

# WFIRST/AFTA NAS Dark Energy Presentation

David Spergel

# Instrument Comparisons

Feature	JDEM/Omega	IDRM	WFIRST DRM1	WFIRST 2.4
Mirror Diameter	1.5 m	1.3 m (unobs.)	1.3 m (unobs.)	2.4 m
Imager				
Detectors	24 H2RG	28 H2RG	36 H2RG	18 H4RG
Total Pixels	96 Mpix	112 Mpix	144 Mpix	288 Mpix
Area on Sky	0.25 sq deg	0.29 sq deg	0.36 sq deg	0.28 sq deg
Plate Scale	0.18"/pix	0.18"/pix	0.18"/pix	0.11"/pix
Wavelength	0.4 – 2.0 $\mu$	0.6 – 2.0 $\mu$	0.6 – 2.4 $\mu$	0.6 – 2.0 (2.4) $\mu$
Spectrometer	Slitless Prism (2x6 H2RG 0.37"/pix)	Slitless Prism (2x4 H2RG 0.45 "/pix)	Slitless Prism	GRISM + IFU
Coronagraph	No	No	No	Yes

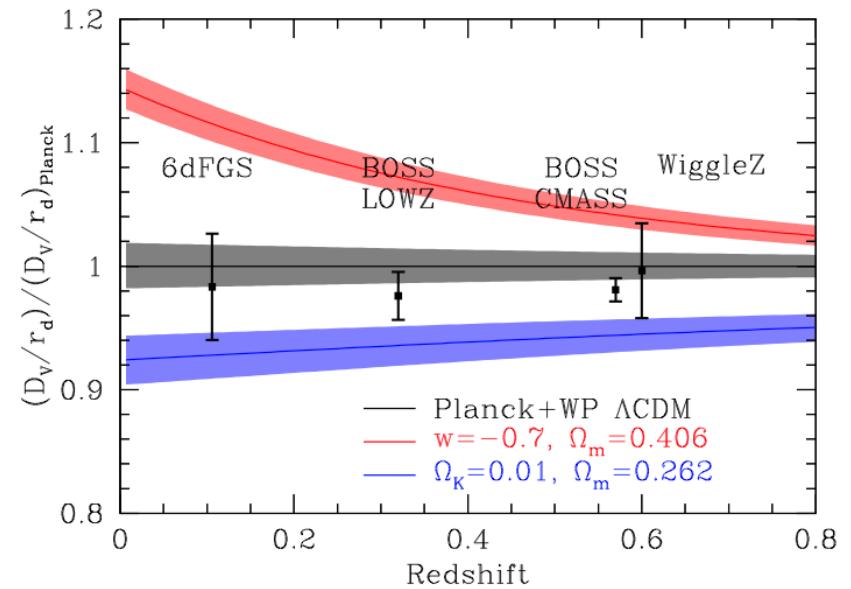
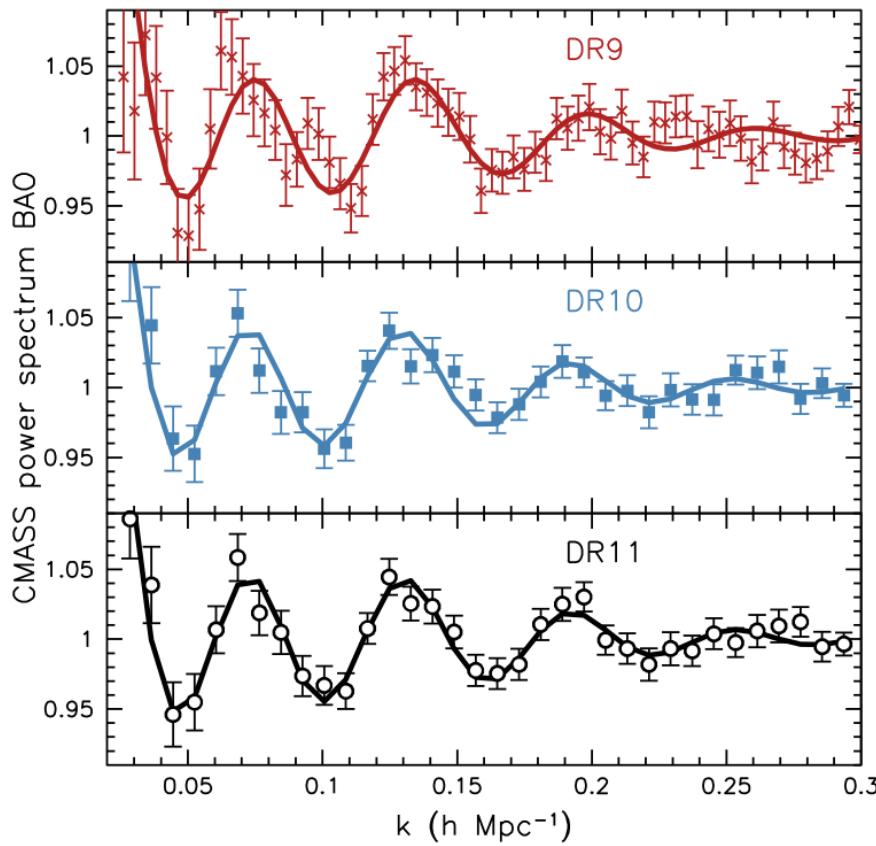
WFIRST/AFTA has 2.9x larger etendue than JDEM/Omega, the version of WFIRST proposed to the decadal survey

