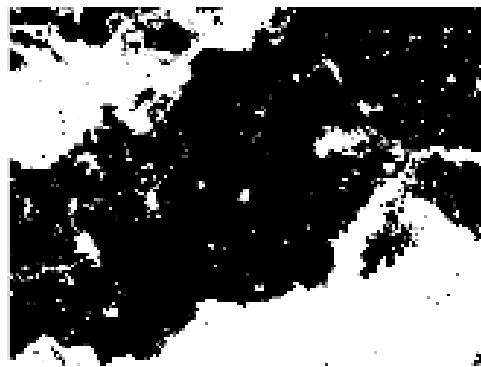
## $\alpha$ cuts are only boolean representations!

0.1



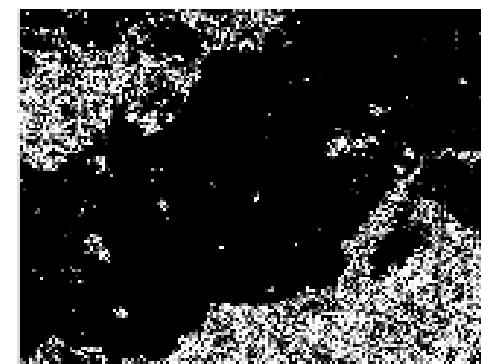
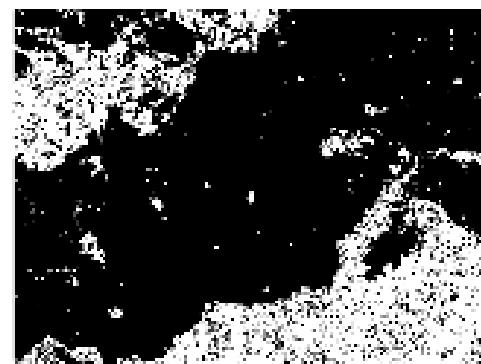
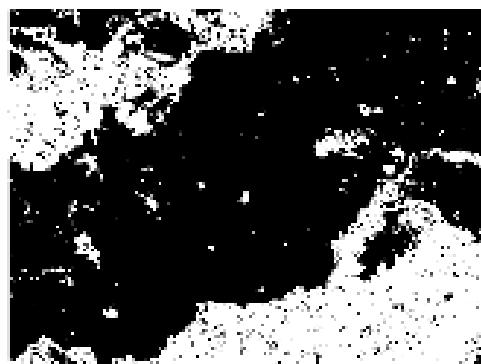
0.3

0.4



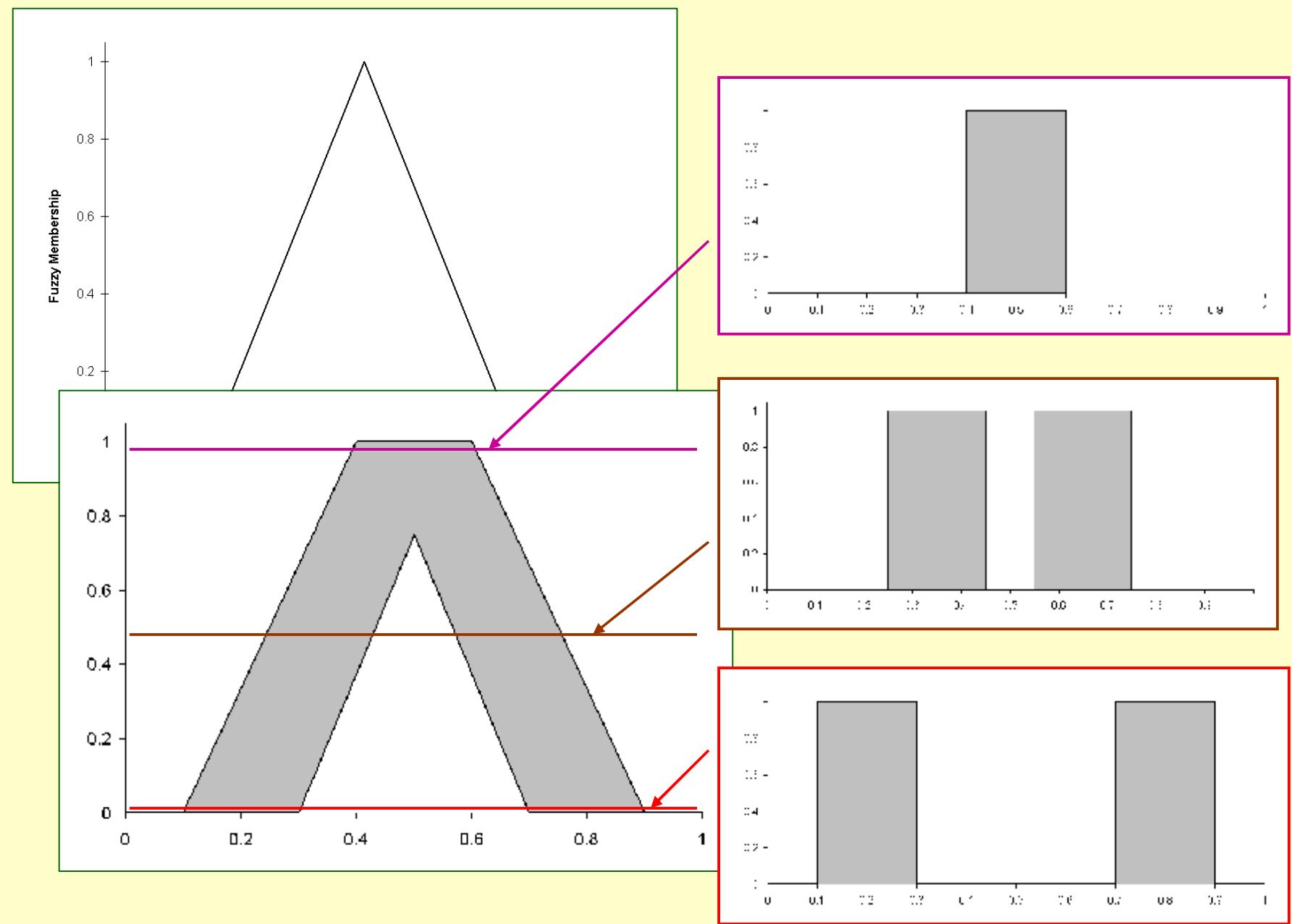
0.6

0.7



0.9

# An interval type-2 fuzzy set

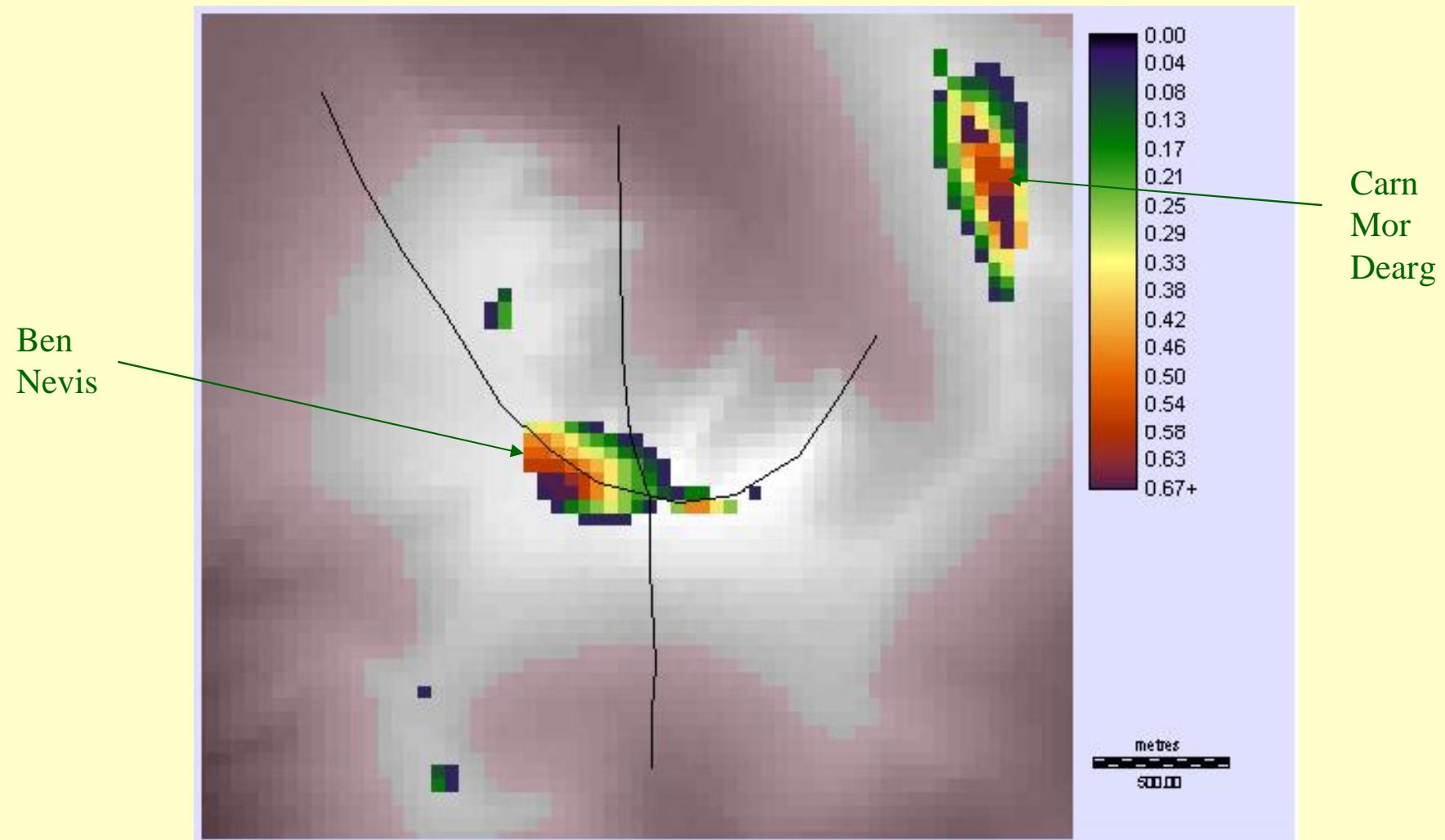


Type 2 Fuzzy sets correspond to  
higher order vagueness

So is there a higher order  
vagueness to a peak?

