

Visualizing Uncertainty: Computer Science Perspective

Ben Shneiderman, Univ of Maryland, College Park

Alex Pang, Univ of California, Santa Cruz

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What do we mean by uncertainty?

Why is this an issue now?

Sources of uncertainty

- Æ Measurement problems
- Æ Ranges/Summaries
- Æ Missing data
- Æ Human ratings
- Æ Potential deceptions
- Æ Privacy protection
- Æ Risk assessments
- Æ Forecasts

- § Scientific data
- § Intelligence sources
- § Statistical analyses
- § Medical images
- § Gene expression
- § Simulations
- § Financial models
- § Weather
- § Consumer ratings

Visualizations

- | Text, statistical measures...

SciViz

- | 1D: Lists, documents, numeric ranges...

- | 2D: Geographic Info

- | 3D: Scientific Visualization

InfoViz

- | Multi-Variate: Information Visualization

- | Temporal: Patient histories, web logs ...

- | Tree: Taxonomies, org charts, directories ...

- | Network: Social, communication...

Text: Statistical uncertainty

I Text

Poll	Dems	Reps
Bush	14%	81%
Kerry	79%	7%
Margin of error +/- 3%		

I 1D

I 2D

I 3D

I Multi-V

I Temporal

I Tree

I Network

	Frustration (N=372)
Time Variables	
Time Lost (Incident)	** .293
Time to Fix (Incident)	** .233
Computer Years	-.041
Hours per Week	* -.124
* = p<.05 ** = p<.01	

	Rain inches	Reliability
SW	1.0	low
SE	1.5	high
NW	1.2	low
NE	0.8	med

Risk/Danger vs. Trust/Validity/Security

I Text

I 1D

I 2D

I 3D

I Multi-V

I Temporal

I Tree

I Network

	Risk
Municipal Bonds	low
Blue Chip Stocks	med
Tech Stocks	high
Real Estate	med



Highly Unlikely	Unlikely	About Even	Likely	Highly Likely
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1D: Ranges, variations & forecasts

- I Text

- I **1D**

- I 2D

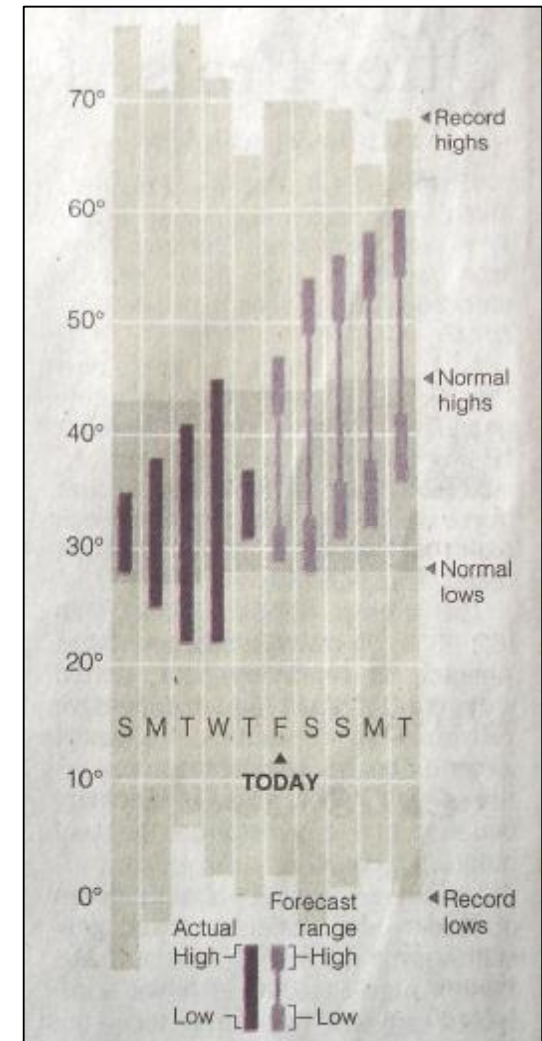
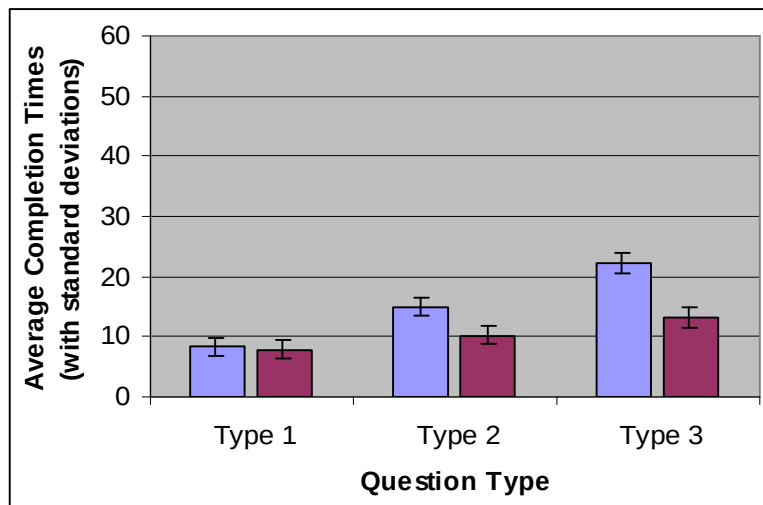
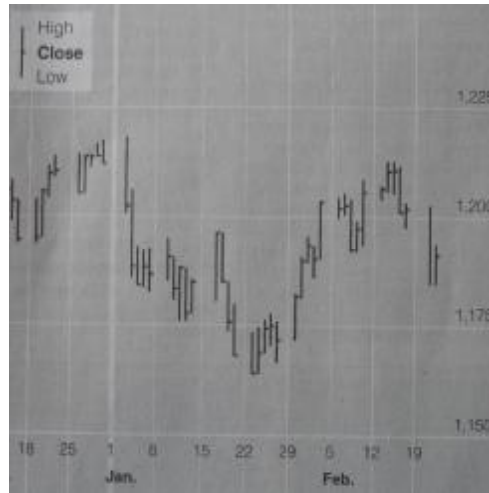
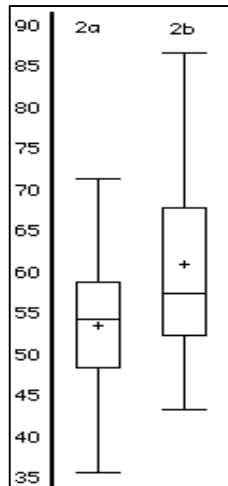
- I 3D

- I Multi-V

- I Temporal

- I Tree

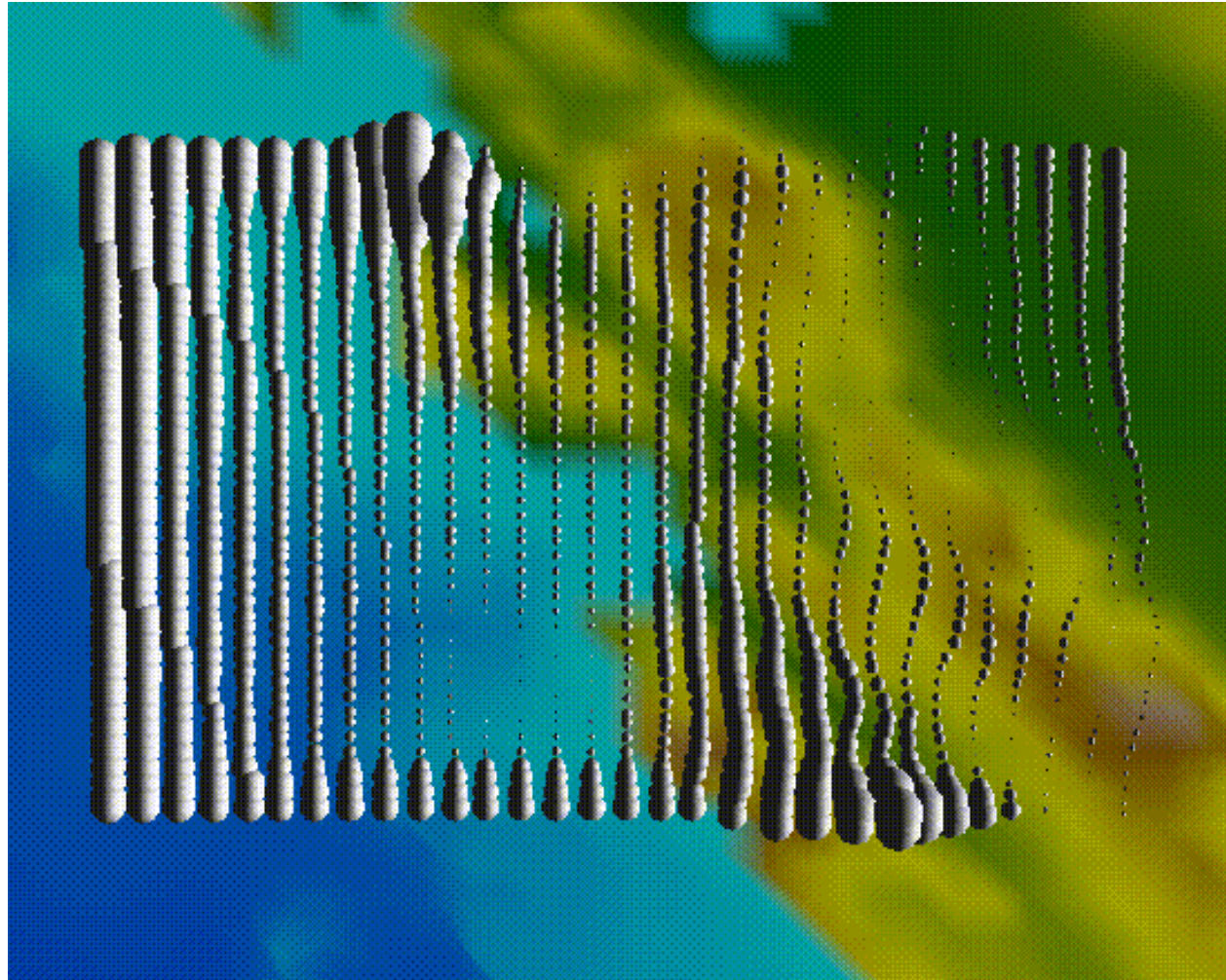
- I Network



2D: Ball glyphs

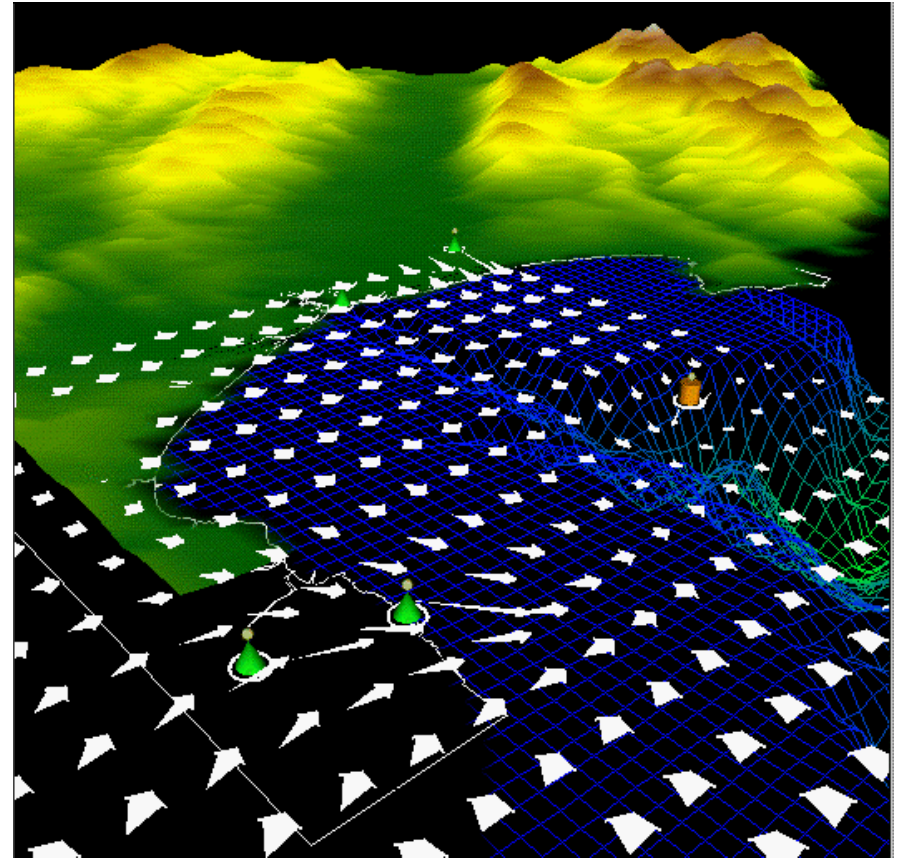
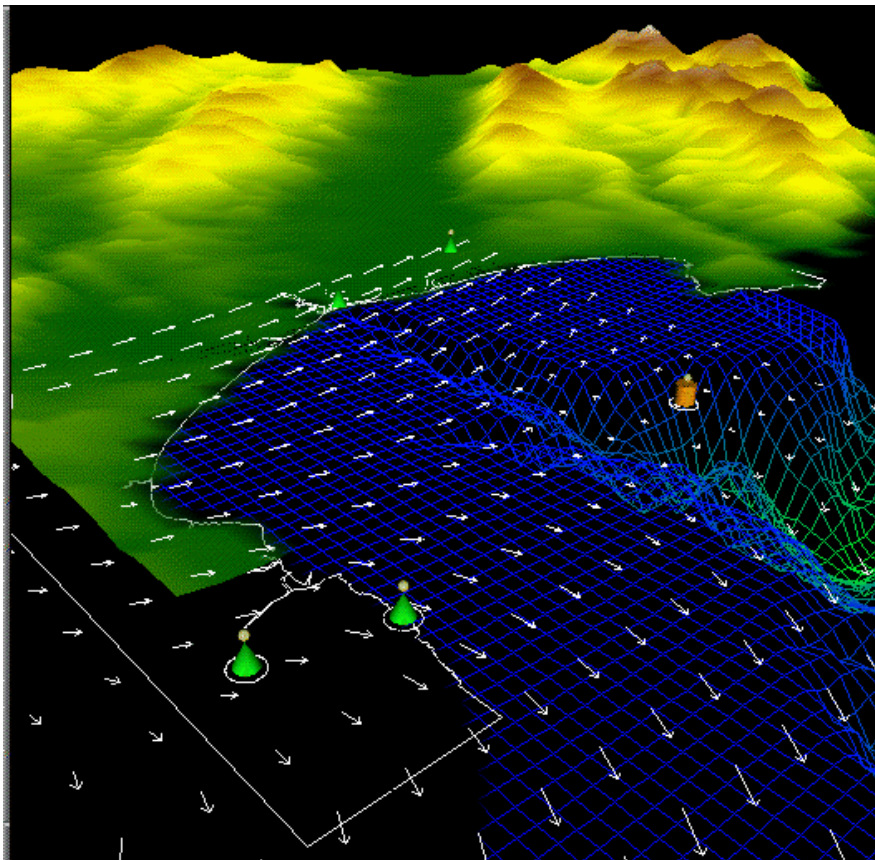
Delta (observation - forecast)