# What is new with dark energy?

- Beyond FOM
  - Deviations from GR
  - Desire to measure growth rate and distance as a function of redshift using many techniques
- Experimental improvements
  - Planck, BOSS results
  - Intriguing tensions in Planck
  - Euclid selected, defined
  - LSST moving forward with NSF+DOE support
  - DESI likely with NSF/DOE support
- By 2023, precision measurements at lower redshifts are likely well underway

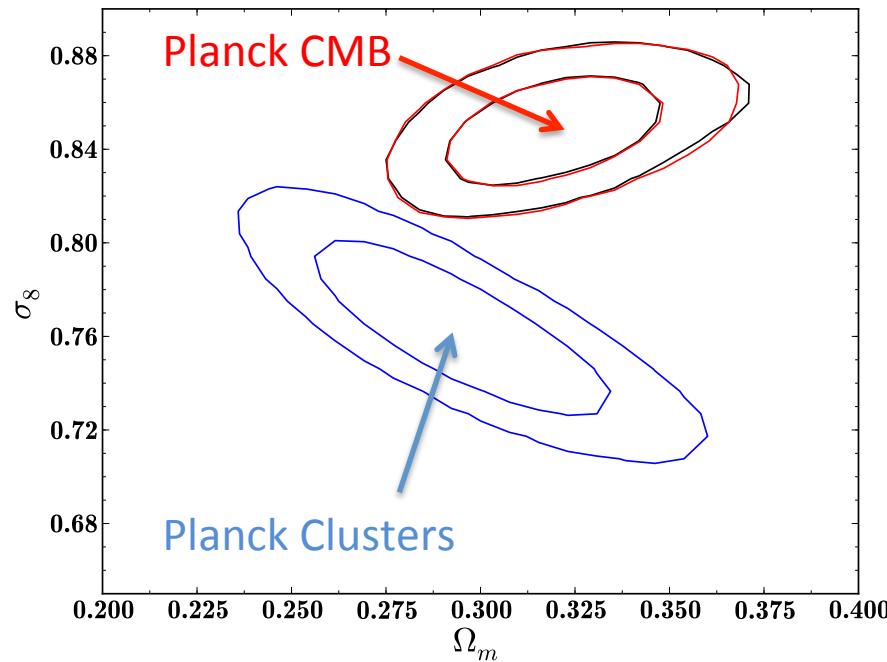
**IMPORTANCE OF MULTIPLE TECHNIQUES AND CONTROL OF SYSTEMATICS!**

# Success of $z < 1$ Ground-Based BAO



Anderson et al. 1312.4877 (SDSS III)