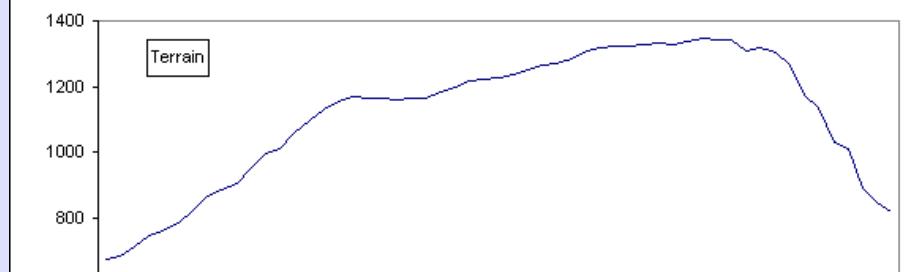
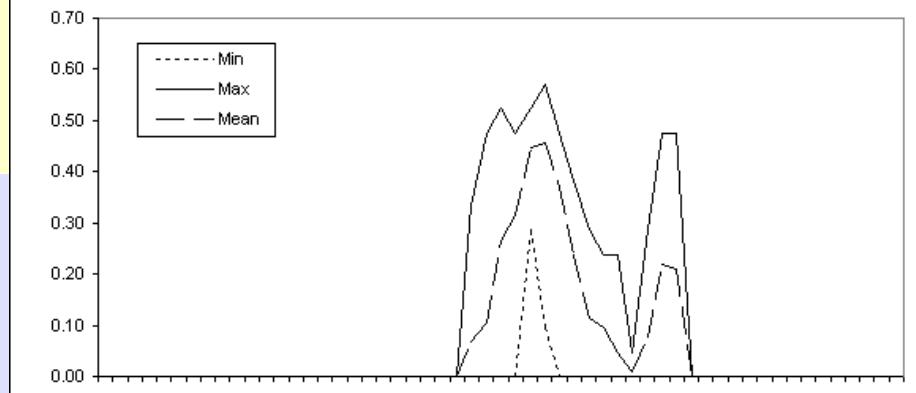
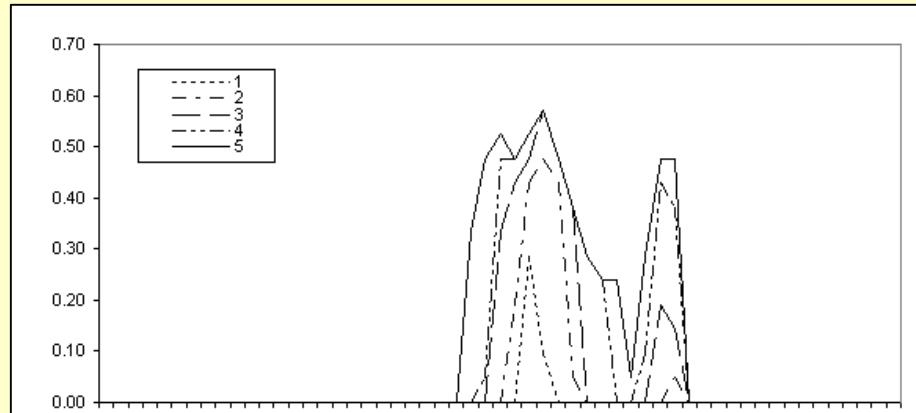
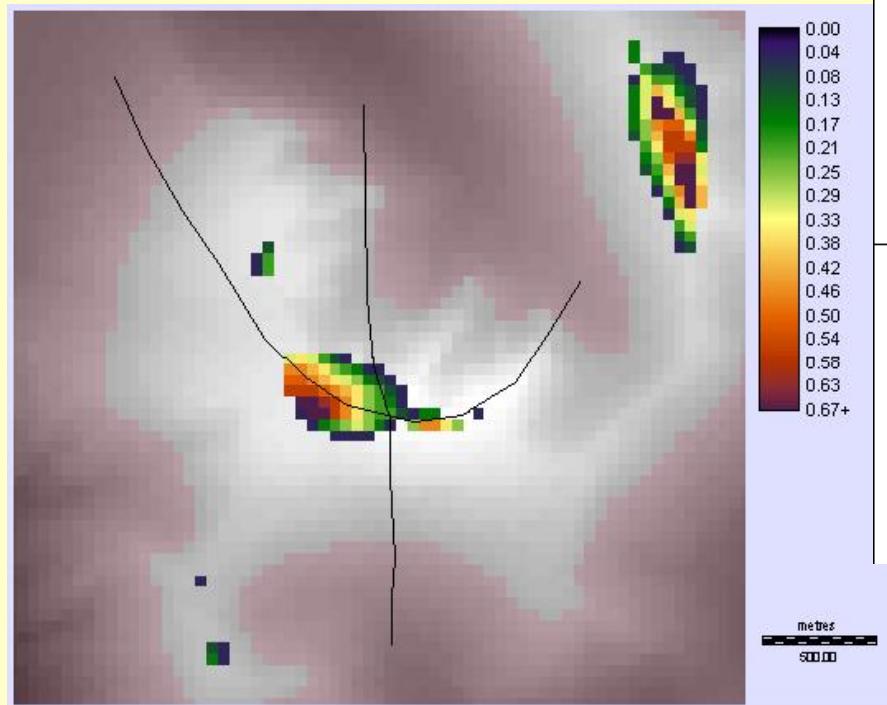
- Alternative smoothing methods
- Alternative parameterisation of the “peak”
  - Slope threshold

# Alternate Resolution Realisations of the Ben Nevis



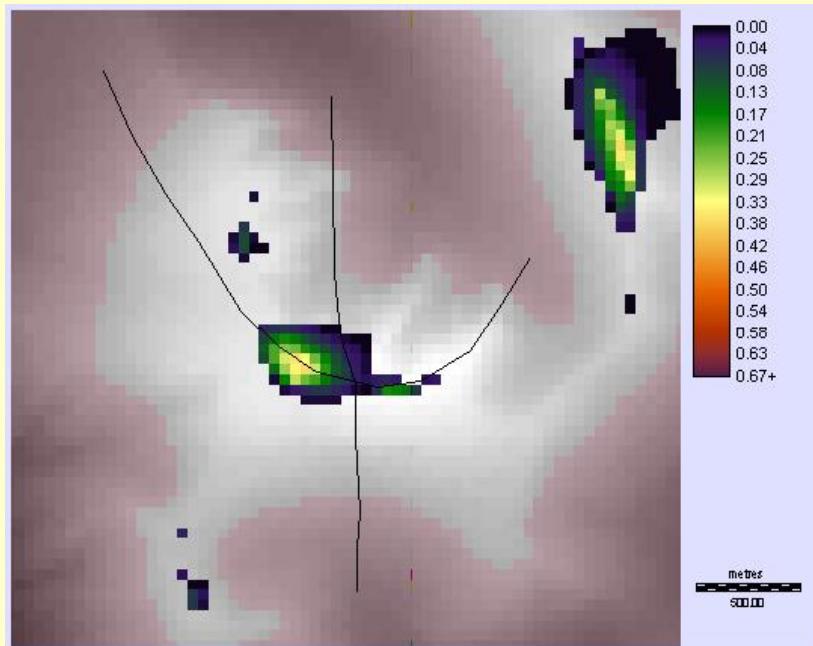
# Type 2 Fuzzy sets of Ben Nevis

## Distribution and Bounds

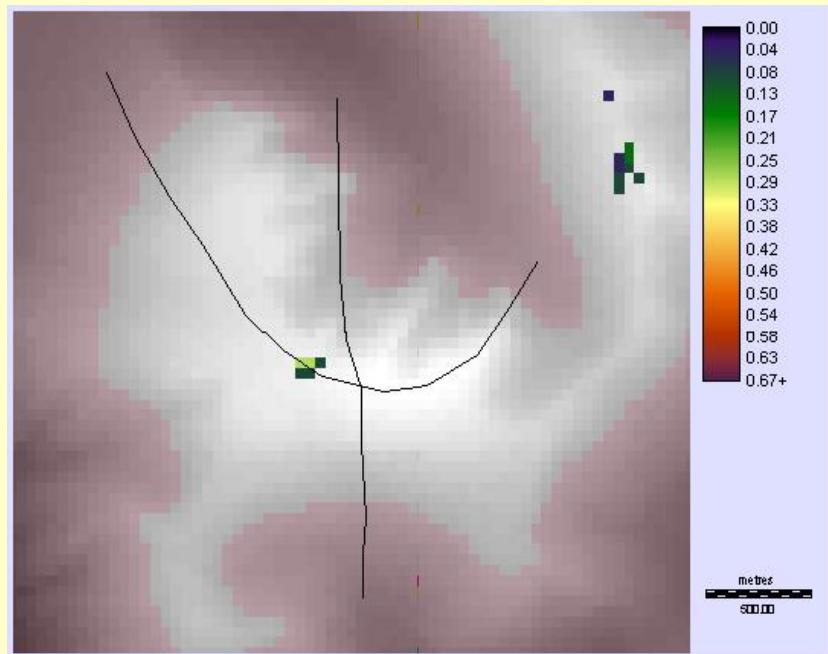
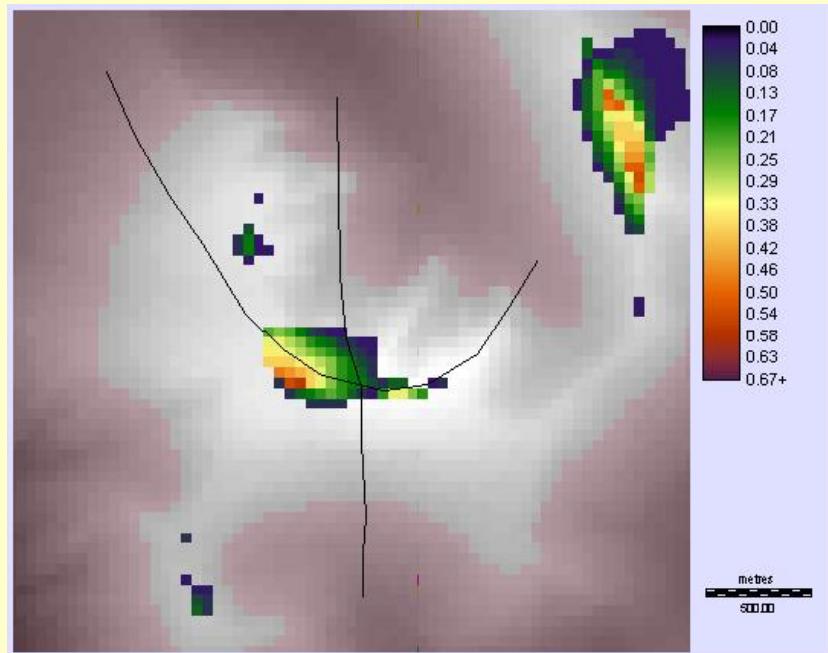