- | Text
- | 1D
- | 2D
- | 3D
- | Multi-V
- | Temporal
- | Tree
- | Network



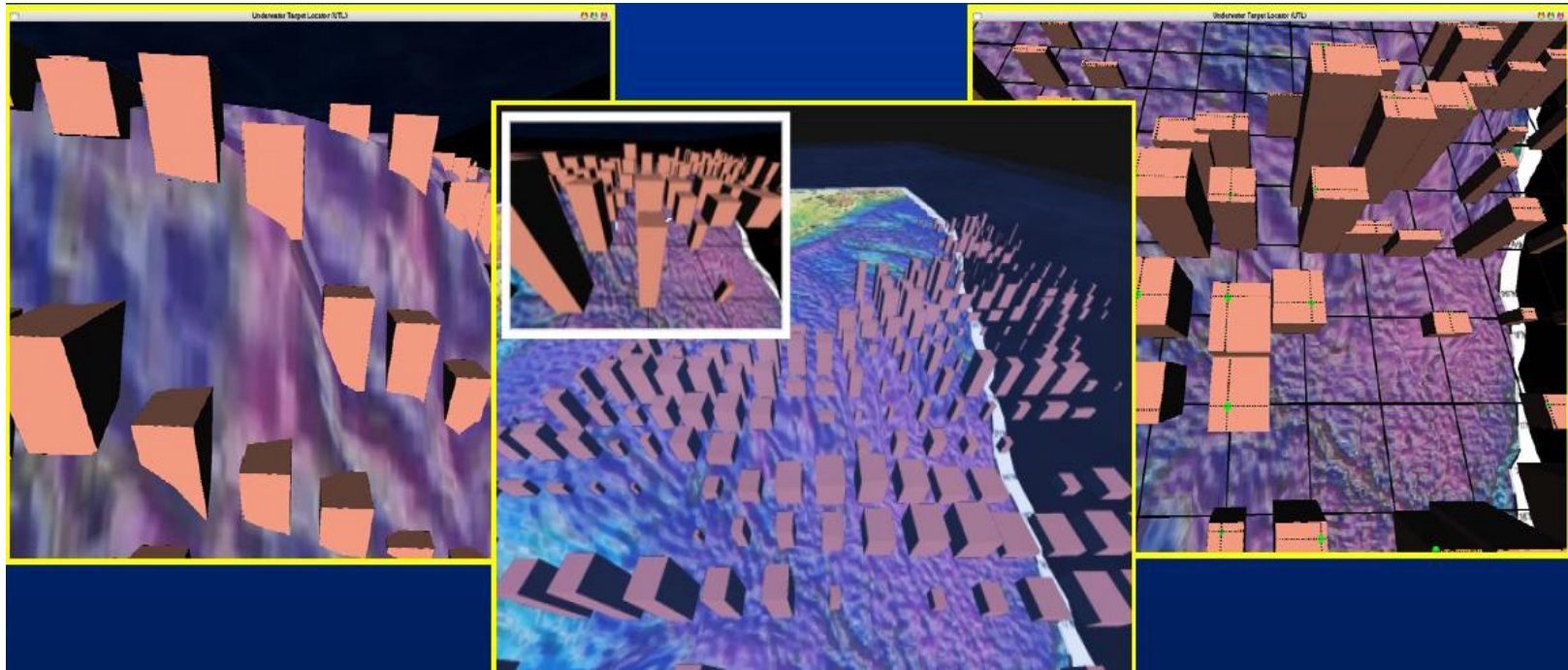
<http://www.cse.ucsc.edu/research/slv/assim.html>

2D: Arrow glyphs (Direction & velocity)



<http://www.cse.ucsc.edu/research/avis/unvis.html>

2D: Box glyphs



Schmidt et al., 2004, Underwater Environmental Uncertainty, IEEE CG&A
<http://csdl.computer.org/comp/mags/cg/2004/05/g5056abs.htm>

2D: Grid with transparency/shading

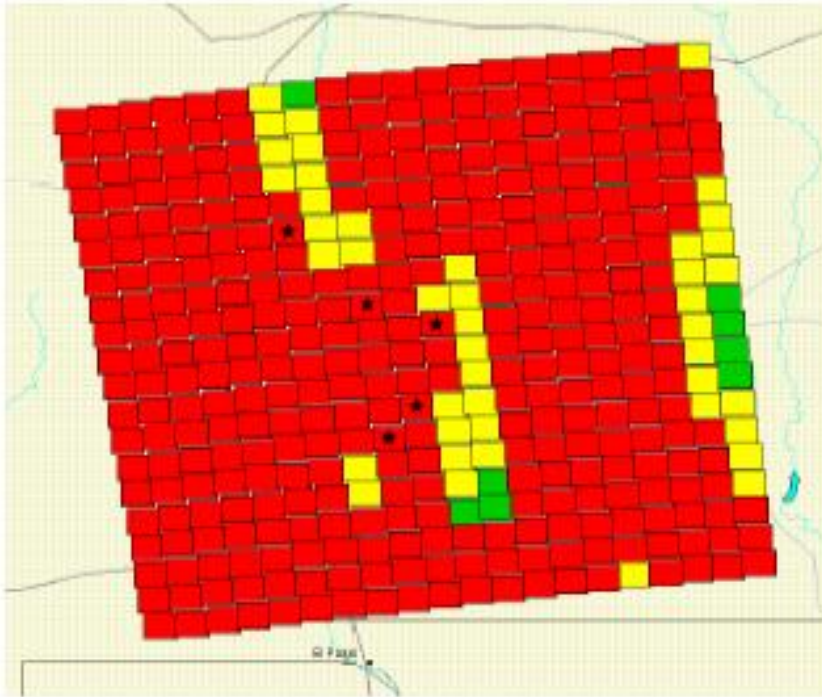


Figure 5: Current IWEDA-like spatial display showing the cloud ceiling at one particular time over the PUMAR domain. The black stars were points of interest during the T-UAV demonstration scenario. The red, yellow, and green "pixels" were assigned based on operational T-UAV cloud ceiling sensitivities.

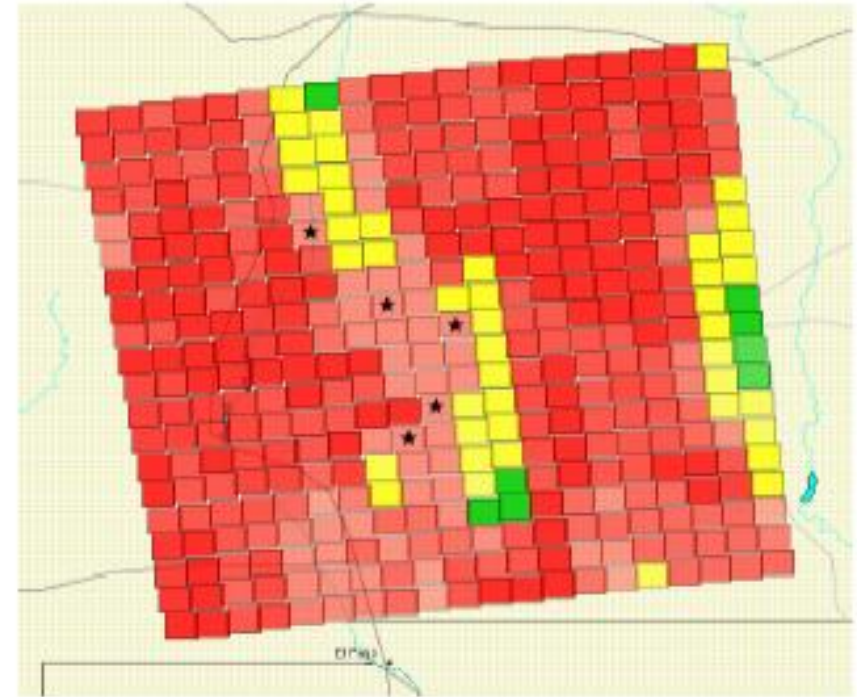
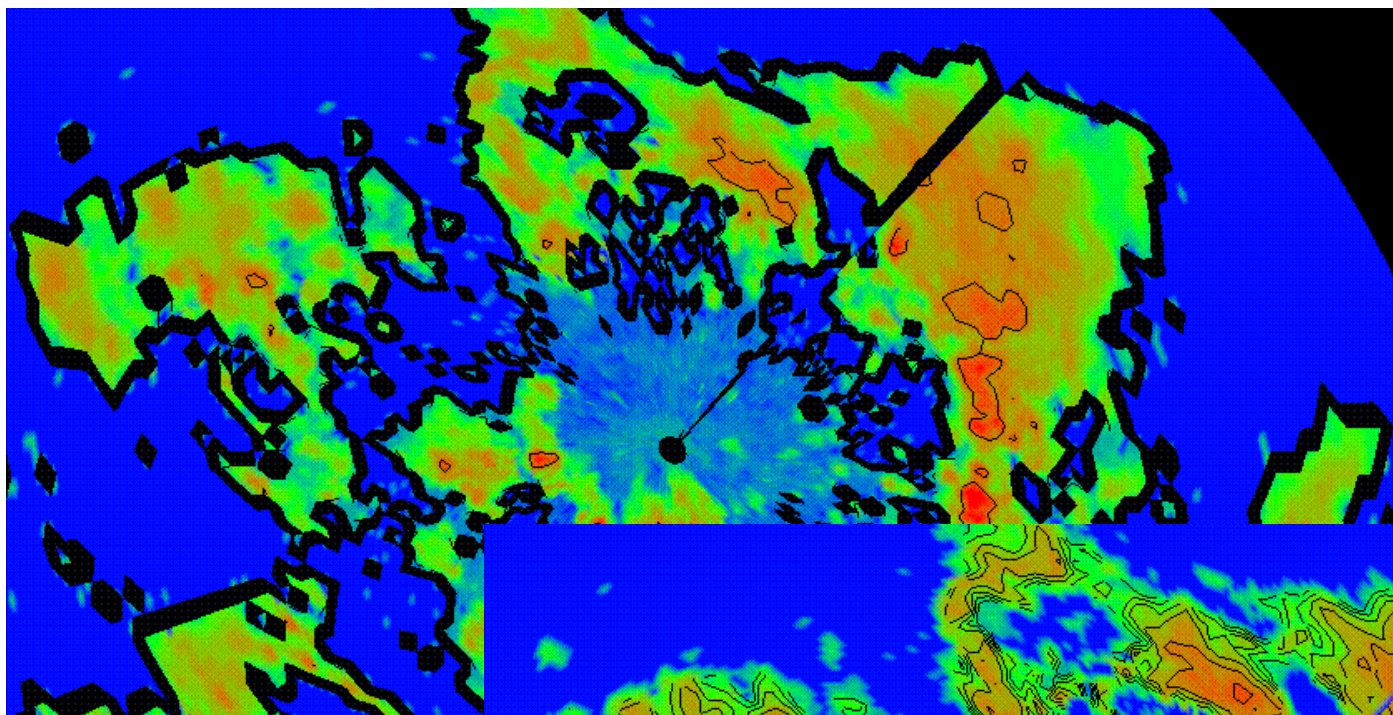


Figure 6: The same display as in Fig. 4, except for the application of cognitive engineering techniques to change the hue (color) and transparency of the cloud ceiling impacts based on the uncertainty of the predicted cloud ceiling.

Lefevre, Pfautz & Jones

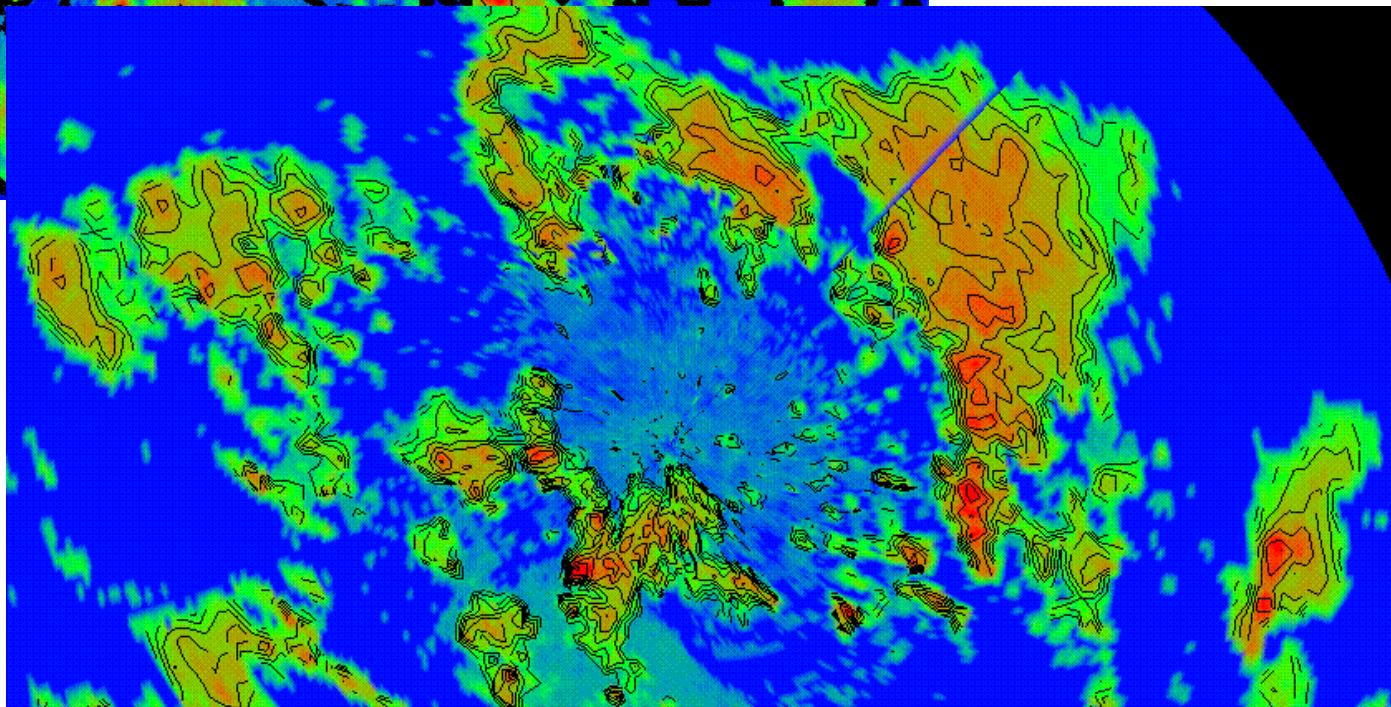
<http://ams.confex.com/ams/pdfpapers/82400.pdf>

2D: Isolines with missing values

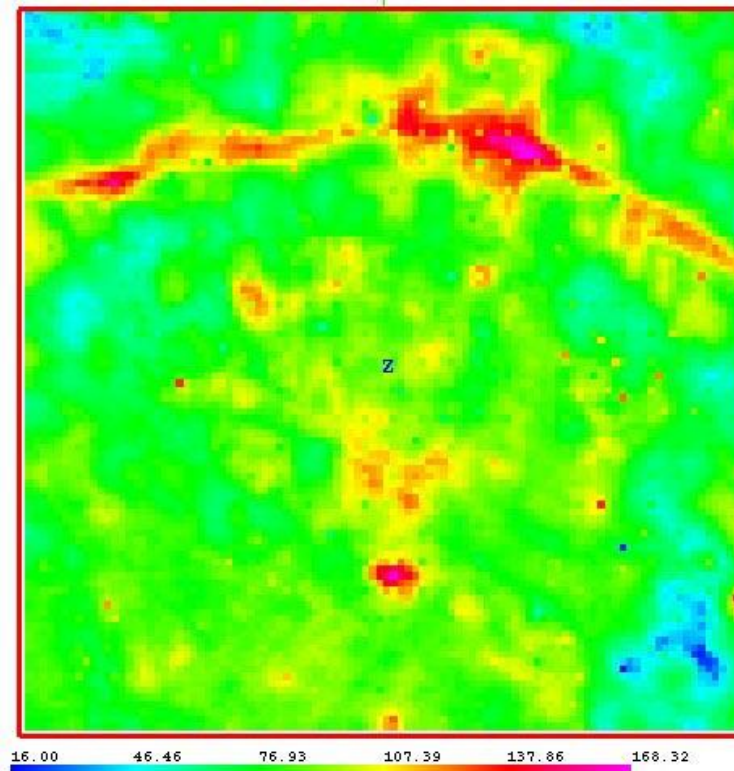


Off-the-shelf software can give incorrect contours on data with lots of missing values.