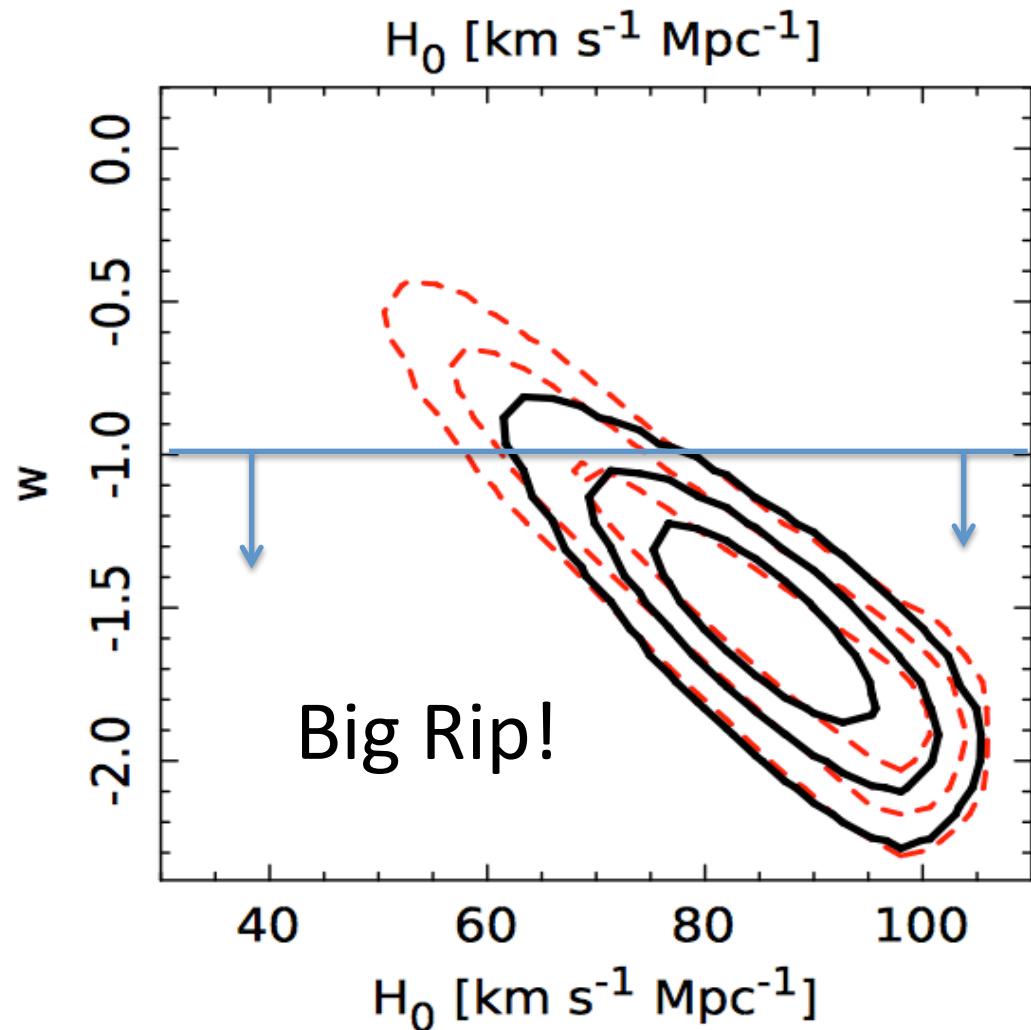
# Has Planck Ruled Out $\Lambda$ CDM?



Planck Paper XX

- Either new physics or a reminder of the importance of control of systematics
  - Need to use only cross-correlations in Planck maps [dangers of auto-correlations in single channel!]
  - Need to better calibrate cluster masses

# Is the Big Rip Coming?



Suyu et al. 1306.4732

$H_0$  tension between Planck ,  
Cepheid and time-delay  
measurements

Systematics or New Physics?

# The WFIRST-2.4 Dark Energy Roadmap

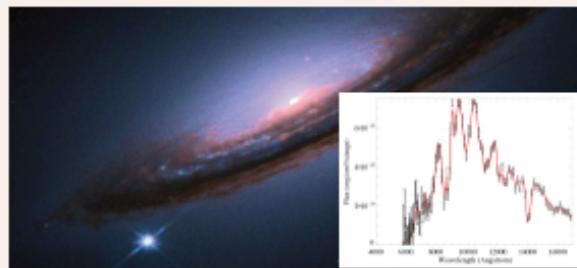
## Supernova Survey

wide, medium, & deep imaging  
+  
IFU spectroscopy

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2700 type Ia supernovae  
 $z = 0.1\text{--}1.7$