# Bounds

Mean Membership

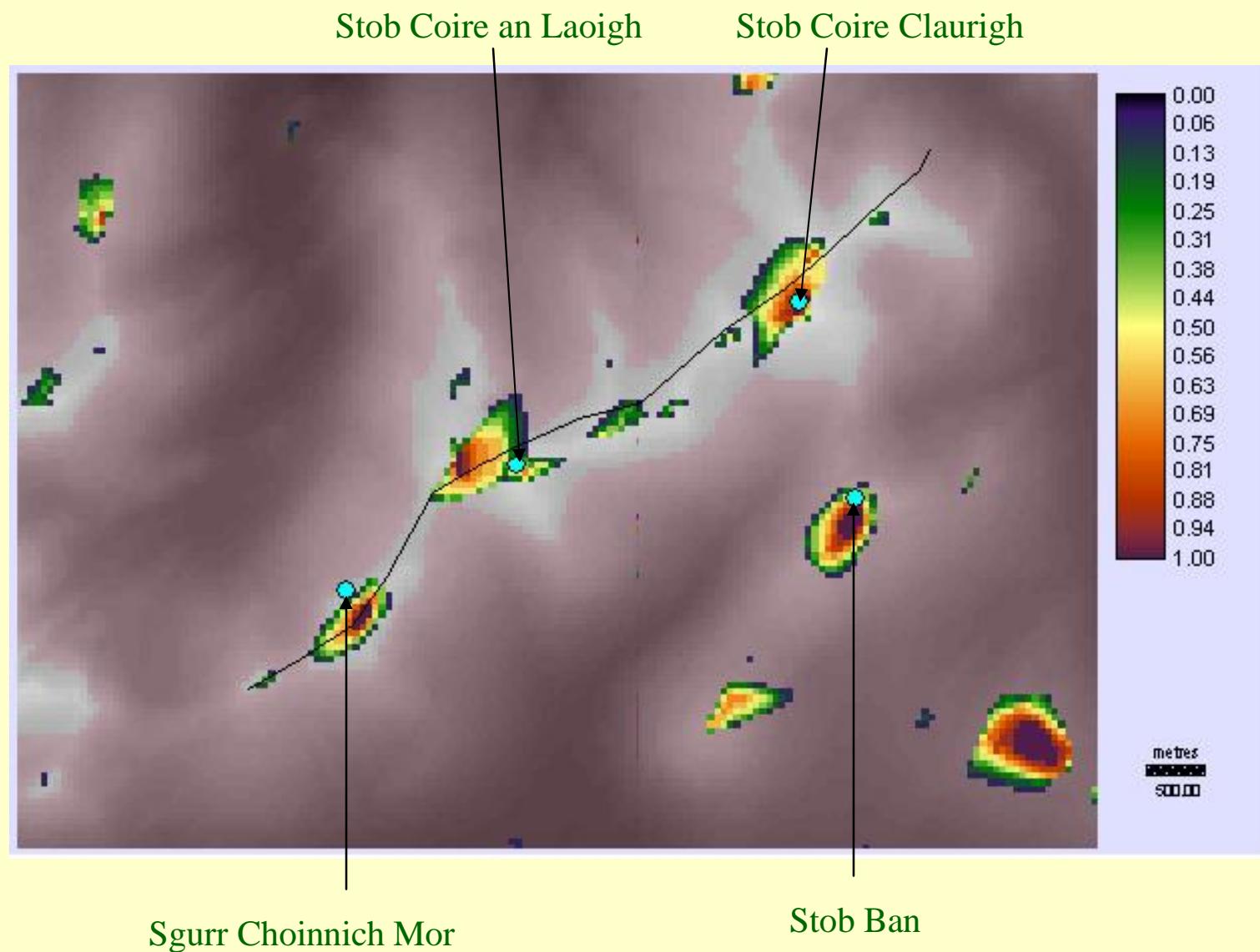


Minimum Membership



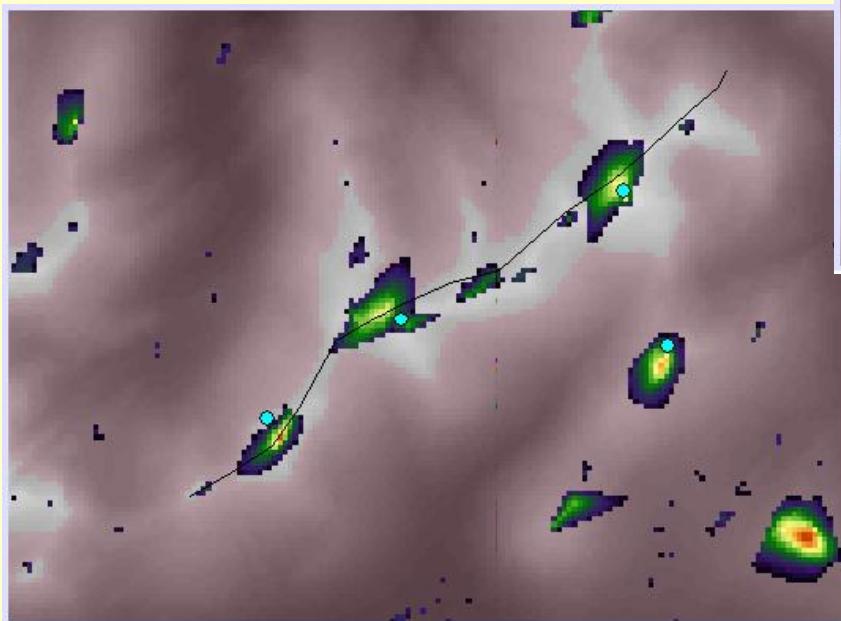
Type 2 Fuzzy Set  
of Ben Nevis

# Alternate Resolution Realisations of the Grey Corries



# Bounds

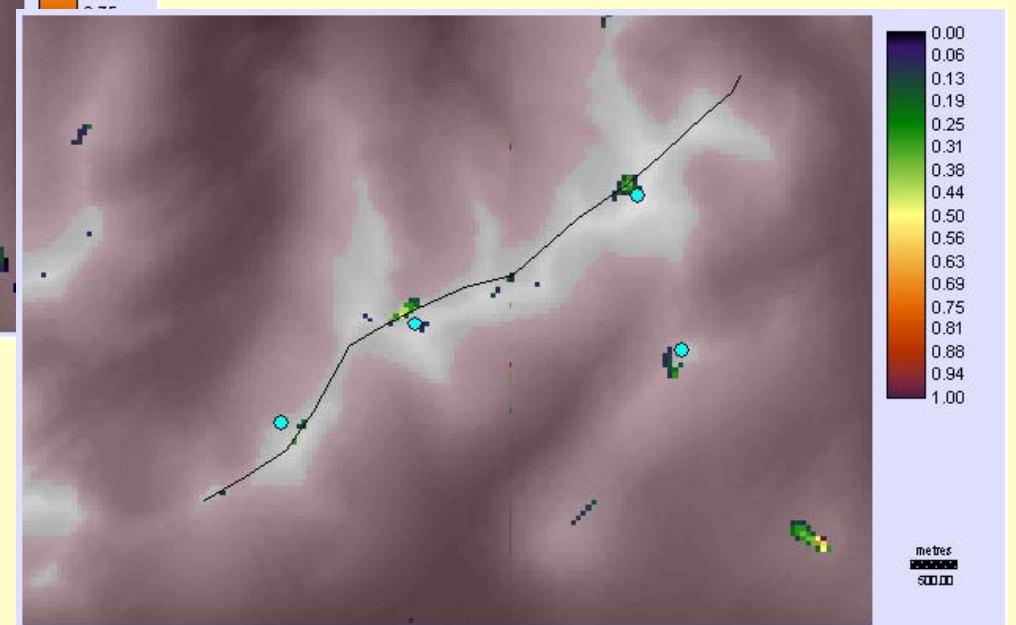
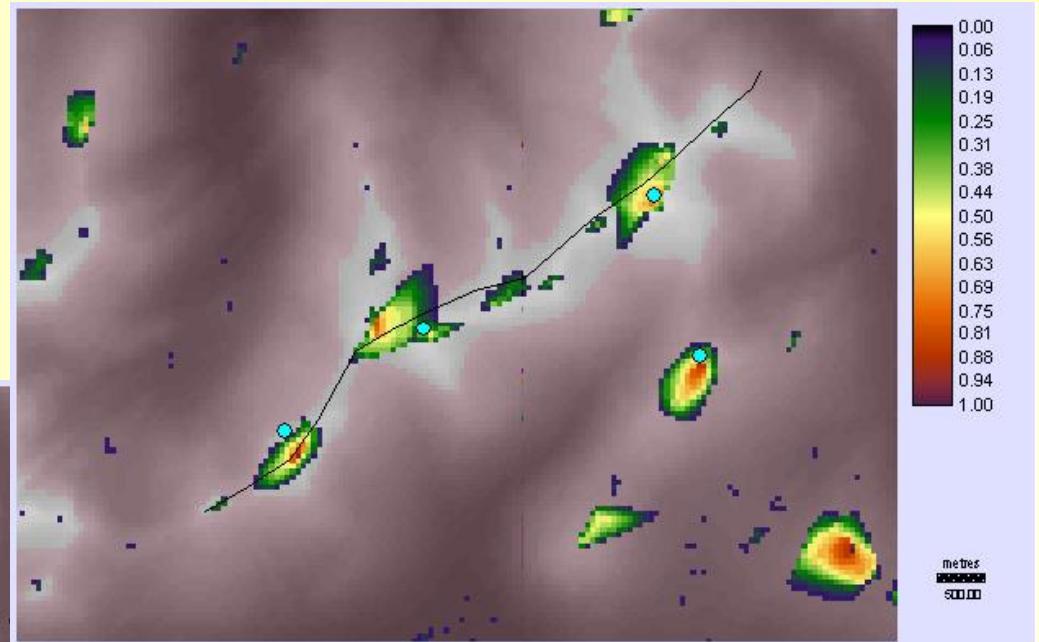
Mean Membership