Modifications to contouring algorithm to account for large number of missing values.

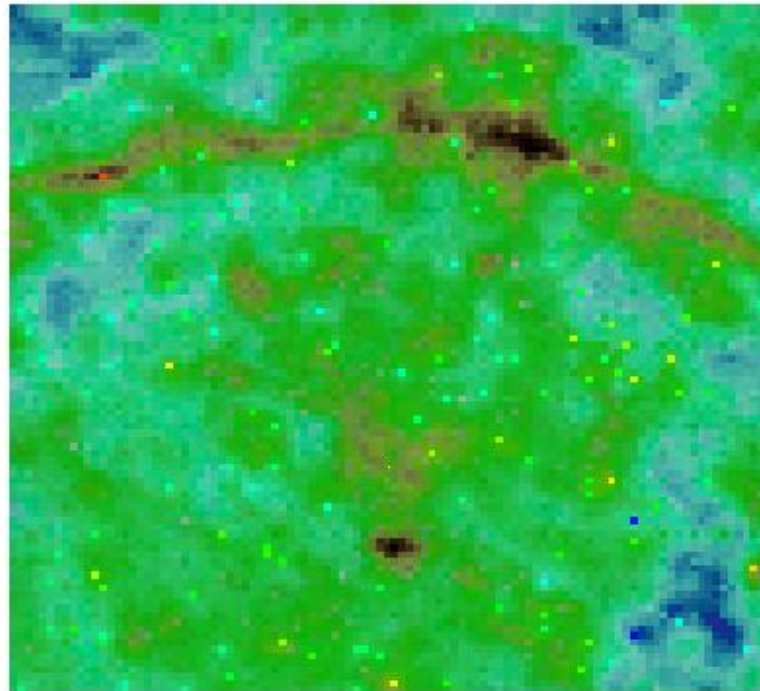


2D: Pseudocolor shows mean values

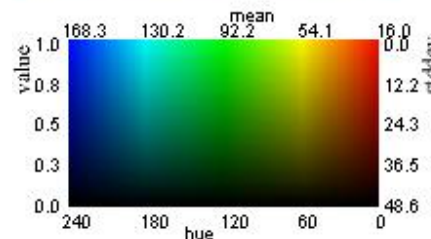


Luo, Kao & Pang, 2003, EuroVis
<http://www.soe.ucsc.edu/~pang/op.pdf>

2D: Darkness = uncertainty (high stddev)

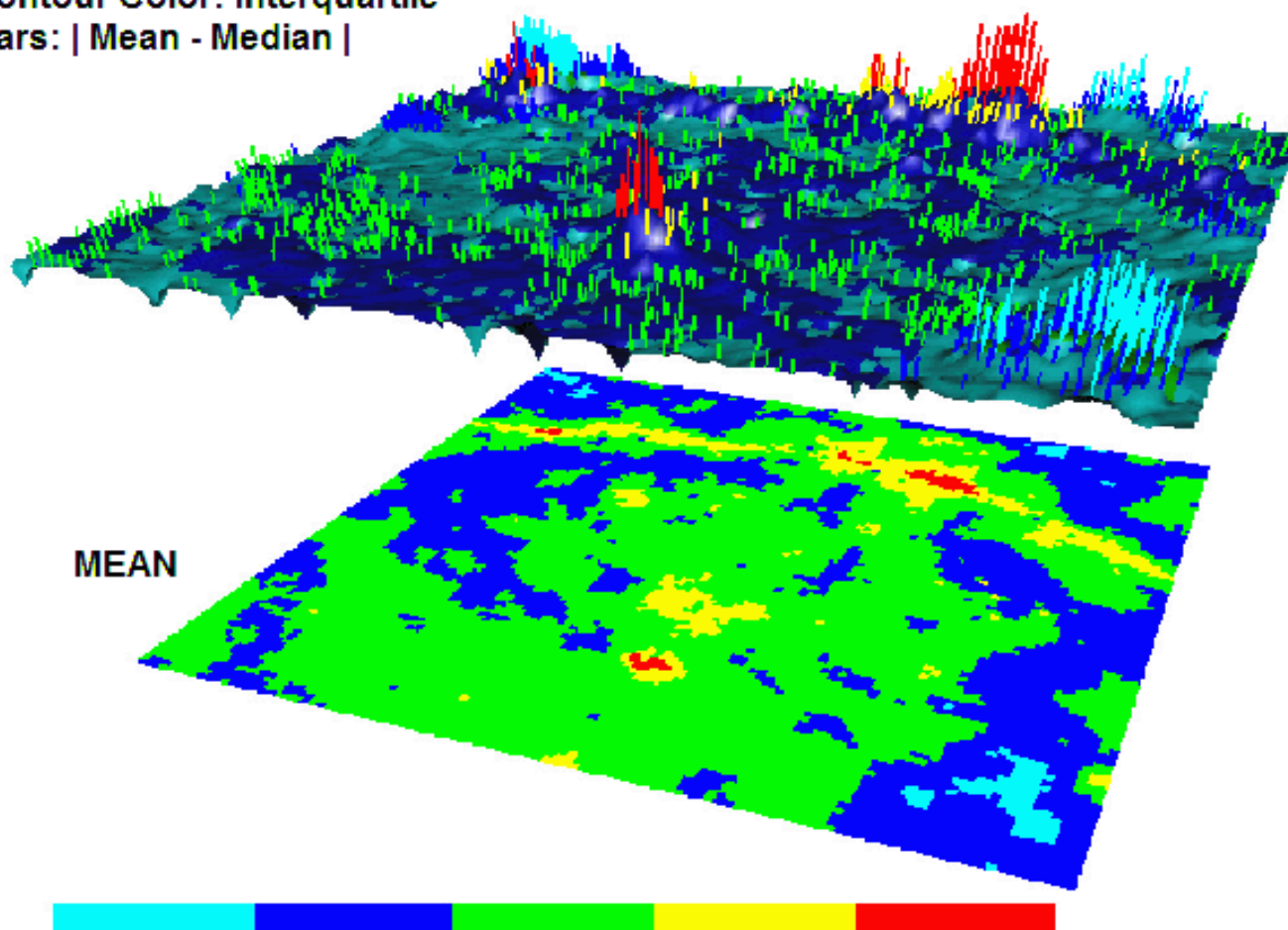


Mean = hue
Skew = 1/saturation
Stddev = 1/value



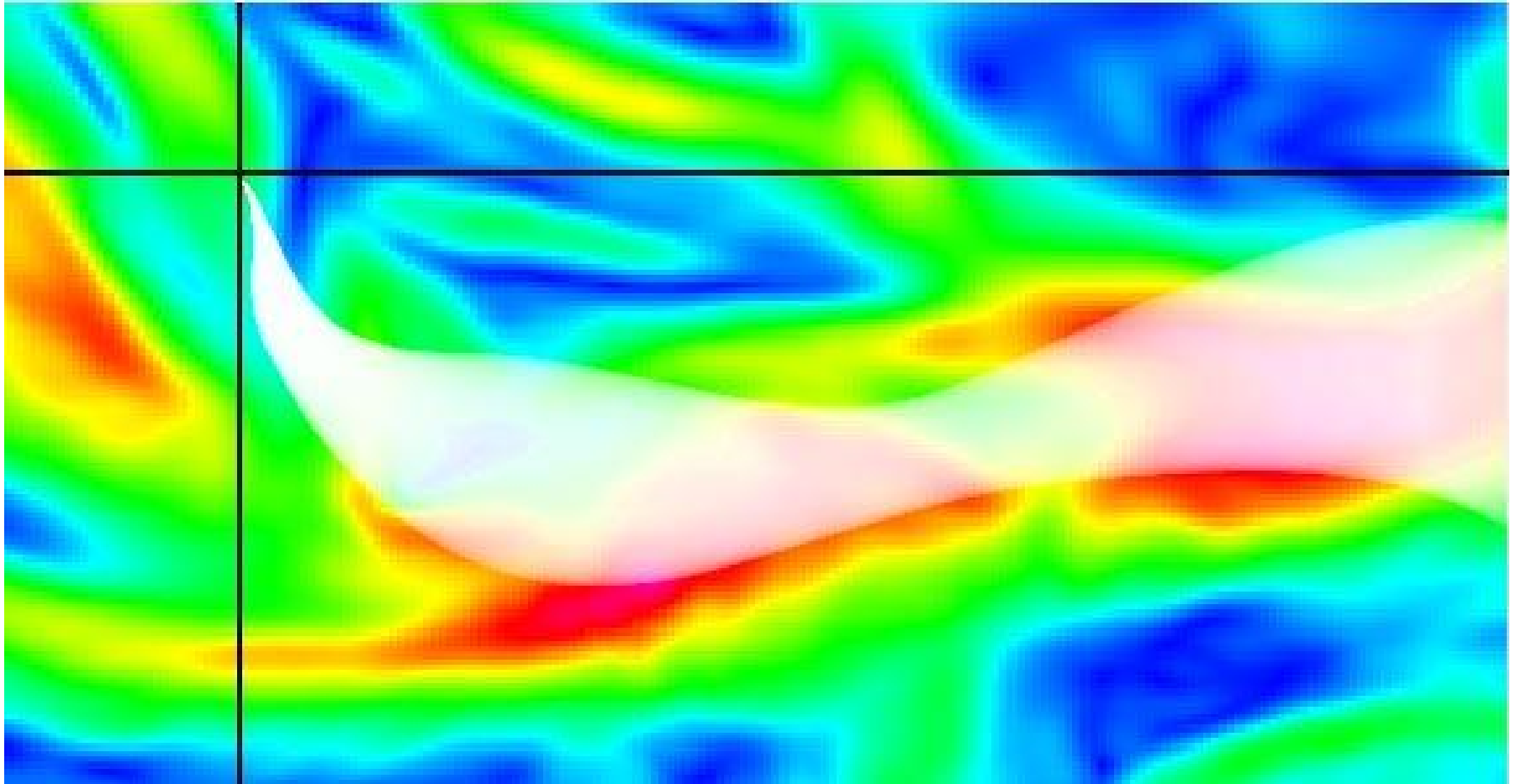
2D: Separate layer

Surface Graph: Standard Deviation
Contour Color: Interquartile
Bars: | Mean - Median |



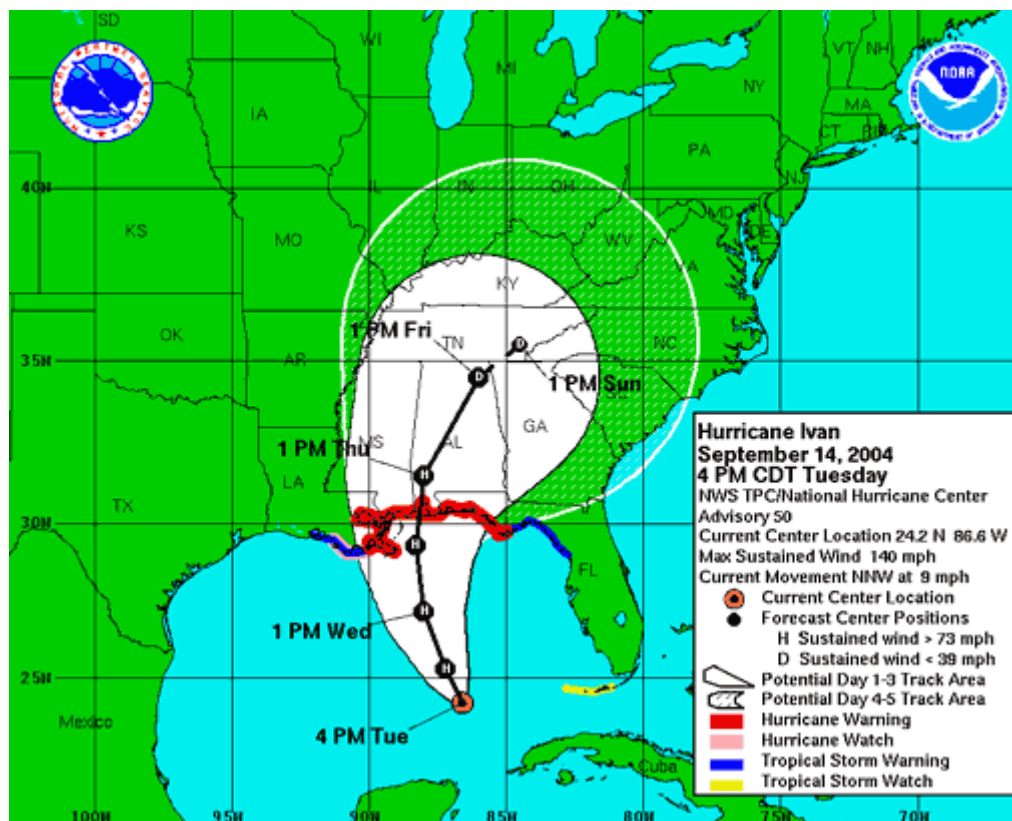
<http://www.cse.ohio-state.edu/~bordoloi/Pubs/pdfCluster.pdf>