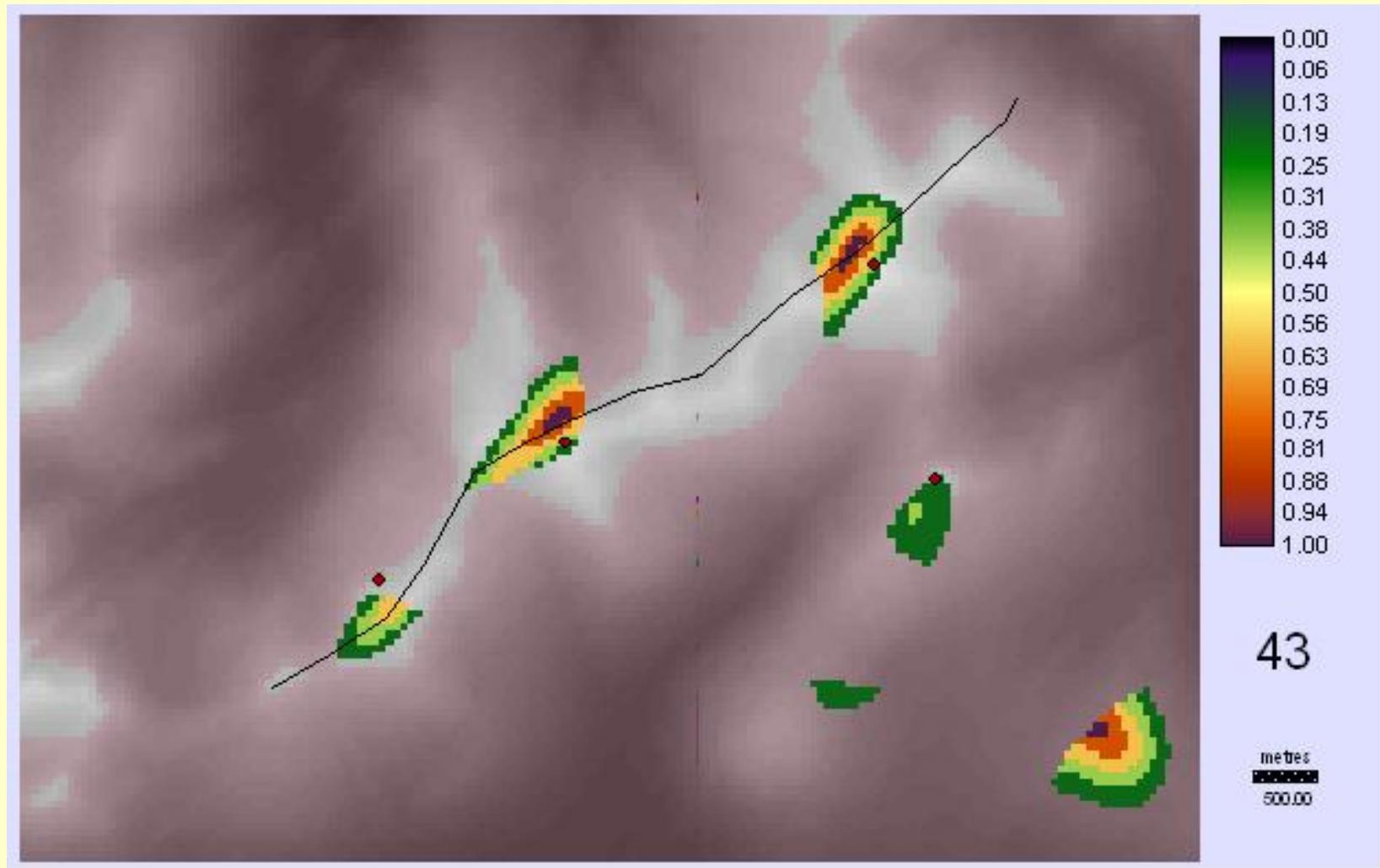
Type 2 Fuzzy Set  
of Grey Corries

Minimum Membership

Maximum Membership

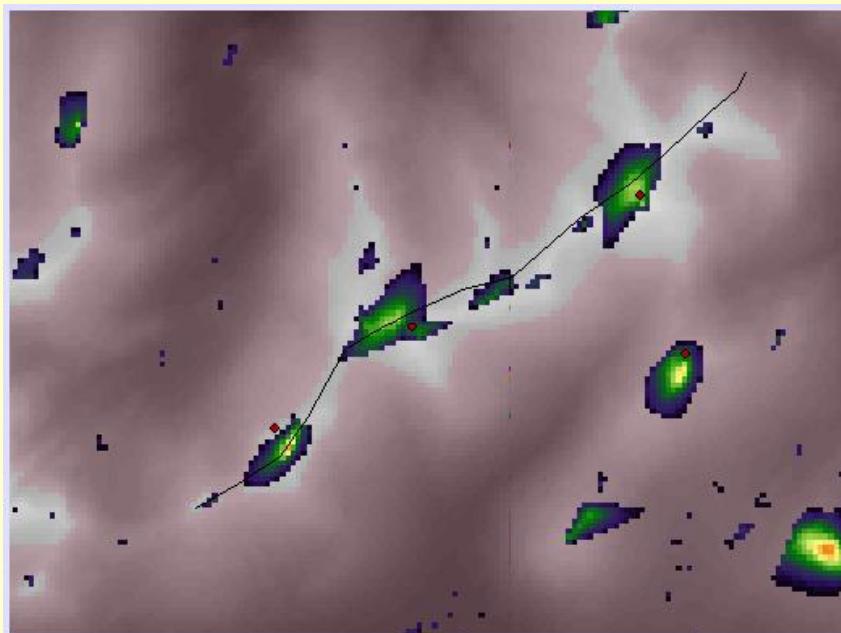


# Alternate Slope Threshold Realisations of the Grey Corries

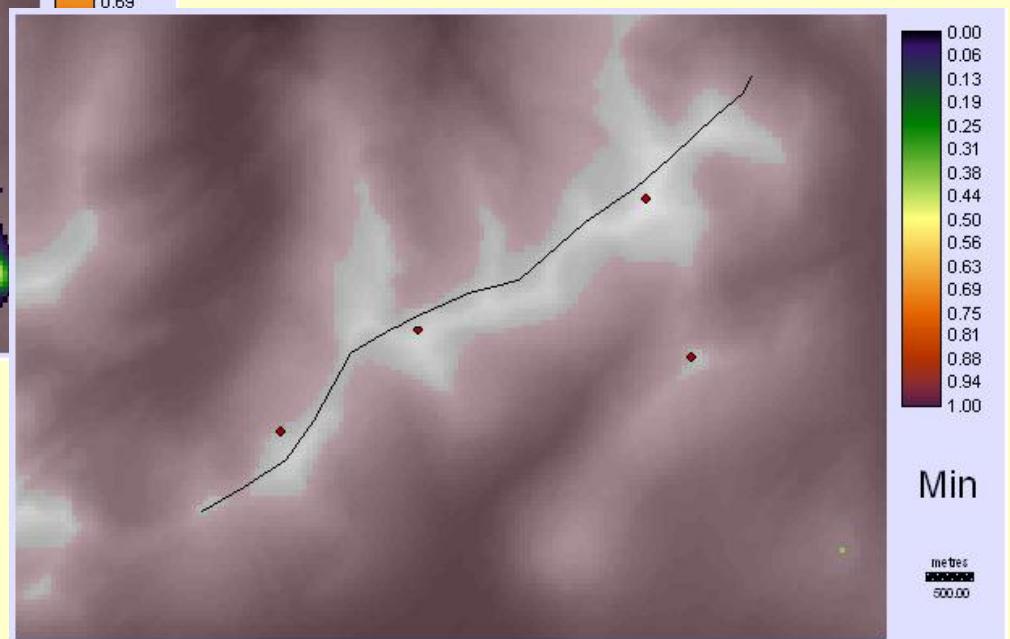


# Bounds

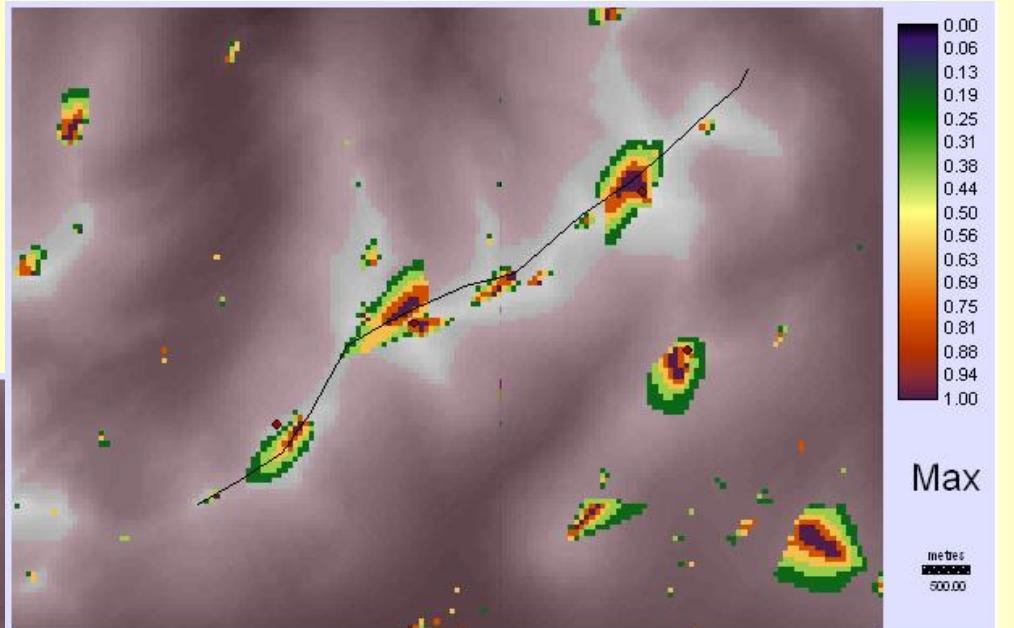
Mean Membership



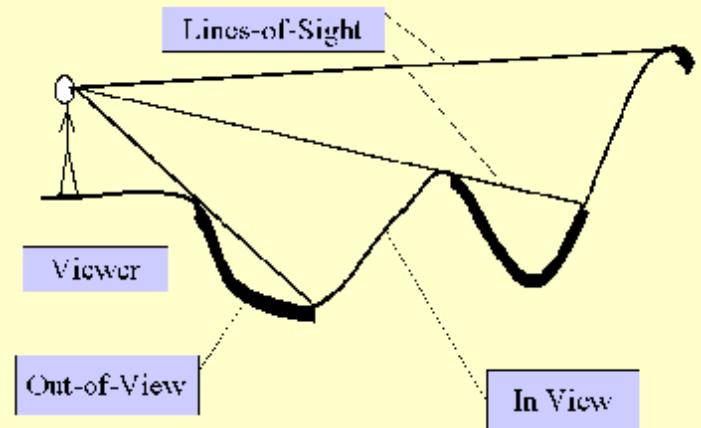
Minimum Membership



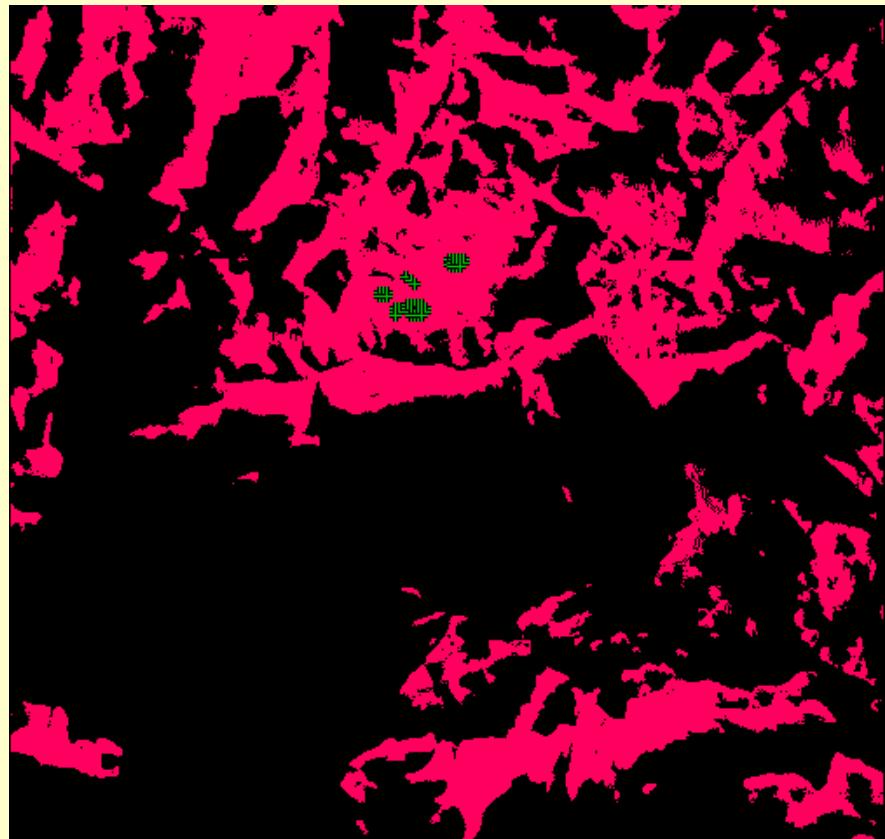
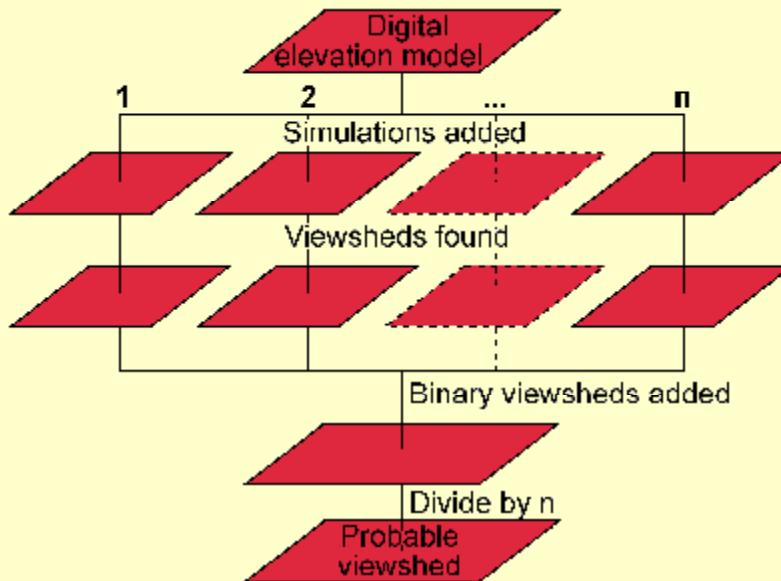
Maximum Membership

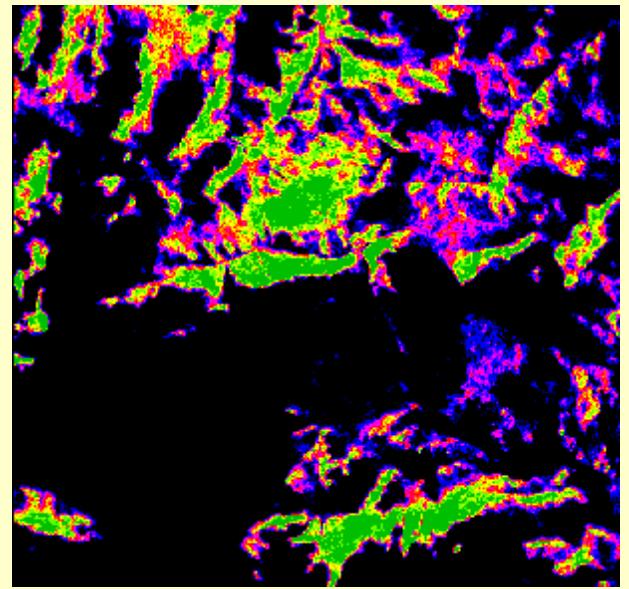
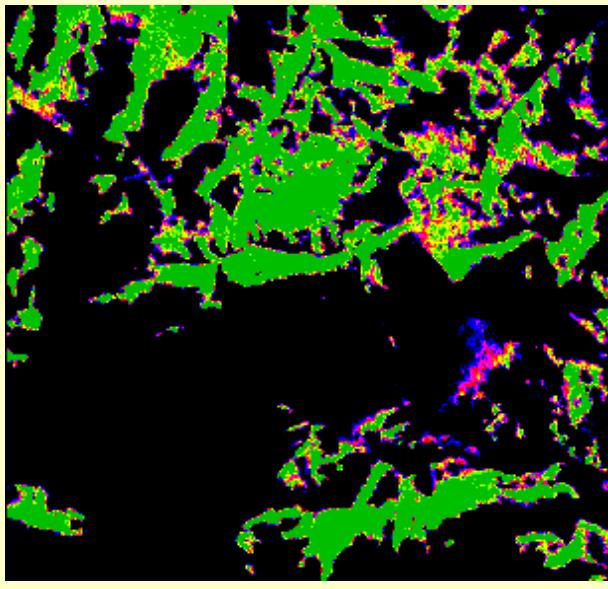
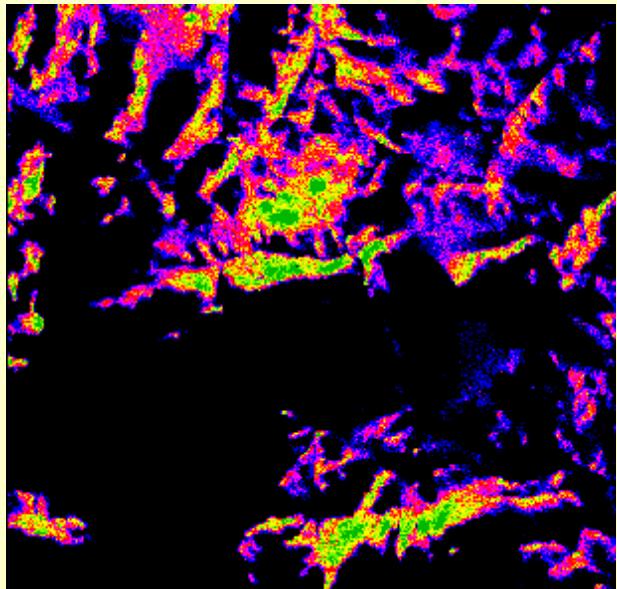
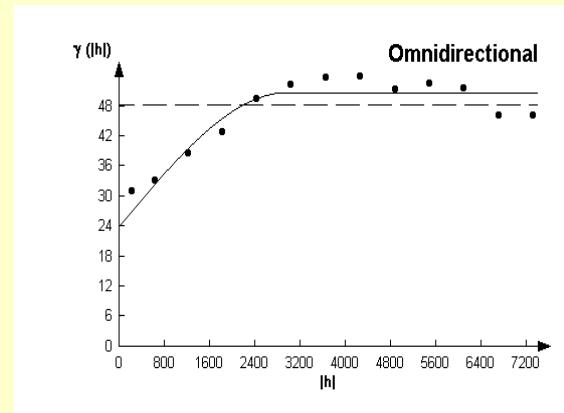
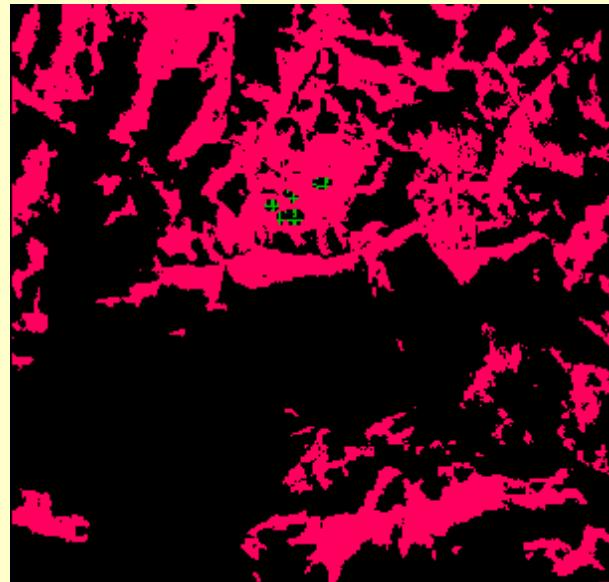
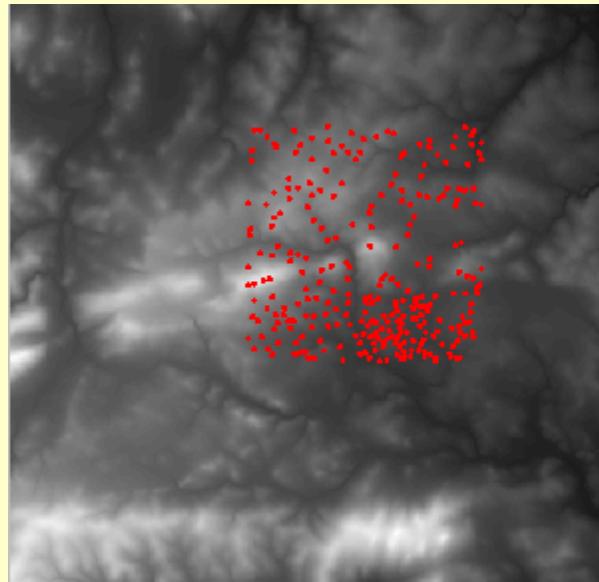