2D: Streamlines with binwise +

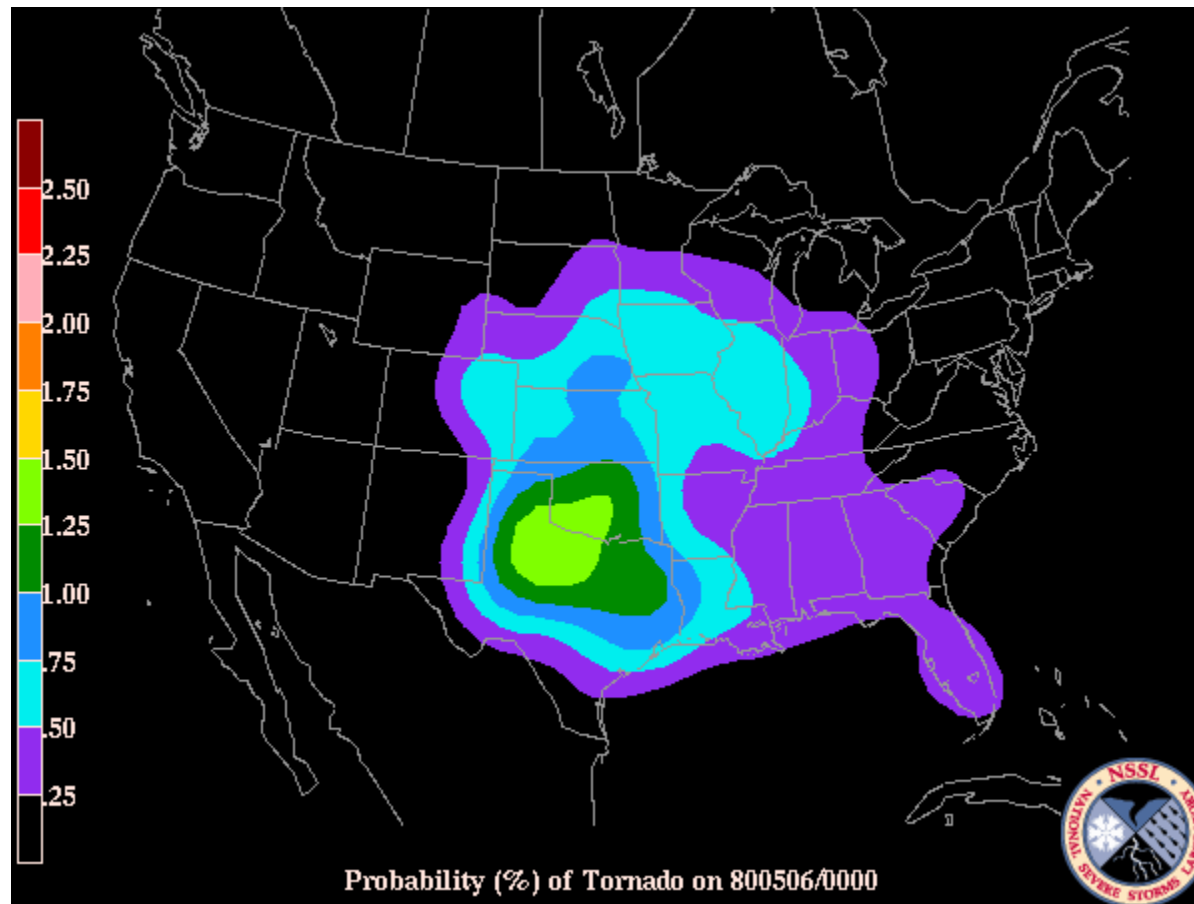


Luo, Kao & Pang, 2003
<http://www.soe.ucsc.edu/~pang/op.pdf>

2D: Weather forecast

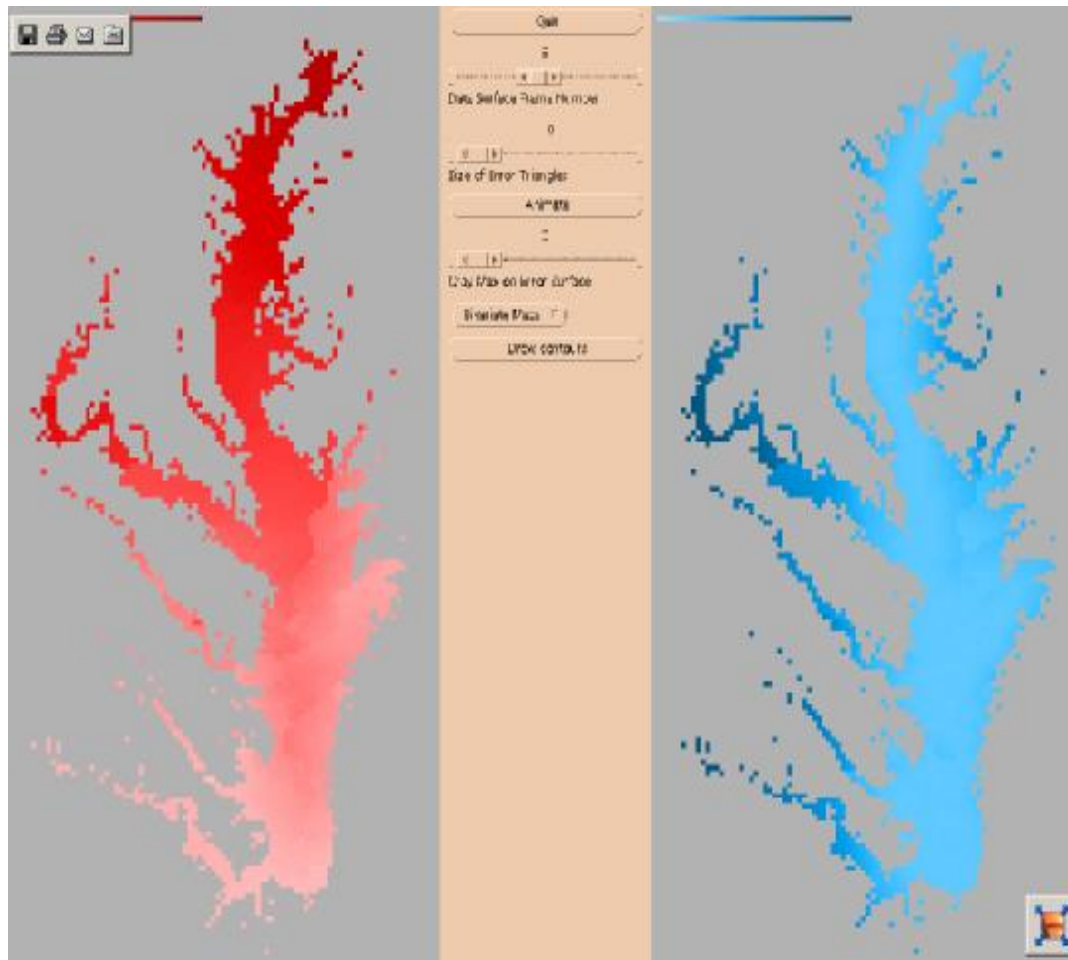


2D: NOAA Storm Prediction Center



<http://www.spc.noaa.gov/products/>

2D: Dual views & grid lines



Dark shows pollution

Dark shows Certainty

(Howard & MacEachren, 1996)

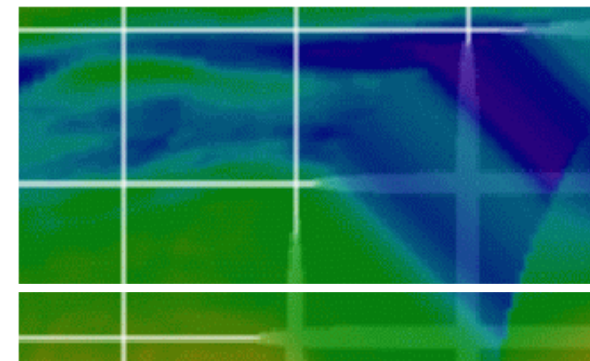


Figure 8: Closeup on the Width variation technique.

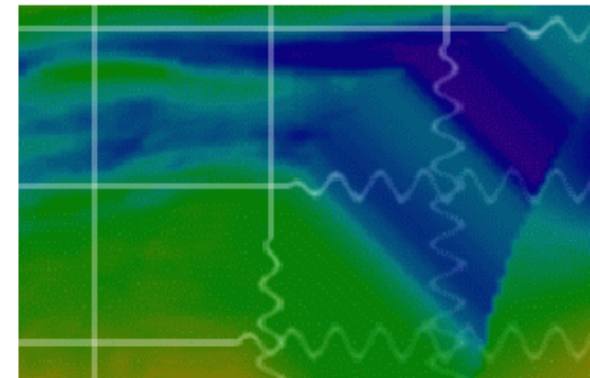
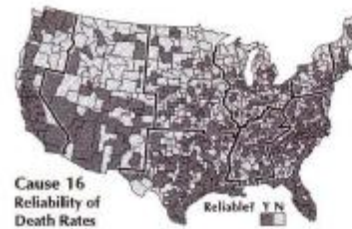
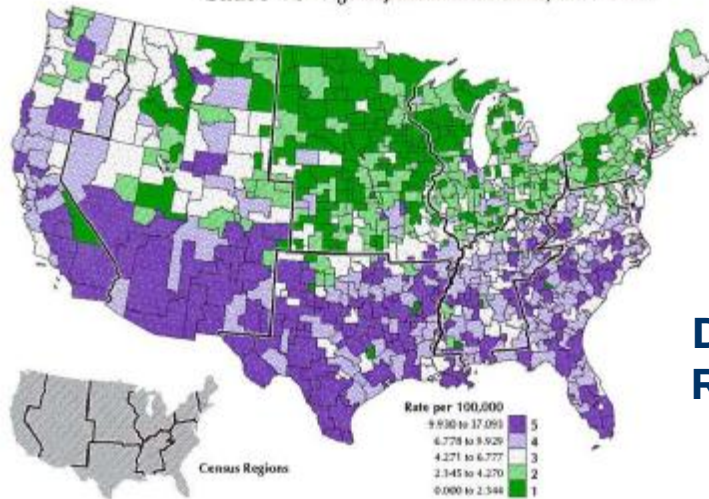


Figure 12: Closeup on the amplitude modulated distortion.

(Cedlink & Rhenigas, 2000)

Cause 16 Age-adjusted Death Rates, 1988–1992



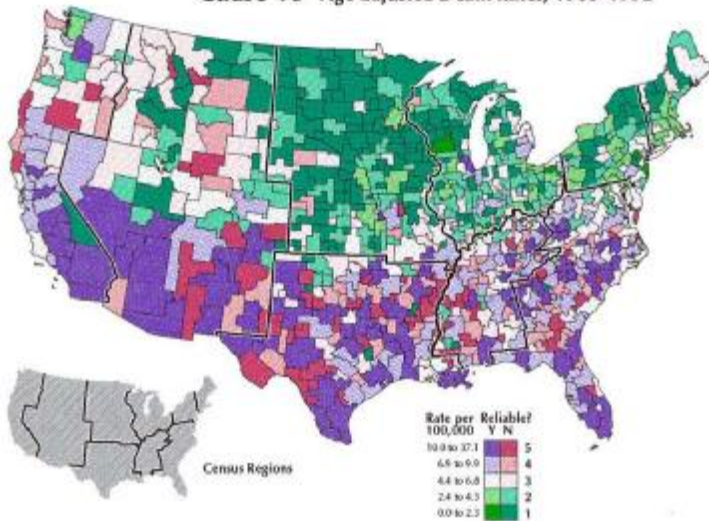
Sample Test Maps:

- cause: 16
- scale: quarter
- color scheme: purple-green
- reliability schemes:
map pairs
color change
texture overlay

Dual maps for Rate and reliability

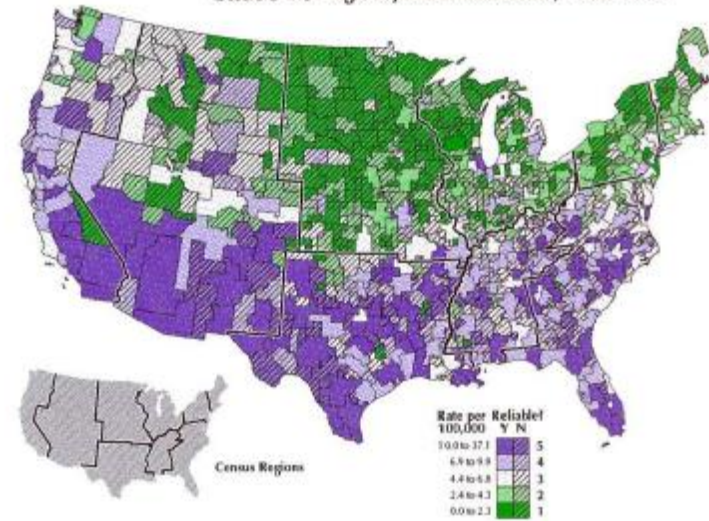
Bivariate color scheme

Cause 16 Age-adjusted Death Rates, 1988–1992



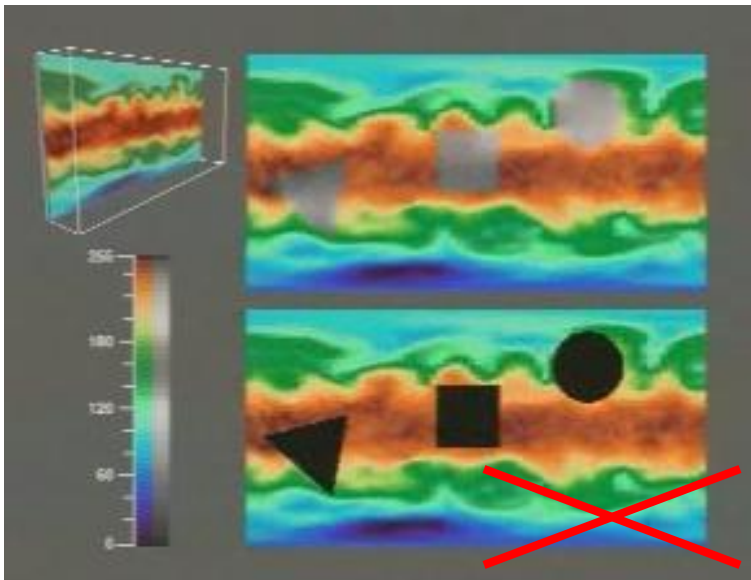
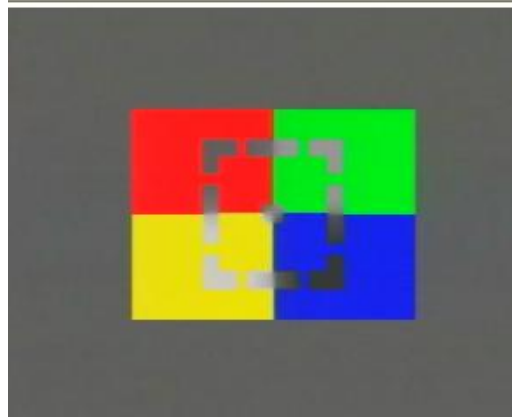
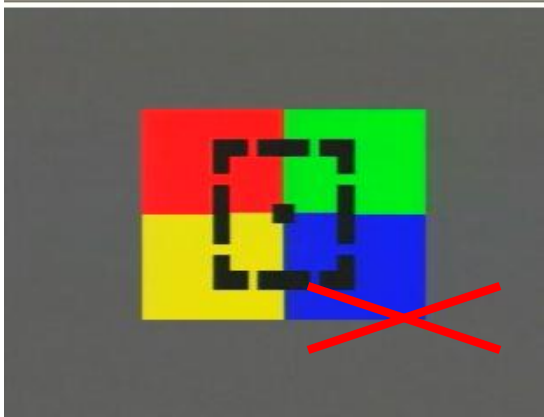
Double hatch shows unreliable