# This is different from Higher order probabilistic uncertainty



## Probable Viewshed





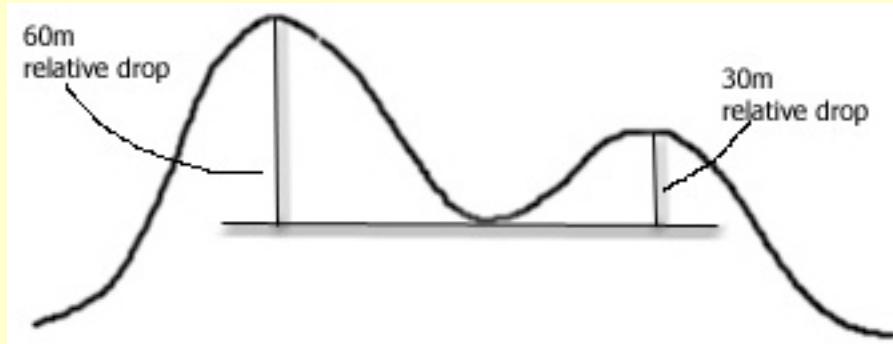
# Semantic Uncertainty - Ambiguity

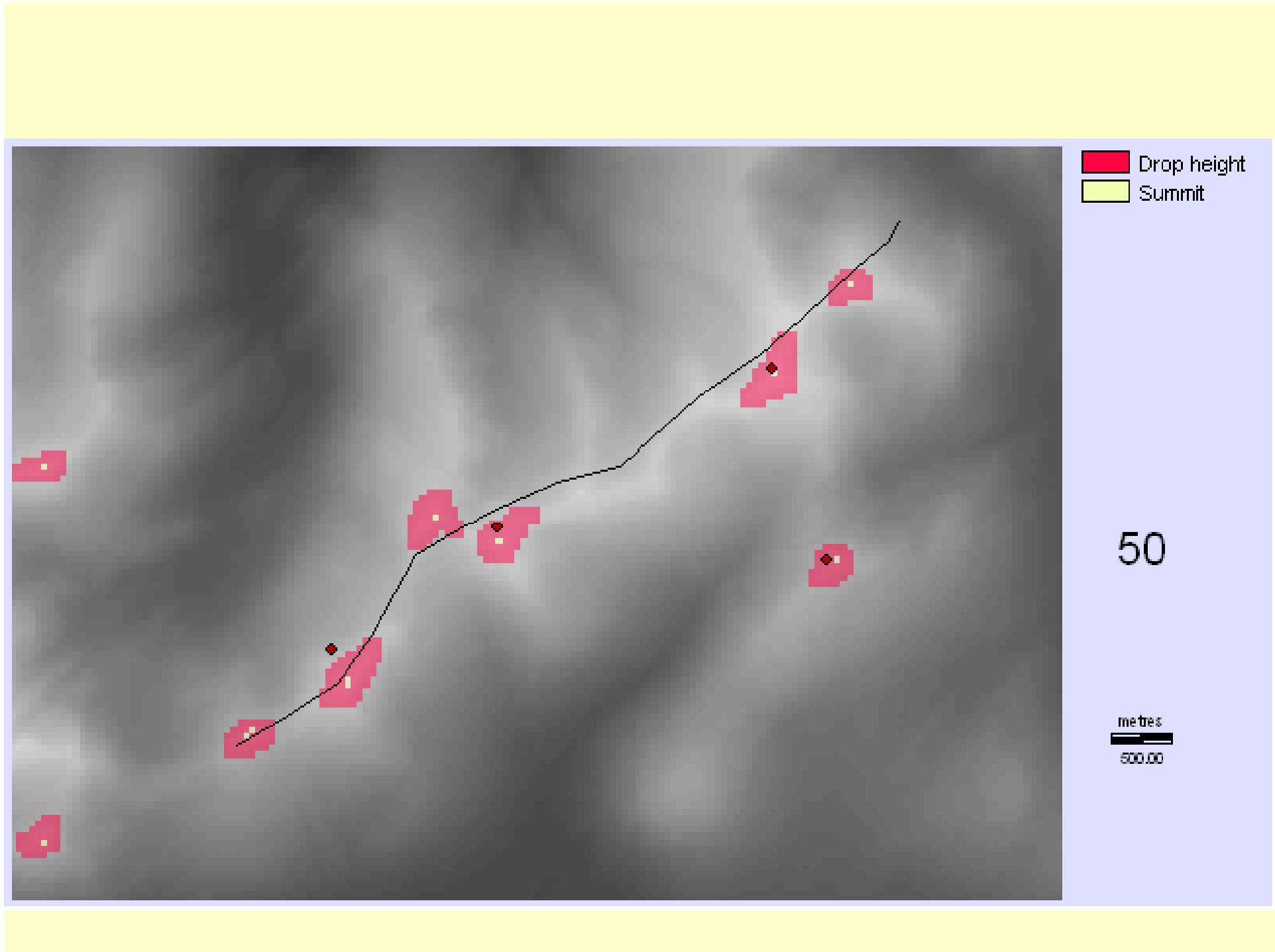
- What if we call the same thing different things?
- Or call two things we are agree are different the same?

**OR DISCORD**

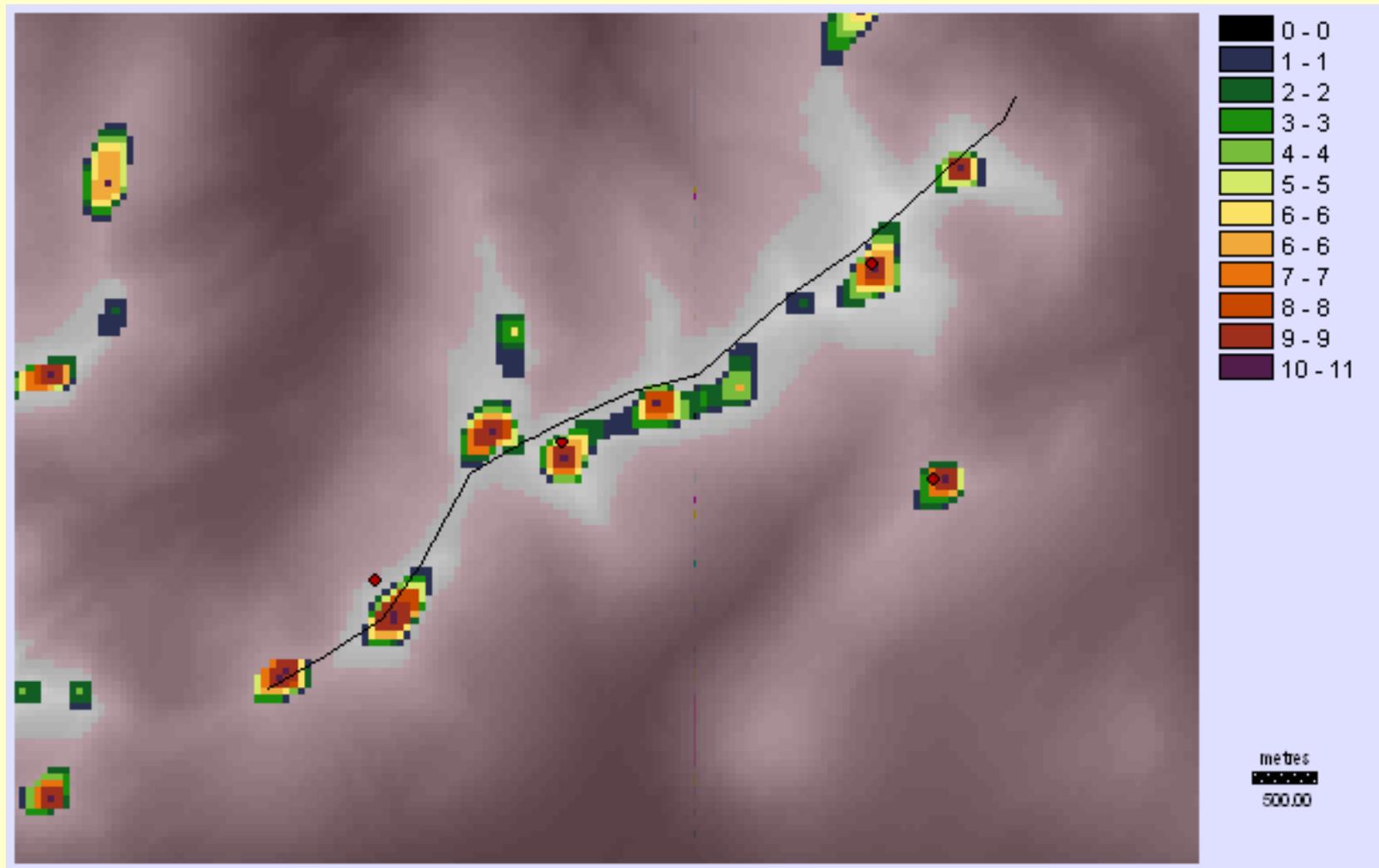
# Reflection

- Peakness is problematic (moving peaks)
- Therefore we redefine precise summits on the basis of relative drop from the highest point