Cause 16 Age-adjusted Death Rates, 1988–1992



(MacEachren et al., 1998)

2D: Gray for missing & interpolation



Gray shows missing & interpolated value,
superior to using black only

Twiddy, R., Cavallo, J., and Shiri, S. 1994.
Restorer: A visualization technique for
handling missing data.
IEEE Visualization 94, 212-216

<http://svs.gsfc.nasa.gov/vis/a000000/a000000/a000010/index.html>

3D: Fuzzy molecular surface: HIV protease

- I Text

- I 1D

- I 2D

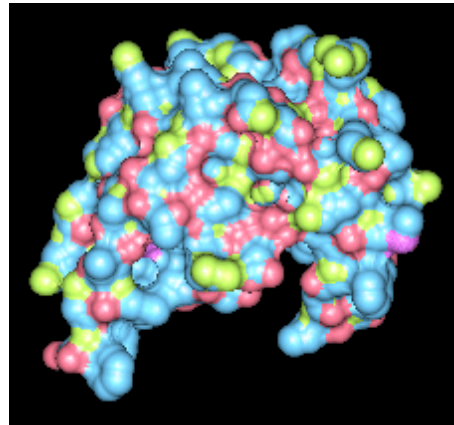
- I 3D

- I Multi-V

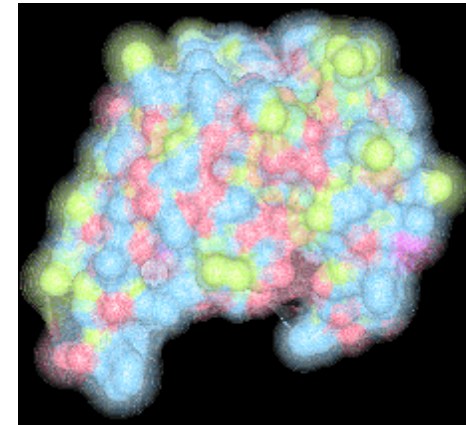
- I Temporal

- I Tree

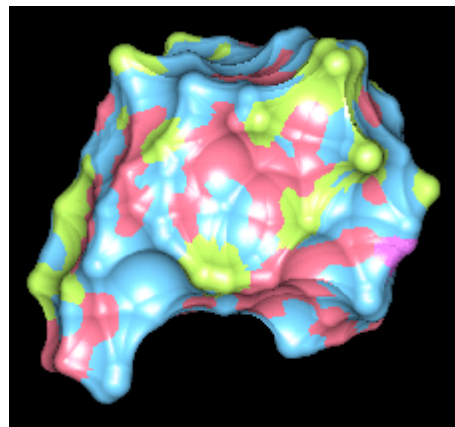
- I Network



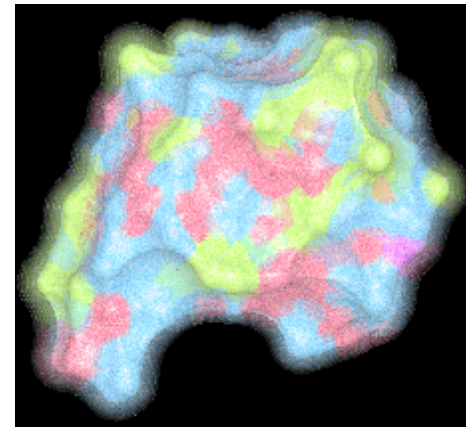
Crisp molecular surface
Probe radius 1.4



Fuzzy molecular surface
Probe radius 1.4



Crisp molecular surface
Probe radius 5.0

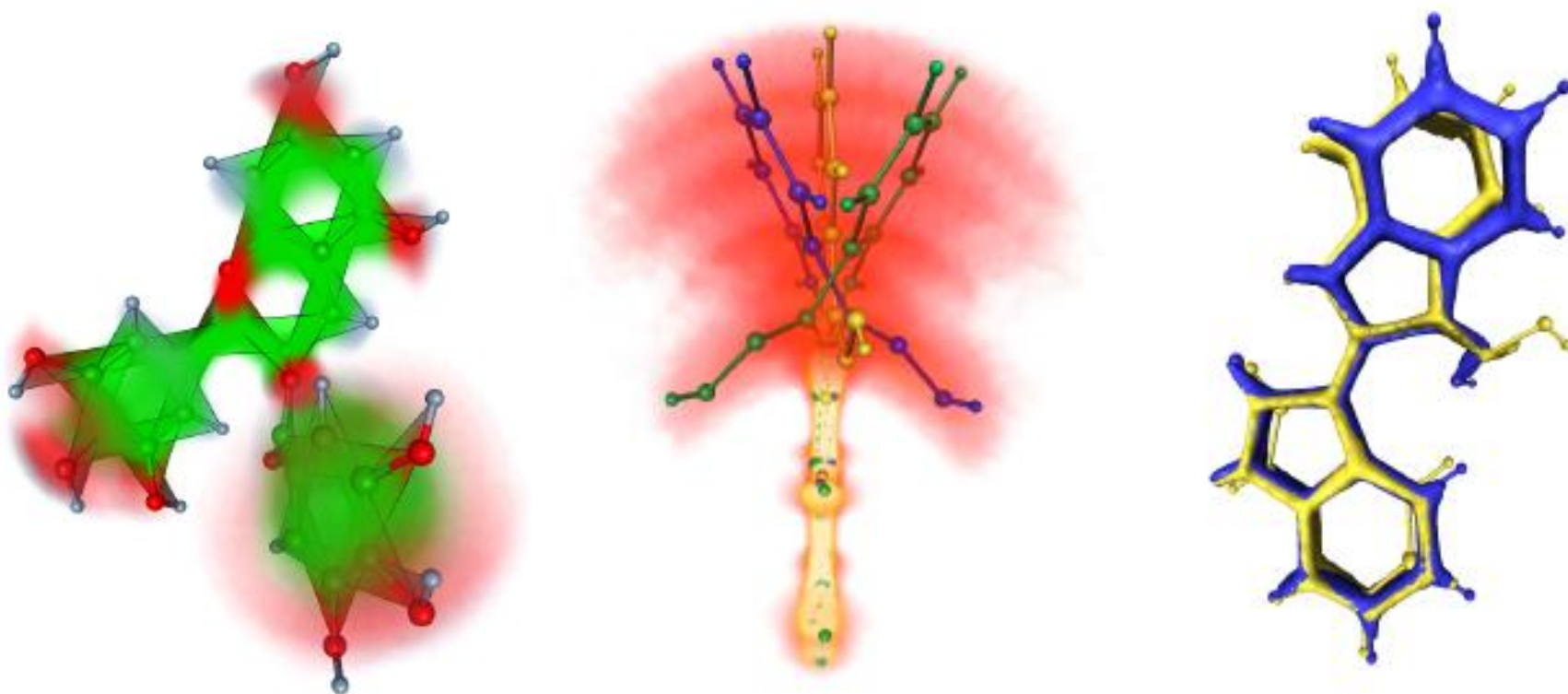


Fuzzy molecular surface
Probe radius 5.0

Lee & Varshney (2002), UM Graphics and Visual Informatics Lab

<http://www.cs.umd.edu/gvil>

3D: Fuzzy molecular densities



3D: Uncertainty 'dust'

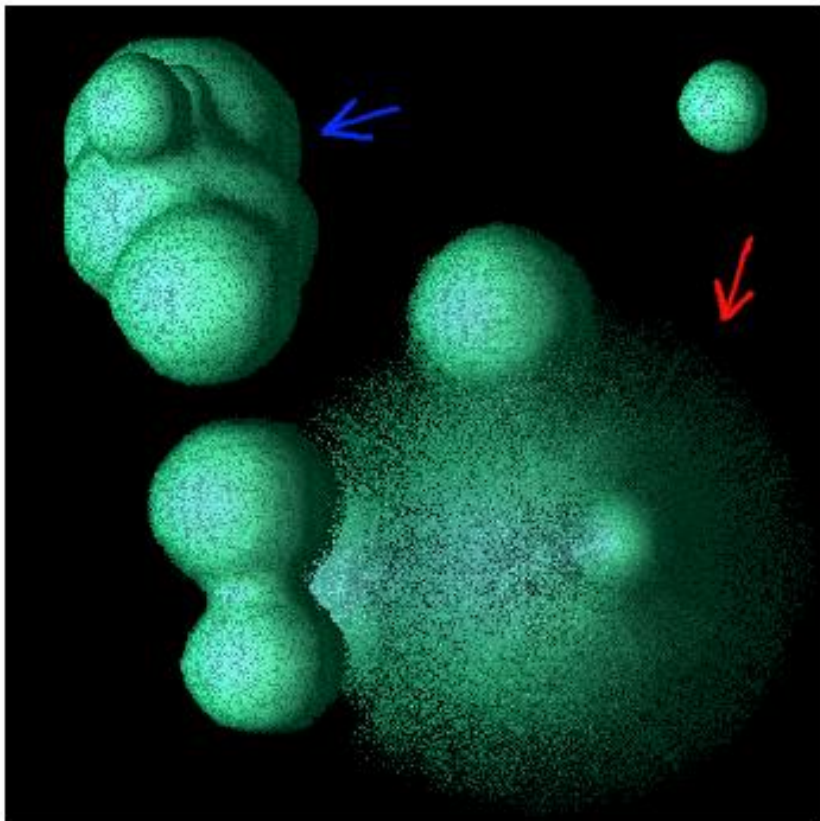


Figure 5: Hybrid of point-based and polygonal models with transparency. Representation of uncertainty is more intuitive since uncertain regions are simply the ones which look uncertain the eye.

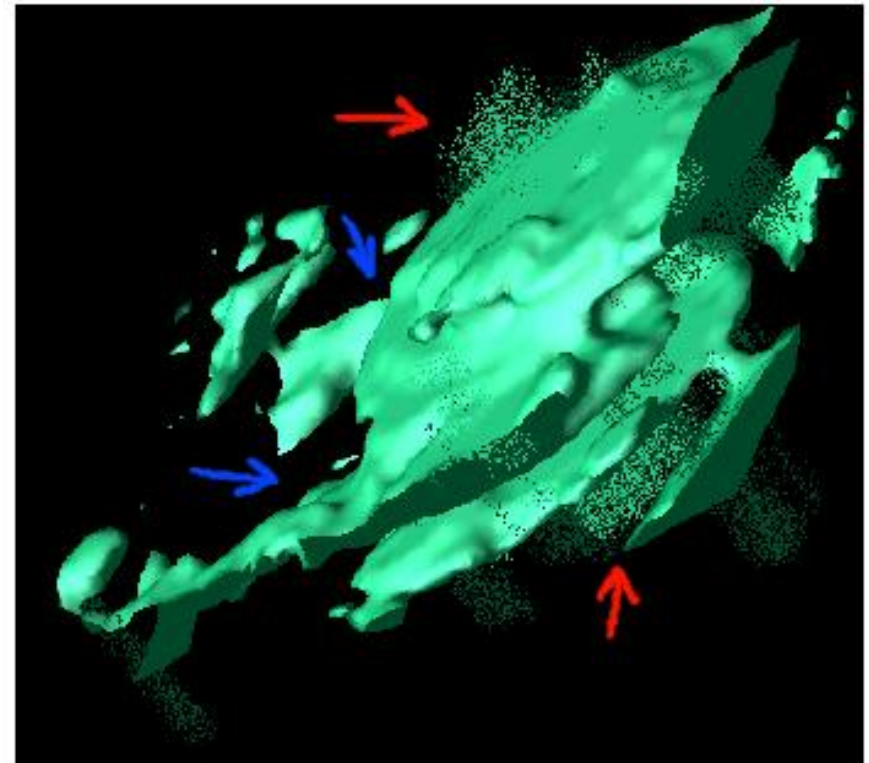
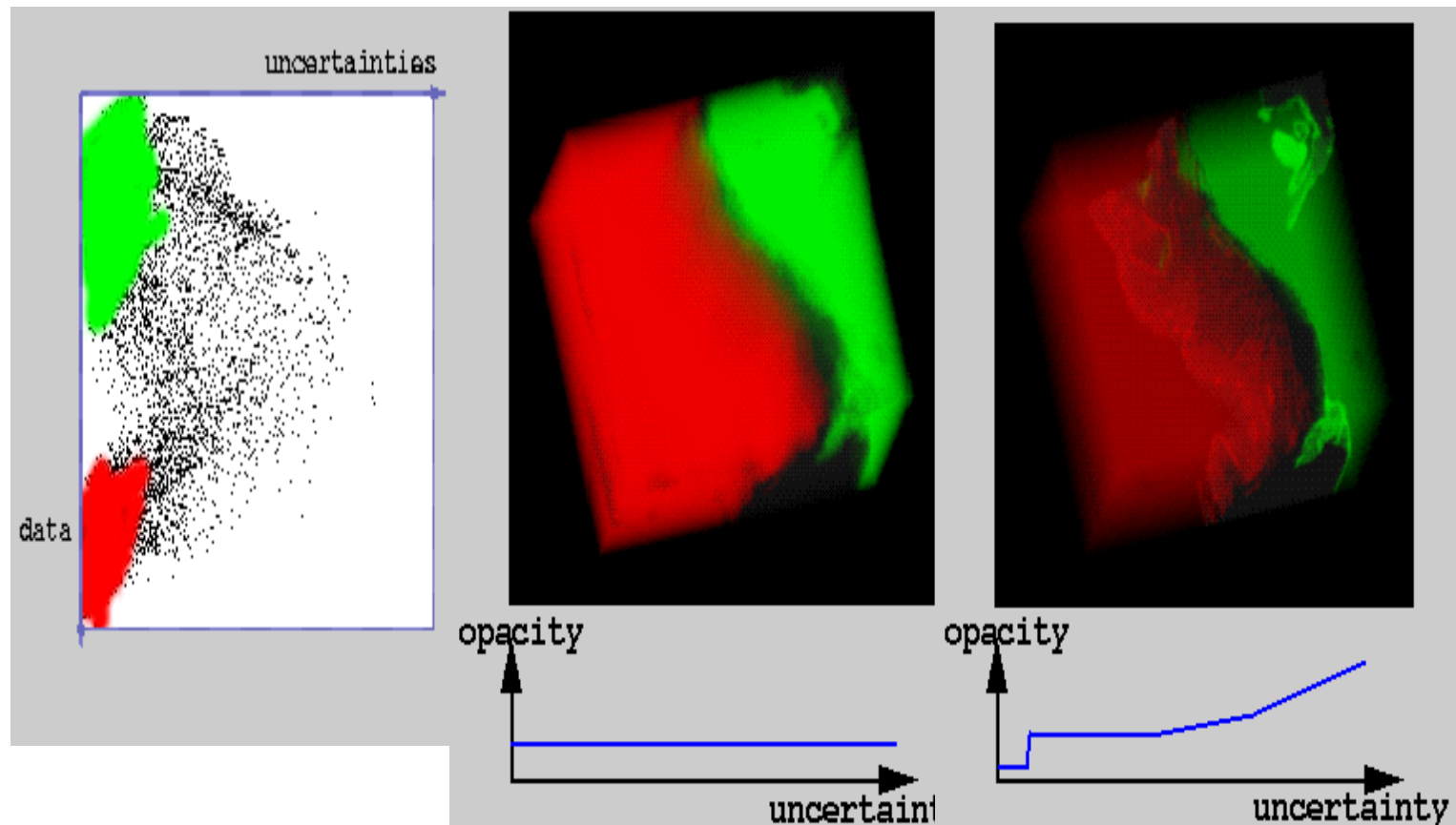


Figure 7: Real tumor data.

clearly see that areas pointed to by red arrows are of particularly high uncertainty while those pointed to by blue arrows are rather certain and strictly shaped. Figure 8 visualizes a larger subvolume of the same data set. Uncertainty distribution is just as intuitive as it is in Figure 3.

3D: Color & opacity



Multi-V: Database/spreadsheet tables

I Text

I 1D

I 2D

I 3D

I **Multi-V**

I Temporal

I Tree

I Network

Guatemala-4 - Spotfire DecisionSite 8.0 - [Table]

v_num	v_age	v_sex	v_ethnicity-Language	Year	Date-Precision	Regime	n_Type	n_Press	n_...
sv0001986		Male		1983	2 07-Schaad	Disappeared		2	
sv0001988	45	Male		1980	1 06-FGarcia	Killed		0	
sv0001989		Male		1991	1 19-Elias	Killed		1	
sv0001990	40	Male	bil	1980	1 06-FGarcia	Killed		0	
sv0047883	90	Male	bil	1980	1 06-FGarcia	Killed		0	
sv0047883	90	Male	bil	1980	1 06-FGarcia	Kidnapped		0	
sv0001991	35	Male	Qeqchi	1970	1 04-Osorio	Killed		0	
sv0001992	23	Male	Kaqchikel	1990	1 09-Arevalo	Killed		0	
sv0001995	20	Male		1990	2 09-Arevalo	Killed		1	
sv0001996		Male		1982	1 07-Schaad	Kidnapped		1	
sv0001997	60	Male	Kiche	1983	2 07-Schaad	Killed		0	
sv0001998		Male		1968	1 03-Montenegro	Killed		1	
sv0001999	19	Female	Espanol	1982	5 07-Schaad	Kidnapped		0	
sv0002000	12	Female	Kiche	1982	5 07-Schaad	Killed		0	
sv0002002		Male		1973	1 04-Osorio	Killed		1	
sv0050071	50	Female	Espanol	1982	1 06-FGarcia	Killed		0	
sv0002004		Male		1982	1 07-Schaad	Kidnapped		1	
sv0002005	23	Male		1980	1 06-FGarcia	Killed		1	
sv0002008	30	Male		1973	1 04-Osorio	Killed		2	
sv0050072	18	Female	Espanol	1982	1 06-FGarcia	Killed		0	
sv0050073	15	Male	Espanol	1982	1 06-FGarcia	Killed		0	
sv0050074	24	Male	Espanol	1982	1 06-FGarcia	Killed		0	
sv0002011		Male		1975	2 05-KGarcia	Killed		1	
sv0002014		Male		1985	1 08-Victores	Killed		0	
sv0002016	37	Male	Kiche	1981	1 06-FGarcia	Disappeared		0	
sv0002017	48	Male	Kiche	1981	1 06-FGarcia	Killed		0	
sv0002018	16	Female	Kiche	1982	5 07-Schaad	Kidnapped		0	
sv0002019	34	Male	Kaqchikel	1985	1 08-Victores	Kidnapped		0	
sv0047919	10	Female		1961	2 01-Fuentes	Disappeared		1	
sv0002020	24	Male		1979	8 06-FGarcia	Killed		1	
sv0002021		Male		1971	1 04-Osorio	Killed		1	
sv0002022	52	Male		1980	1 06-FGarcia	Killed		0	

Ready 17205 out of 17423 records visible (98.75 %), 0 marked

Query Devices

v_num
(ALL)

v_age
1 99

v_sex
☒ Female
☒ Male
☒ Unknown

v_ethnicity-Language
(ALL)

Year
1969 1995

Date-Precision
1 8

Regime
(ALL)

Details on Demand

Column	Value
v_num	sv0005880
v_age	31
v_sex	Female
v_ethnicity-Lon...	
Year	1983
Date-Precision	1
Regime	07-Schaad
n_Type	Kidnapped
n_Press	2
n_Document 49...	0
n_Interviews	0
Total Reports	2

Multi-V: Database/spreadsheet tables

I Text

I 1D

I 2D

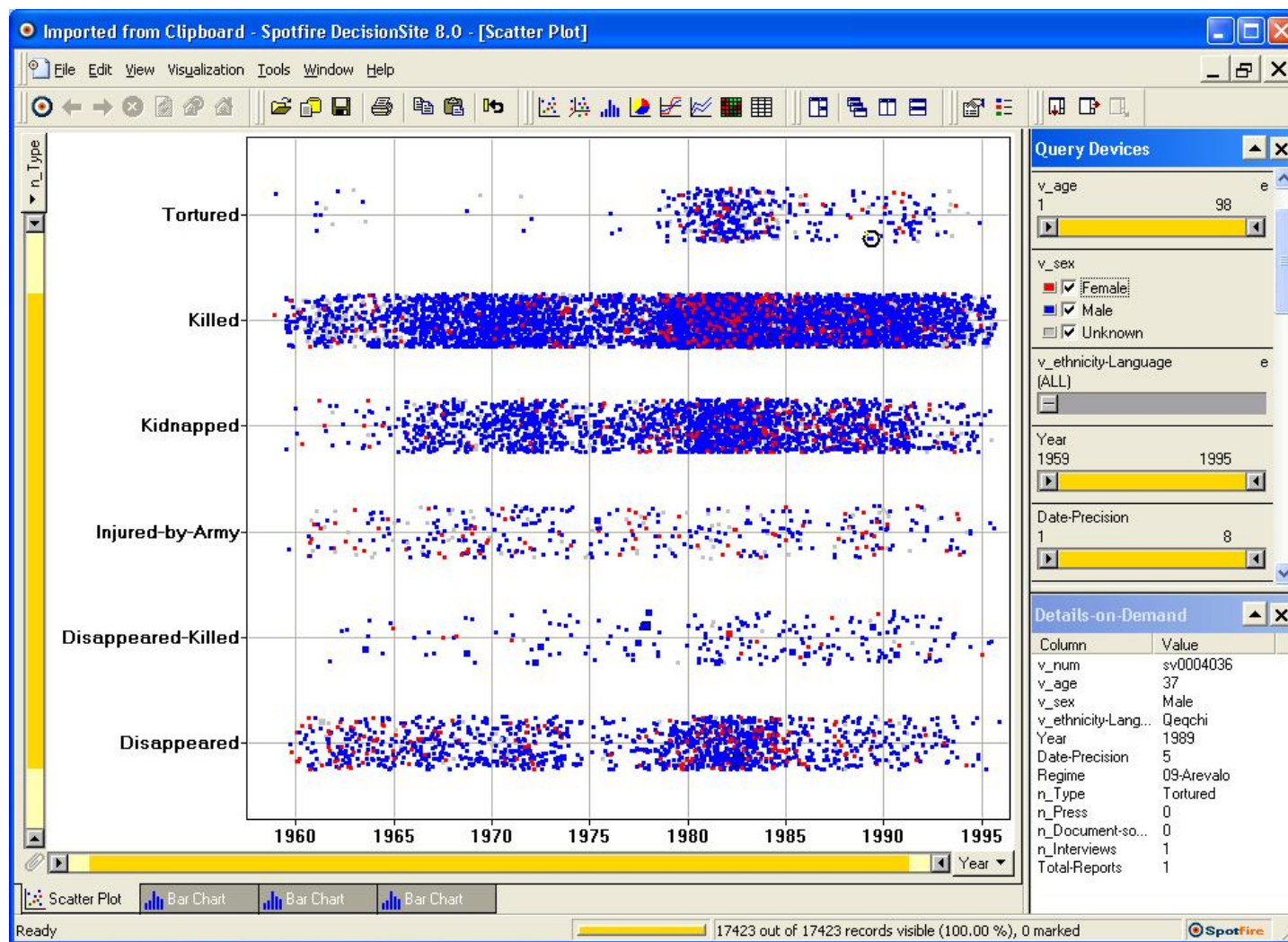
I 3D

I Multi-V

I Temporal

I Tree

I Network



Temporal: Granularity of time

- I Text

- I 1D

- I 2D

- I 3D

- I Multi-V

- I Temporal

- I Tree

- I Network

April 14, 1865 - The Stars and Stripes is ceremoniously raised over Fort Sumter. That night, Lincoln and his wife Mary see the play "Cousin" at Ford's Theater. At 10:13 p.m., during the third act of the play, John Wilkes Booth shoots the president in the head. Doctors in the theater then move him to a house across the street. He never regains consciousness.

April 15, 1865 - President Abraham Lincoln dies at 7:22 in the morning. Vice President [Andrew Johnson](#) assumes the presidency.

April 18, 1865 - Confederate Gen. Joseph E. Johnston surrenders to Sherman near Durham in North Carolina.



Funeral Procession on Pennsylvania Ave. - April 19, 1865

April 26, 1865 - John Wilkes Booth is shot and killed in a tobacco barn in Virginia.

May 4, 1865 - Abraham Lincoln is laid to rest in Oak Ridge Cemetery, outside Springfield, Illinois.

In May - Remaining Confederate forces surrender. The Nation is reunited as the Civil War ends. Over 620,000 Americans died in disease killing twice as many as those lost in battle. 50,000 survivors return home as amputees.



Temporal: Granularity of time

I Text

I 1D

I 2D

I 3D

I Multi-V

I Temporal

I Tree

I Network

- [THE ROMAN CONQUEST](#)
- (43AD - 303AD)
- [THE ANGLIAN INVASIONS](#)
- (306AD - 593AD)
- [AETHELFRITH AND EDWIN](#)
- (598AD - 633AD)
- [OSWALD AND AIDAN](#)
- (633AD - 655AD)
- [WILFRID AND CUTHBERT](#)
- (657AD - 688AD)
- [THE AGE OF BEDE](#)
- (690AD - 735AD)
- [KINGDOM AT WAR](#)
- (736AD - 854AD)
- [JORVIK](#)
- (866AD - 900AD)
- [THE IRISH NORWEGIANS](#)
- (900AD - 945AD)
- [ERIC BLOODAXE](#)
- (946AD - 989AD)
- [THE BIRTH OF DURHAM](#)
- (990AD - 1031AD)
- [THE NORMAN CONQUEST](#)
- (1031AD - 1066AD)
- [CONQUEST OF THE NORTH](#)
- (1067AD - 1080AD)
- [THE PRINCE BISHOPS](#)
- (1081AD - 1135AD)

USING THE TIMELINE

You can use the timeline in one of the three following ways

- Choose a subject from the column on the left
- Choose a century from the column on the right
- Choose an era from below

[Roman period](#)

[Anglo-Saxon period](#)

[Viking Period](#)

[Norman period](#)

[Medieval period](#)

[Tudor and Stuart period](#)

[Georgian period](#)

[Victorian period](#)

CHOOSE A CENTURY

- [1st century](#)
- 1-100 AD
- [2nd century](#)
- 100-200 AD
- [3rd century](#)
- 200-300 AD
- [4th century](#)
- 300-400 AD
- [5th century](#)
- 400-500 AD
- [6th century](#)
- 500-600 AD
- [7th century](#)
- 600-700 AD
- [8th century](#)
- 700-800 AD
- [9th century](#)
- 800-900 AD
- [10th century](#)
- 900-1000 AD
- [11th century](#)
- 1000-1100 AD
- [12th century](#)
- 1100-1200 AD
- [13th century](#)
- 1200-1300 AD
- [14th century](#)
- 1300-1400 AD
- [15th century](#)
- 1400-1500 AD