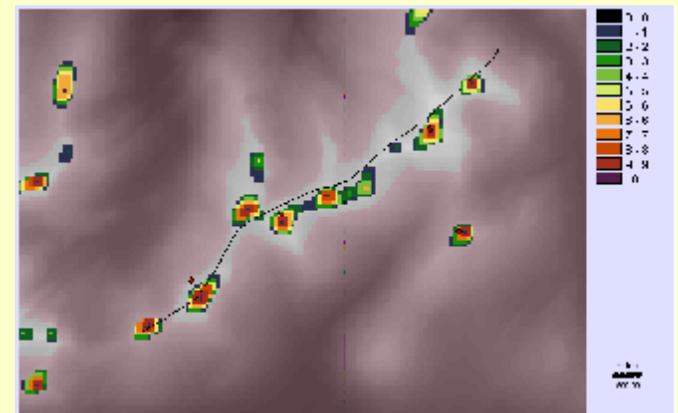
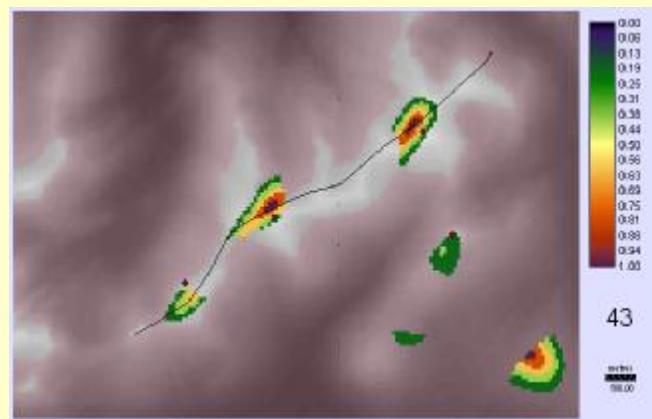
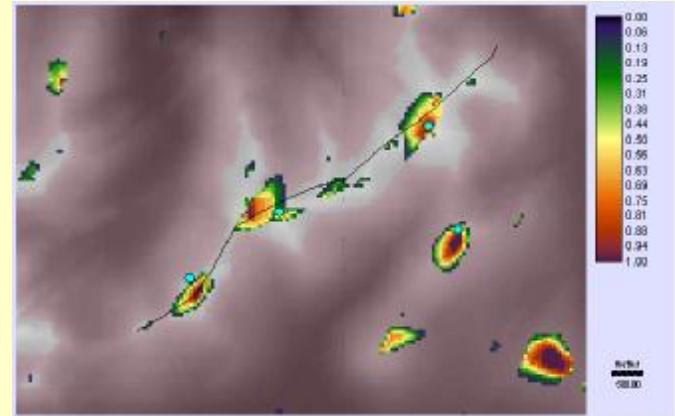


# Summits and 50m Drops



# Alternative Algorithmic Semantics

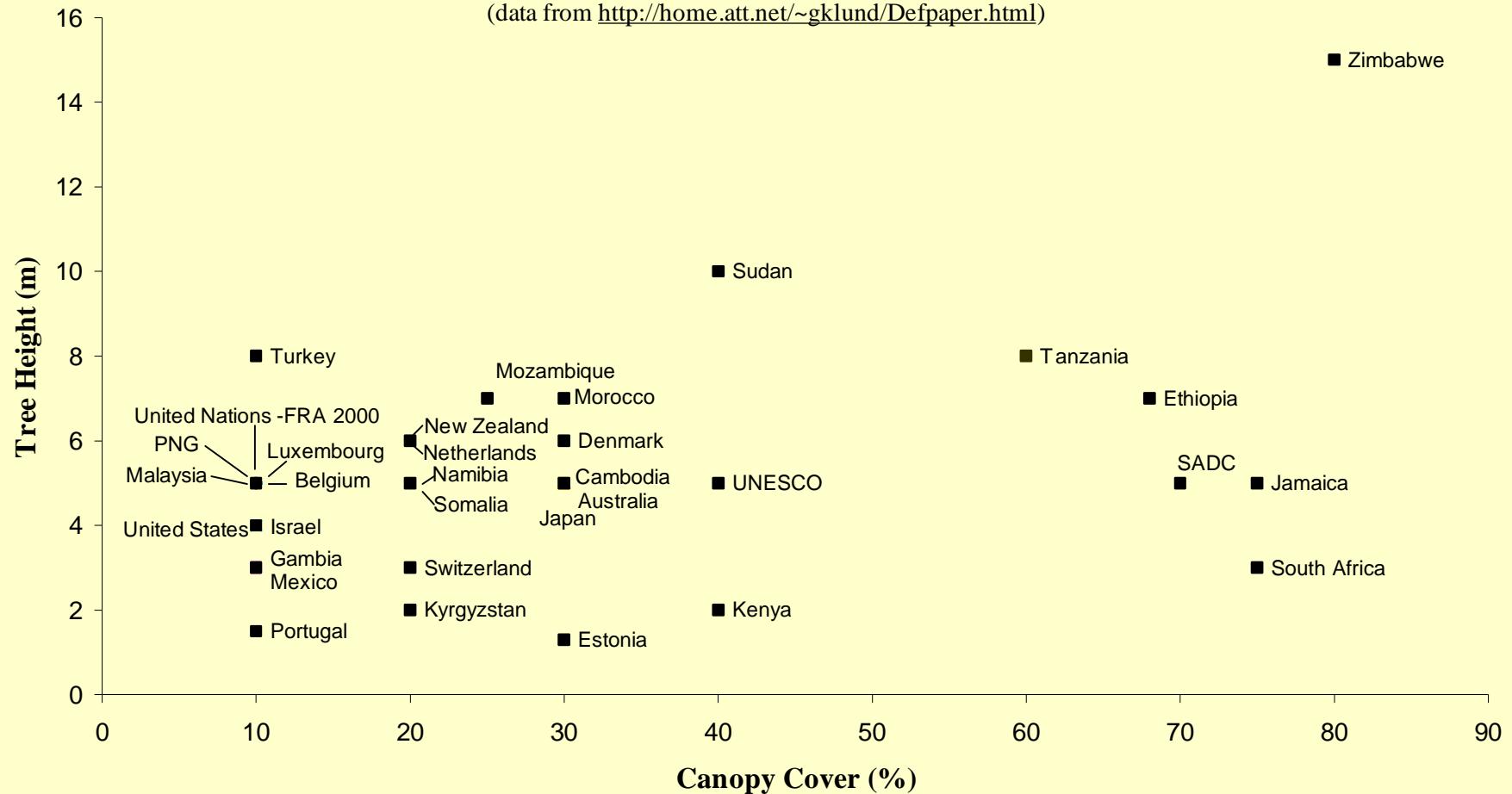
- Peaks
  - Resolution
  - Slope Threshold
- Drop height
- Inverted Watersheds?
- Further definitions
- All discordant vague definitions