Temporal: Granularity of time

I Text

I 1D

I 2D

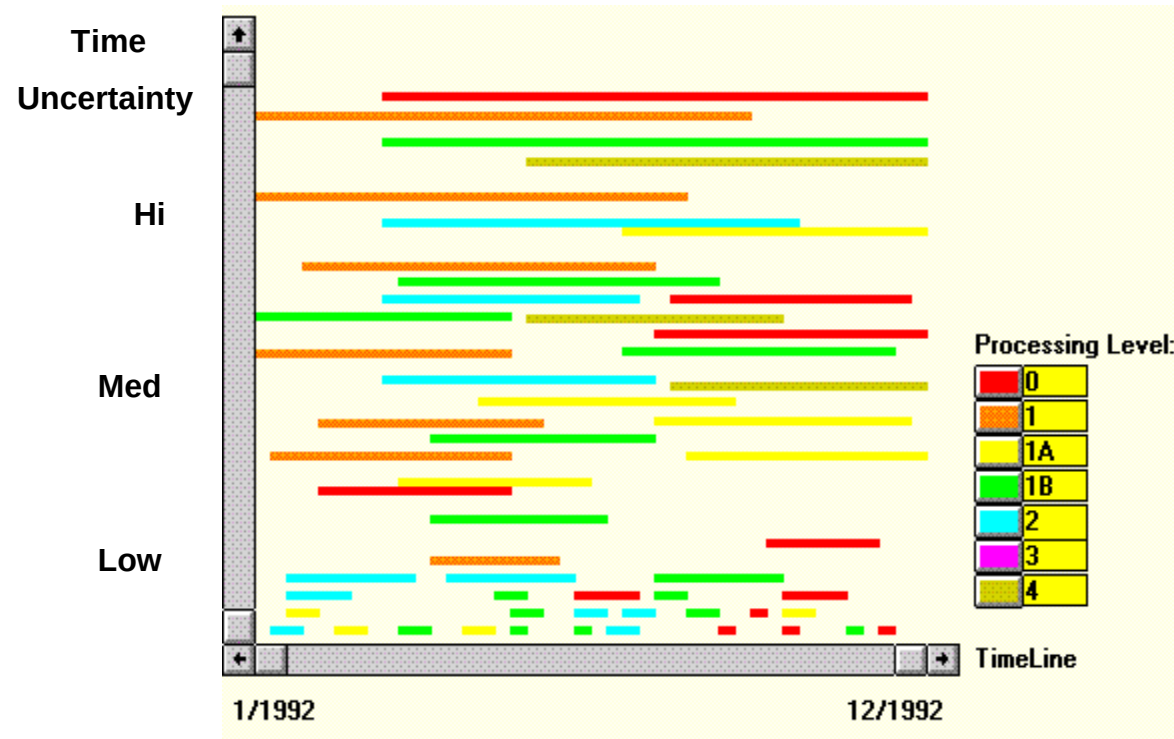
I 3D

I Multi-V

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Temporal: Granularity of time

- I Text

- I 1D

- I 2D

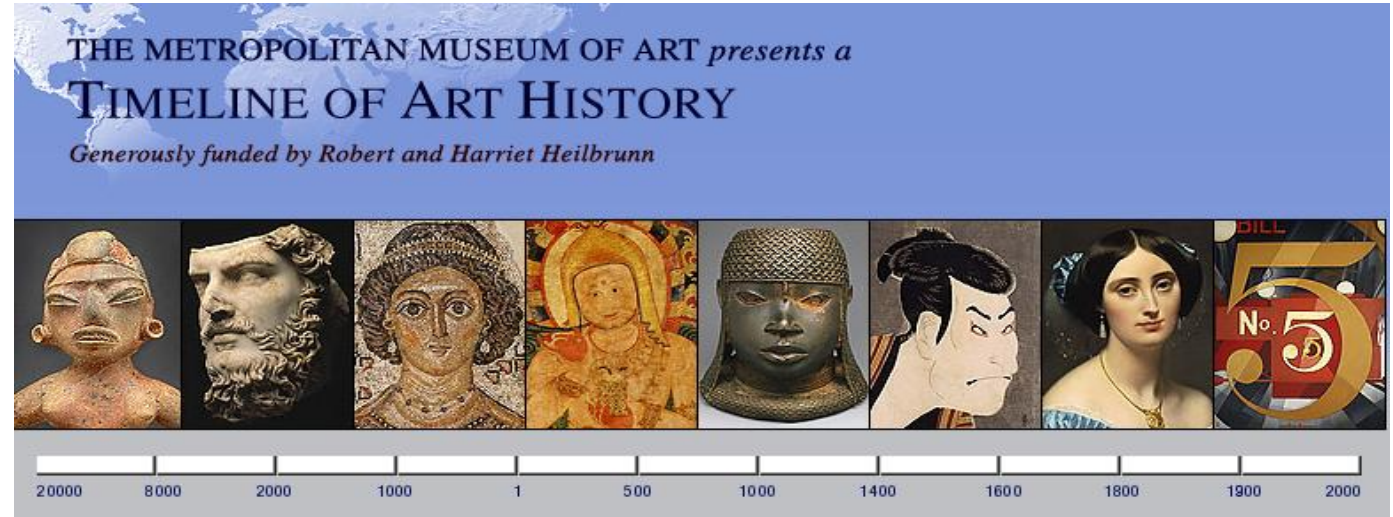
- I 3D

- I Multi-V

- I Temporal

- I Tree

- I Network



Tree: **Topology**, values & names

| Text

| 1D

| 2D

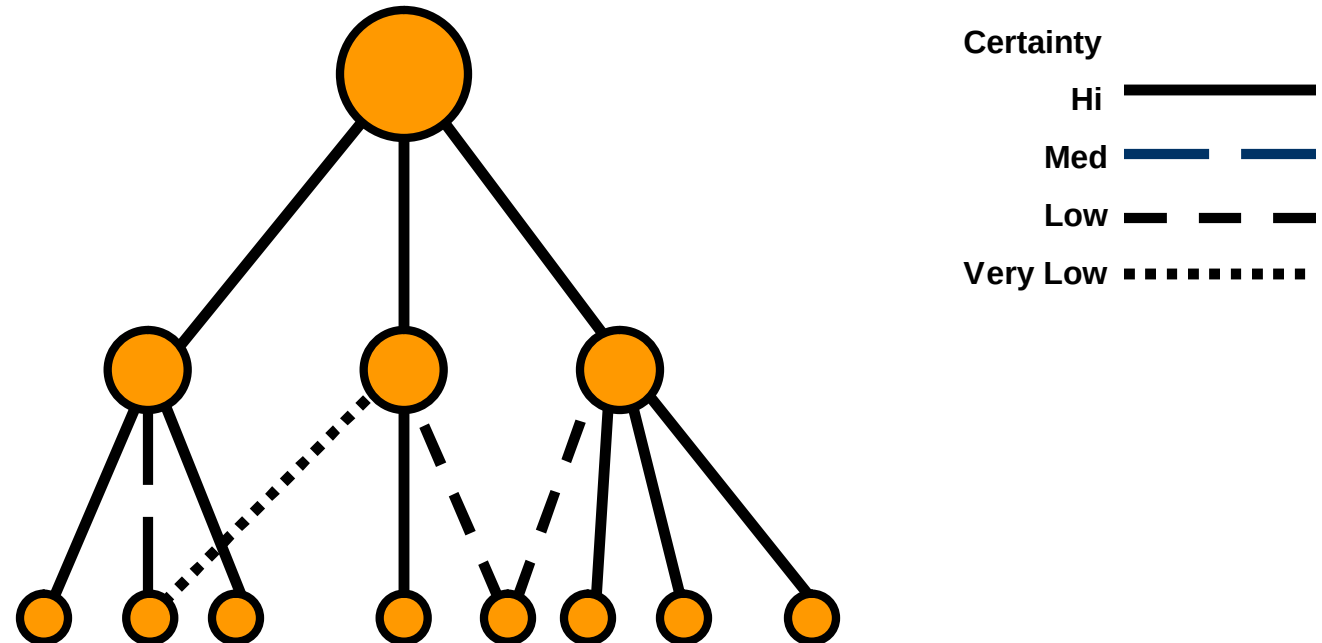
| 3D

| Multi-V

| Temporal

| **Tree**

| Network



- Gene Ontology
- Tree of Life
- Medical Subject Heading (MeSH)
- Chain of command/Org chart

Tree: Topology, values & names

I Text

I 1D

I 2D

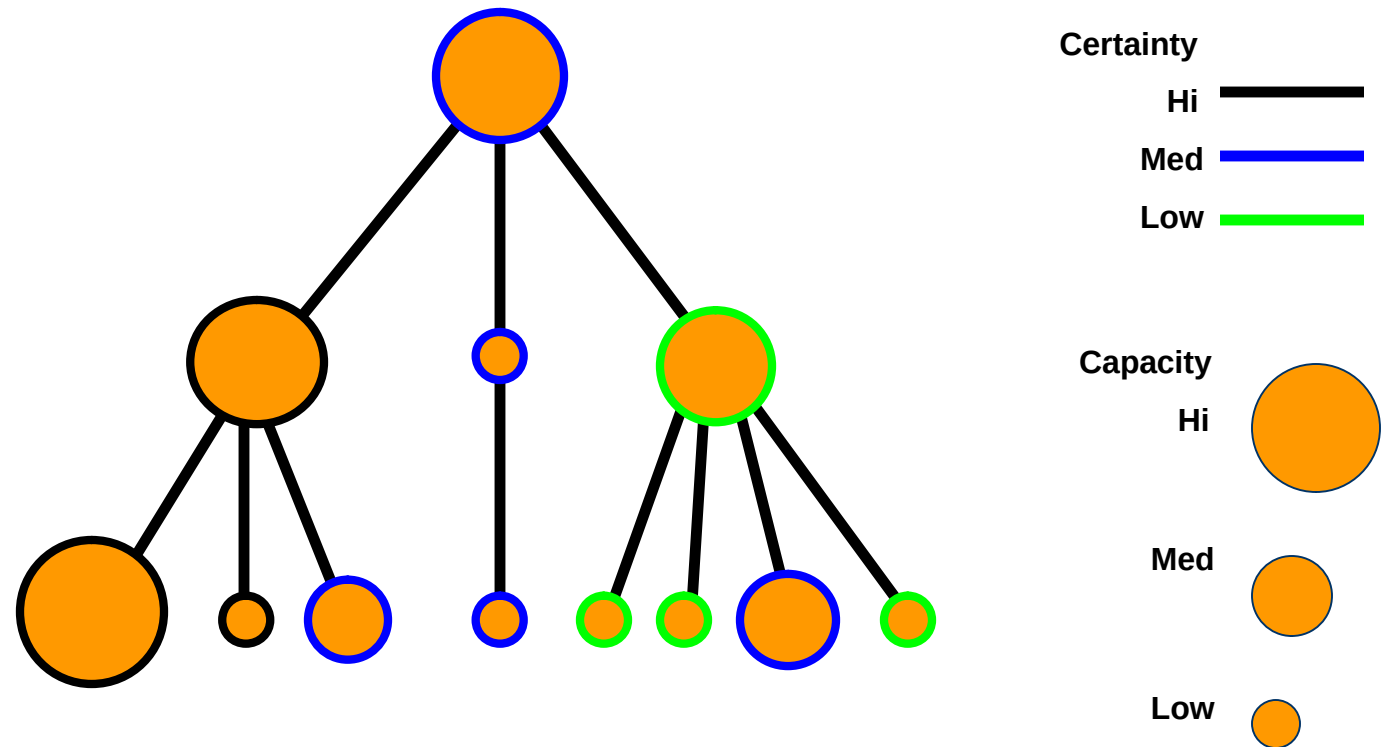
I 3D

I Multi-V

I Temporal

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Tree: Topology, values & names

I Text

I 1D

I 2D

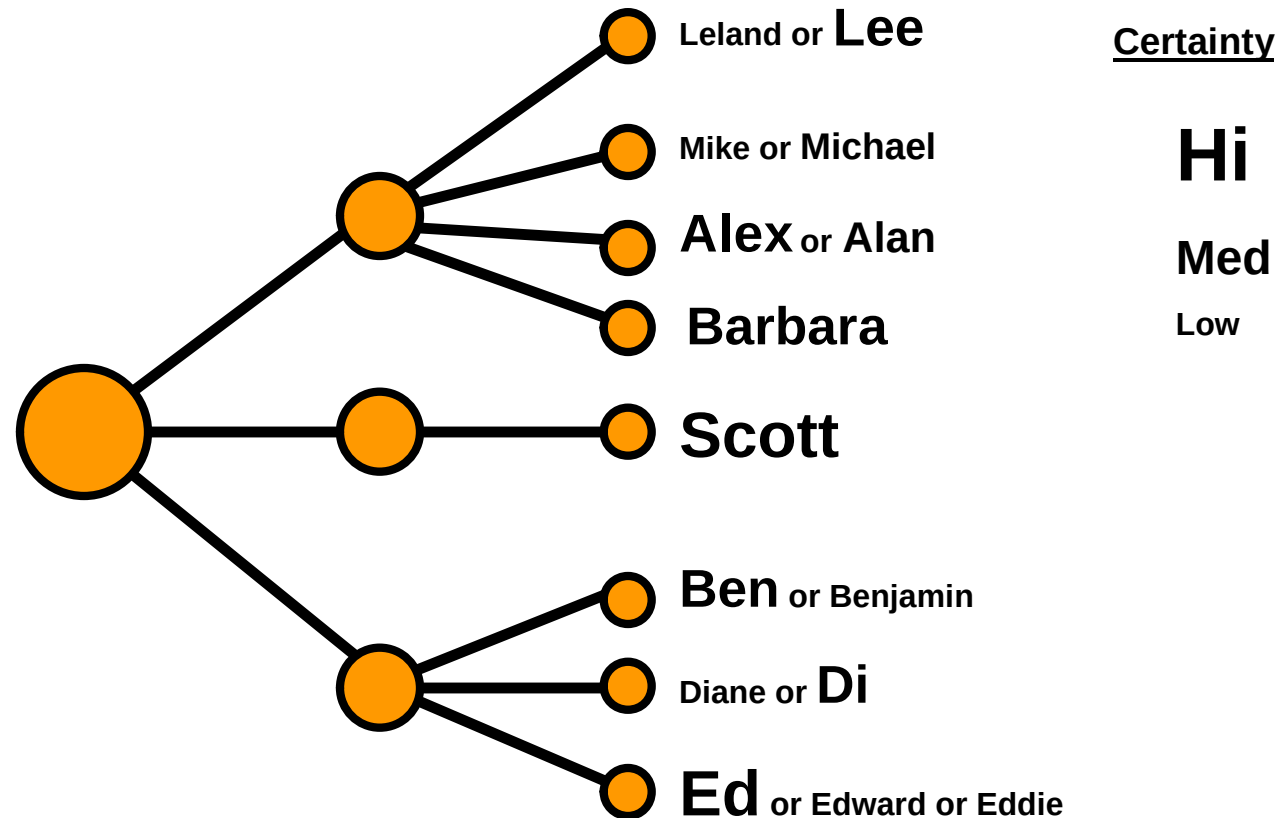
I 3D

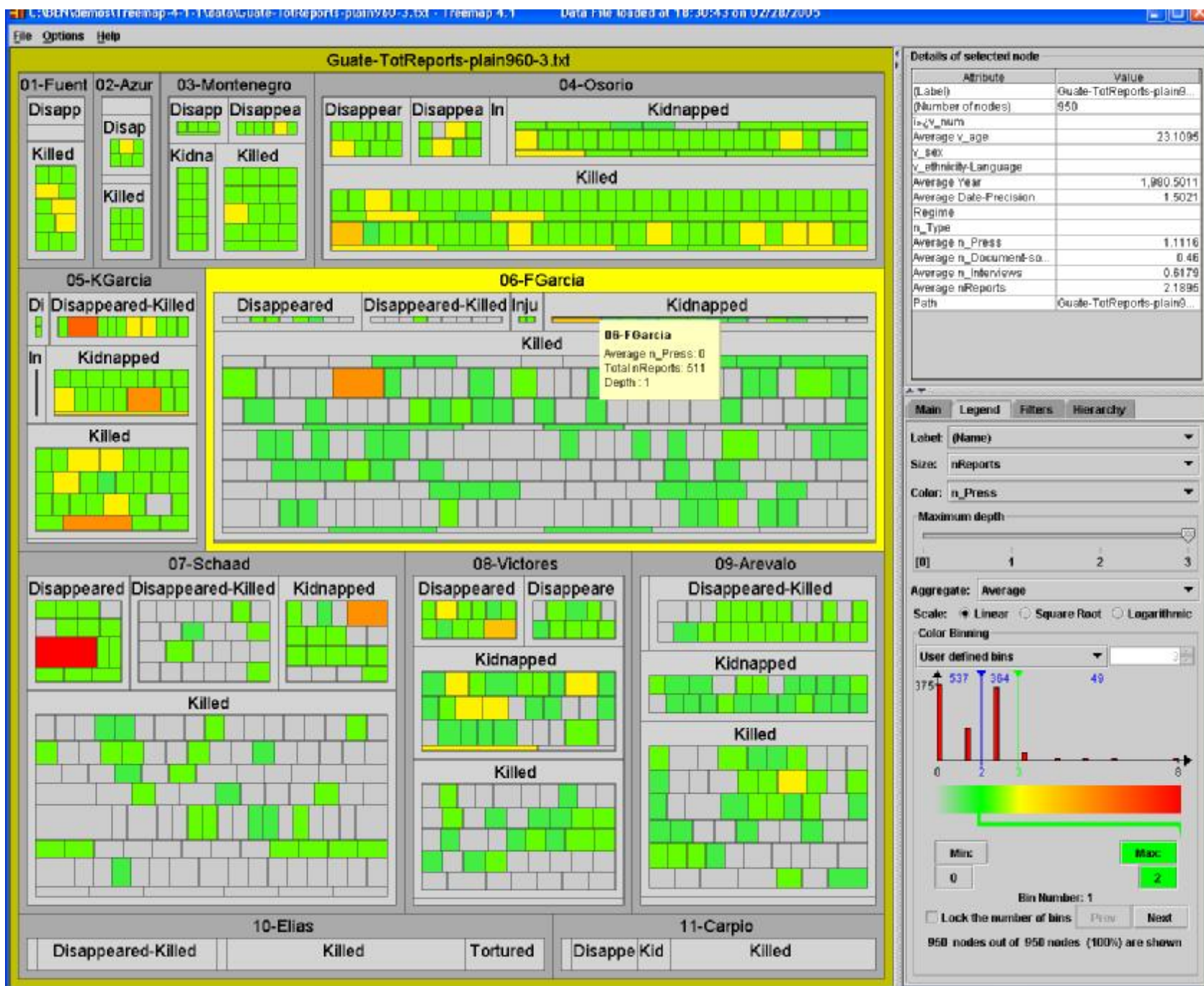
I Multi-V

I Temporal

I **Tree**

I Network





Network: Social relationship

I Text

I 1D

I 2D

I 3D

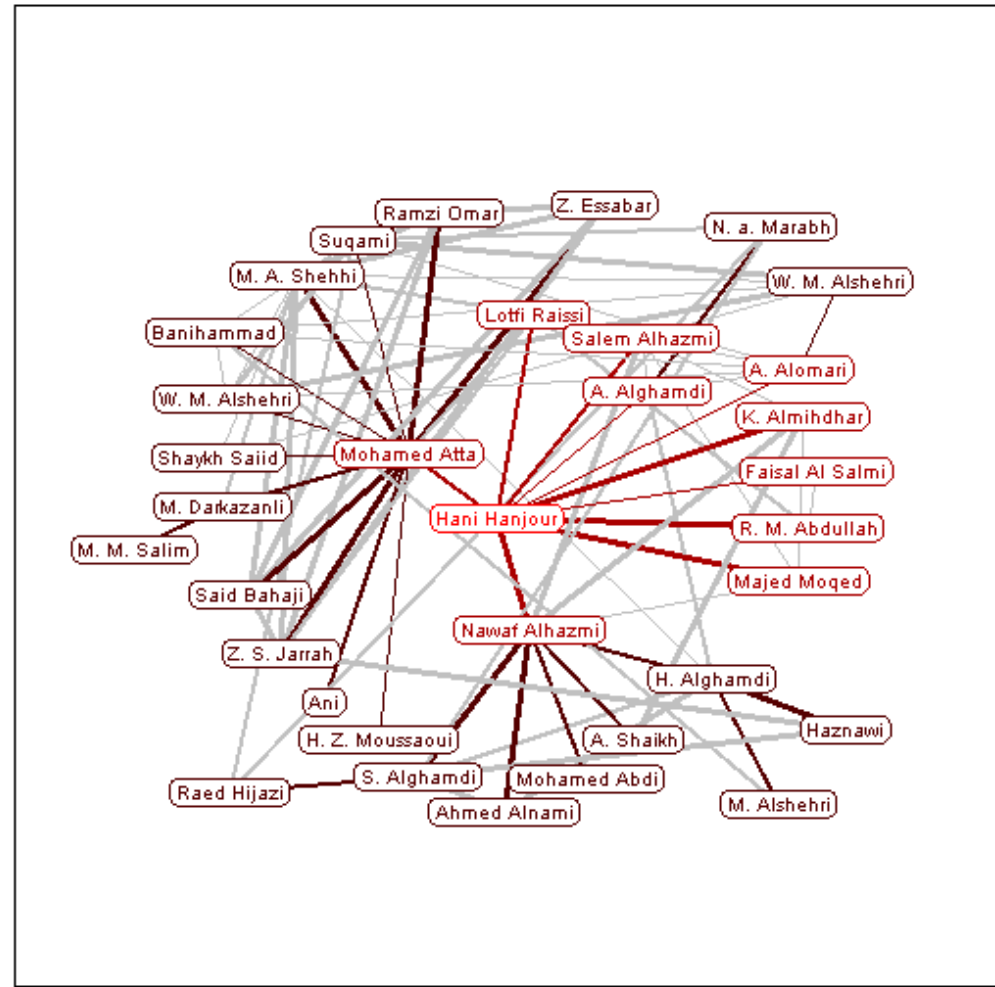
I Multi-V

I Temporal

I Tree

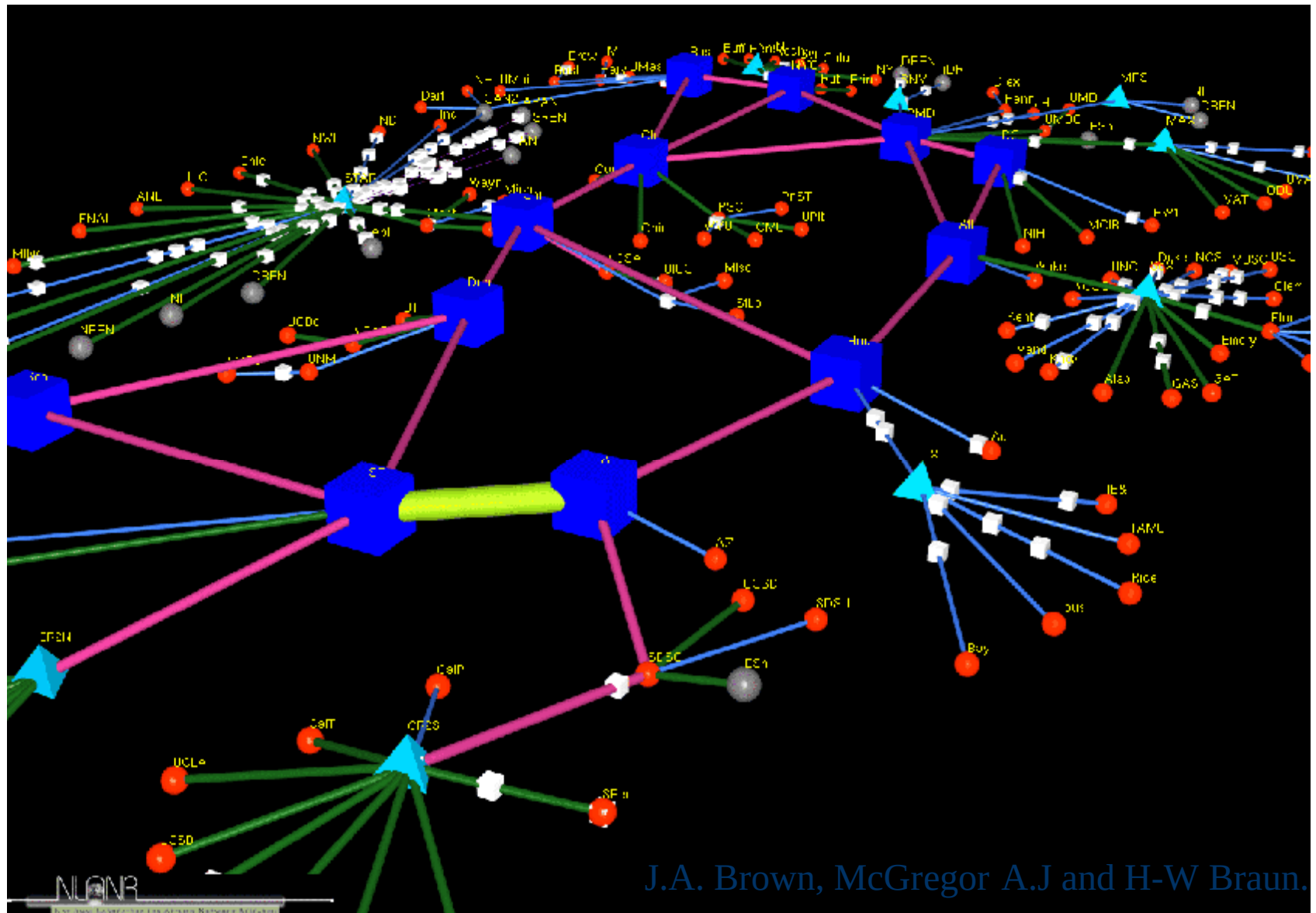
I **Network**

prefuse demos: radial layout



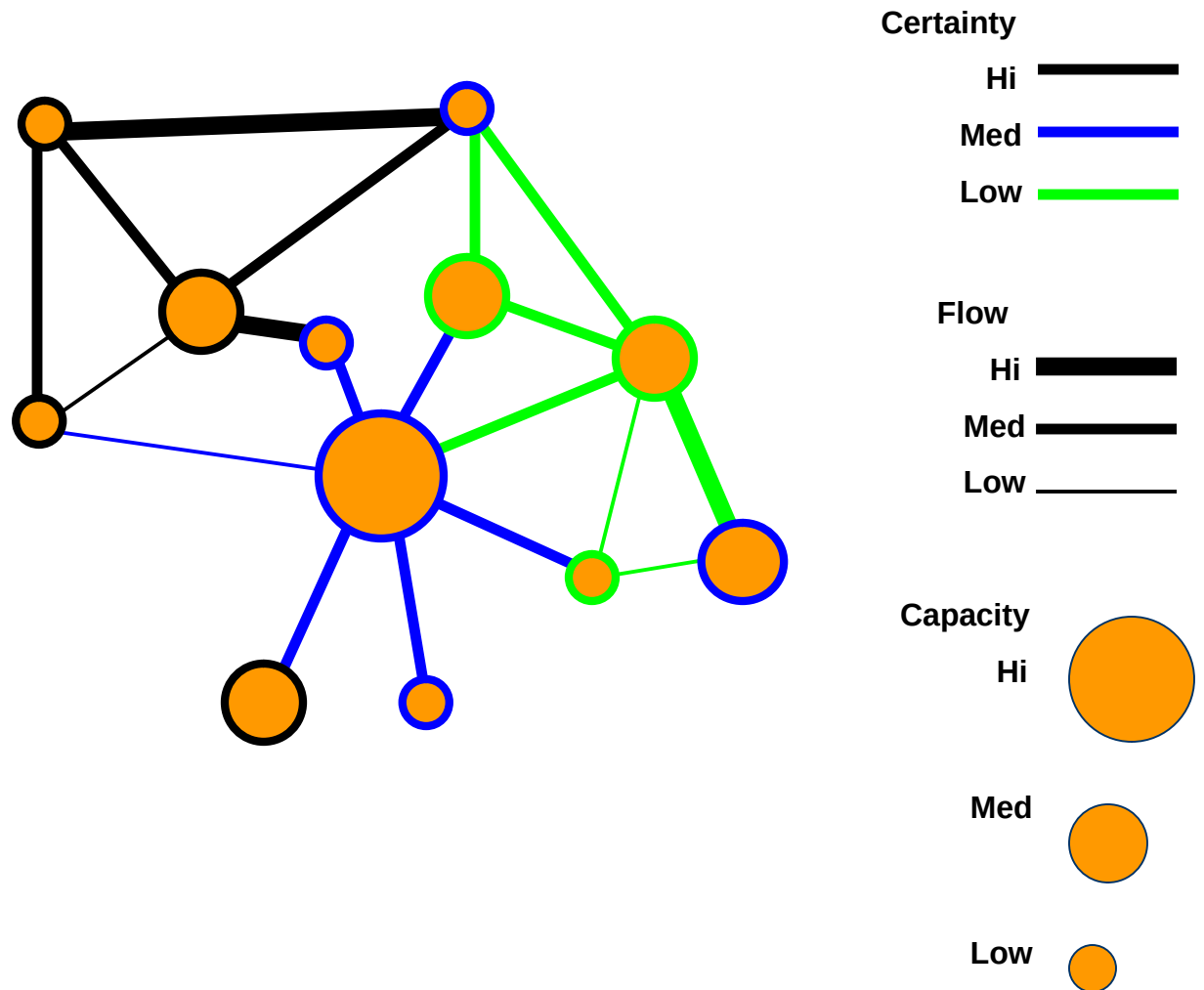
<http://prefuse.sourceforge.net/demos-radial.html>

Network: Communication capacity



Network: Node & edge uncertainty

- I Text
- I 1D
- I 2D
- I 3D
- I Multi-V
- I Temporal
- I Tree
- I **Network**



Next steps

Explore novel approaches to:

- | Text: standard terms, percent, probabilities
- | Box plots, whiskers, ranges
- | Uncertainty glyphs, isoclines,...
- | Contours, surfaces, volume rendering
- | Hue, saturation, value, focus, haze, dust,...
- | Dual views, probes
- | Animation, blinking, shaking, flipping,...
- | Sound, haptics,...

Next steps

- | Heighten awareness of the problem among public, professionals, researchers & developers
- | Support multi-valued data representation standards
- | Explore techniques for each data type
- | Develop guidelines for implementers:
 - Data formats
 - Interactive interfaces
 - Visual presentations
- | Develop human performance evaluation methods
- | Publish benchmark datasets & evaluation metrics
- | Form guidelines for how to propagate/integrate uncertainty markers