# Other Semantic or Ontological Confusions

## Minimum physical requirements of a "Forest"

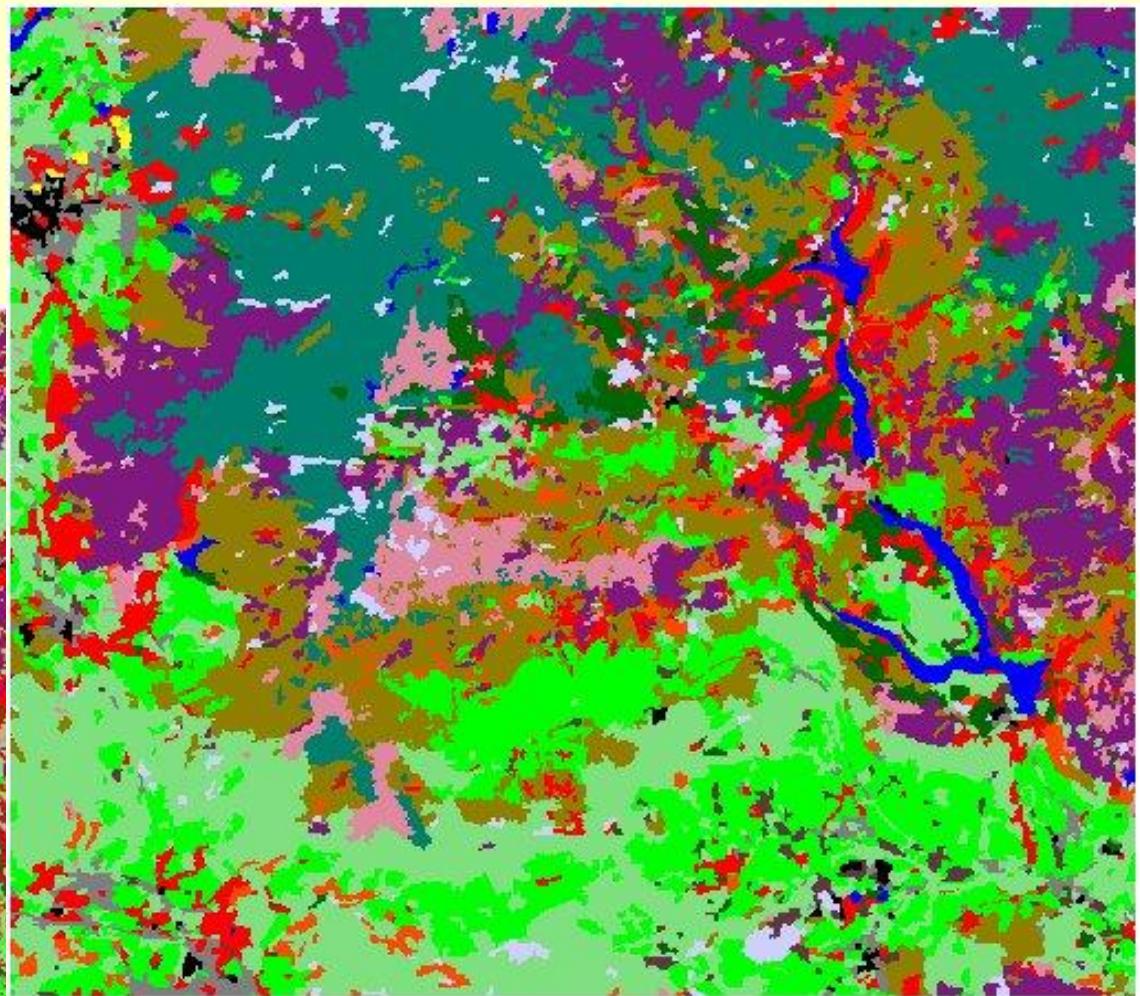
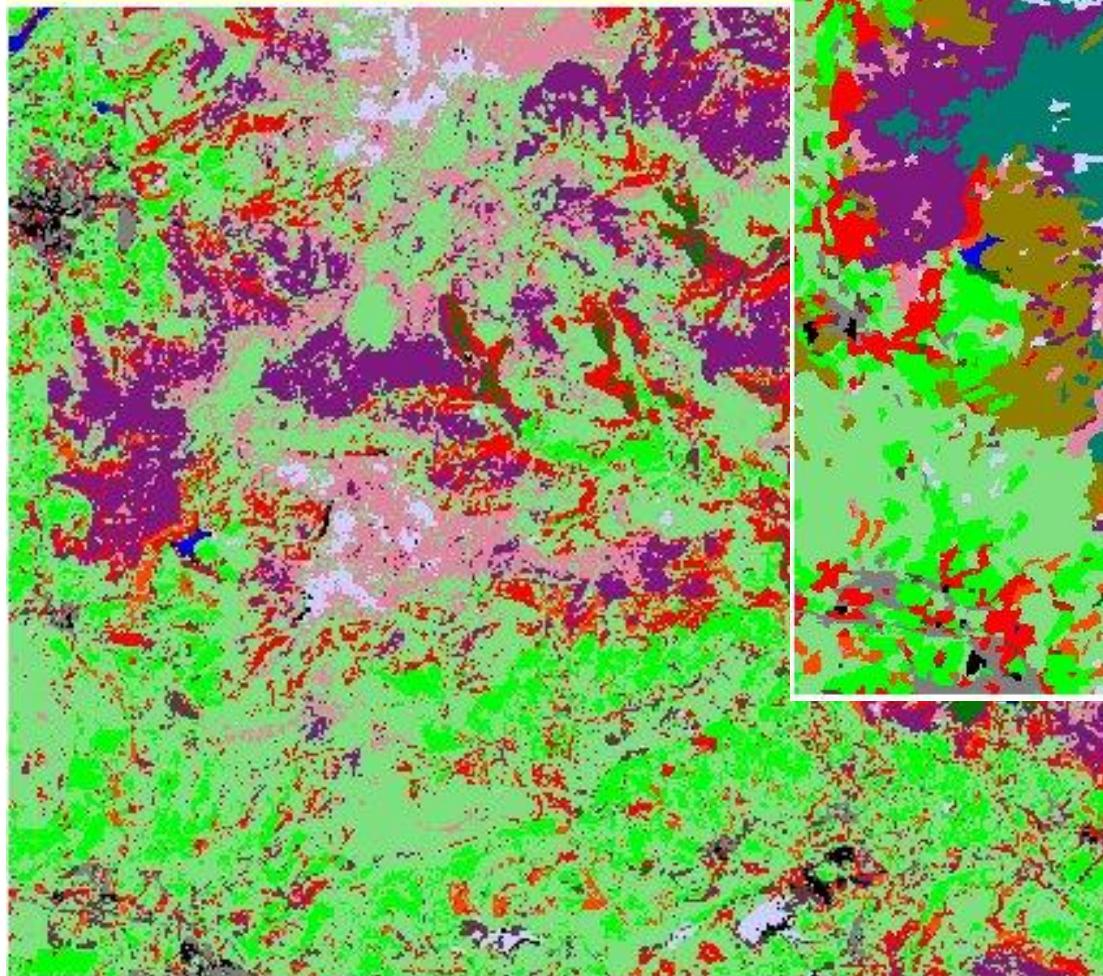
Note most countries do not define their forests in this way  
(data from <http://home.att.net/~gklund/Defpaper.html>)



# Land Cover Mapping

- Within EU funded REVIGIS project
- 1990 LCMGB vs LCM2000:
  - Landsat TM, Centre for Ecology & Hydrology
- Same phenomenon but changes:
  - Representation (raster vs. parcel structures)
  - Conceptualisation eg Classification
    - 1990: 25 Target classes
    - 2000: 26 Broad Habitats
  - Technology (LCM2000: extensive object level meta-data)
  - Objectives (Science and Policy)
- Endemic problem
  - USGS-LCDS / MODIS / GLC
  - National soil classifications ....
- This is a problem if you are trying to map change in the landscape

LCMGB 1990

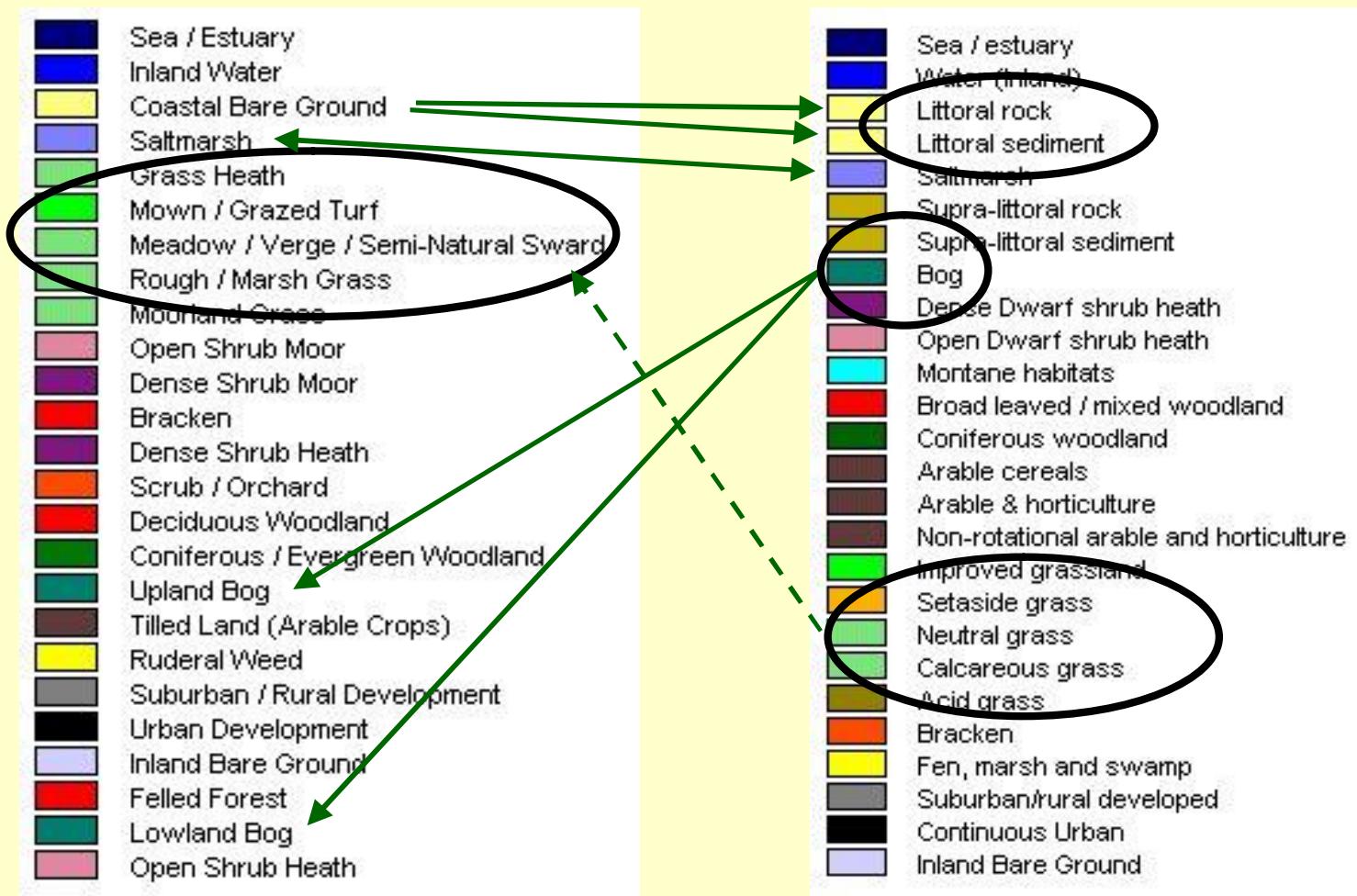


LCM 2000

# But what is a “bog”?

- LCMGB
  - 12 pixels (<1 ha) in SK tile
    - permanent waterlogging, resulting in depositions of acidic peat
    - mostly herbaceous communities of wetlands with permanent or temporary standing water
    - Lowland Bogs: carry most of the species of upland bogs, but in an obviously lowland context, with *Myrica gale* and *Eriophorum* spp. being highly characteristic.
    - Upland bogs: have many of the species of grass and dwarf shrub heaths
    - characterised by water-logging, perhaps with surface water, especially in winter. species such as bog myrtle (*Myrica gale*) and cotton grass (*Eriophorum* spp.) in addition to the species of grass and dwarf shrub moorlands.
- LCM2000
  - 120728 pixels (75 km<sup>2</sup>) in SK tile
    - Bogs include ericaceous, herbaceous and mossy vegetation in areas with peat >0.5 m deep; ericaceous bogs are distinguished at subclass level. Inclusion of Ericaceous bogs contrasts with LCMGB 1990 where bogs were herbaceous or mossy in seasonal standing water

# Concepts



LCMGB 1990

LCM 2000

# Remaining Problems

- Formalising the different natures of uncertainty is fundamental
- Visual clues for the types of uncertainty
  - Object level
  - Uncertainty taxonomy
  - Unaddressed
- Visualising higher dimensions of uncertainty
- Visualising discord and semantic uncertainty