standard candle distances  
 $z < 1$  to 0.20% and  $z > 1$  to 0.34%



## High Latitude Survey

spectroscopic: galaxy redshifts

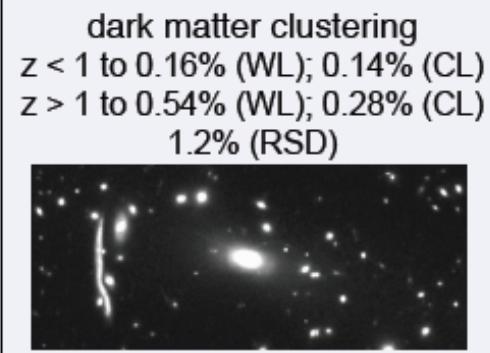
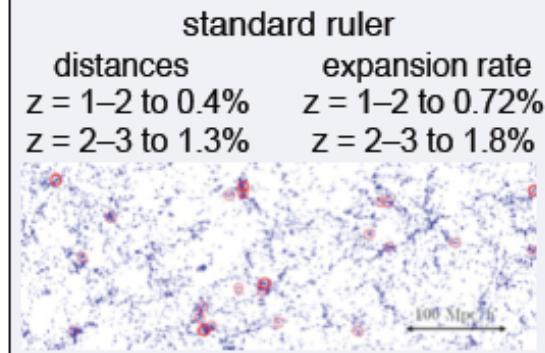
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20 million H $\alpha$  galaxies,  $z = 1\text{--}2$   
2 million [OIII] galaxies,  $z = 2\text{--}3$

imaging: weak lensing shapes

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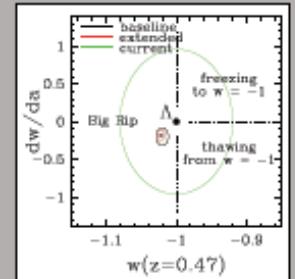
500 million lensed galaxies  
40,000 massive clusters



history of dark energy  
+  
deviations from GR

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$w(z)$ ,  $\Delta G(z)$ ,  $\Phi_{\text{REL}}/\Phi_{\text{NREL}}$



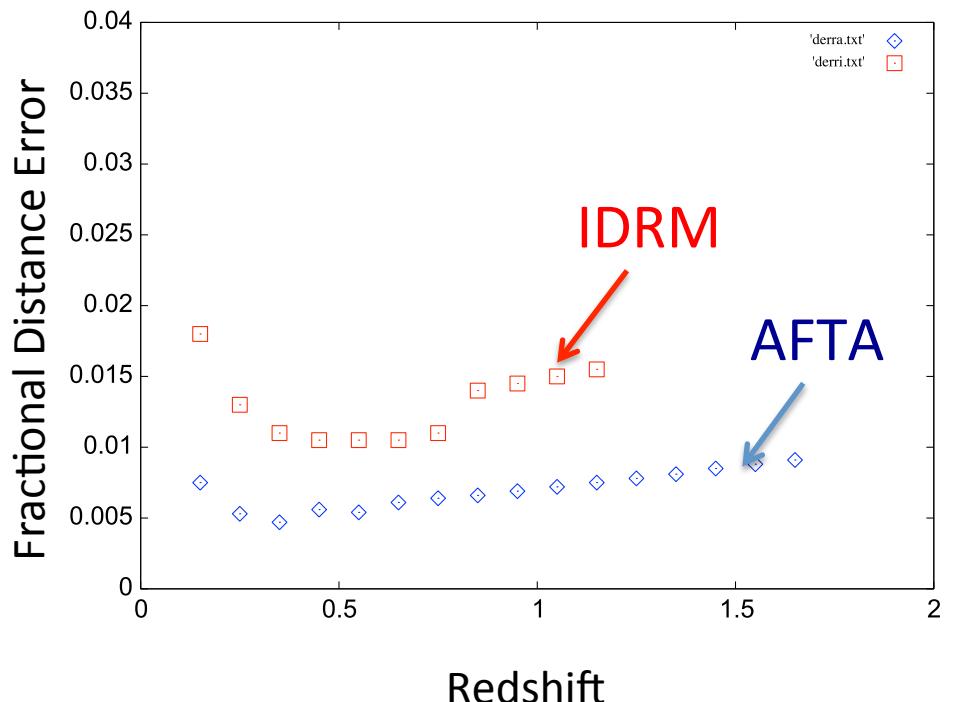
# Supernova Comparison

Larger aperture and IFU allow  
*major* improvements over DRM1  
and IDRM:

- More SNe (2750 vs. 1500)
- More even redshift distribution
- *Lower systematics*: Better photometry and calibration, no K-corrections, spectral diagnostics to compare similar high- and low-z SNe

Observing strategy can be tailored to match statistical and systematic uncertainties in each redshift bin.

Euclid has no planned SN program

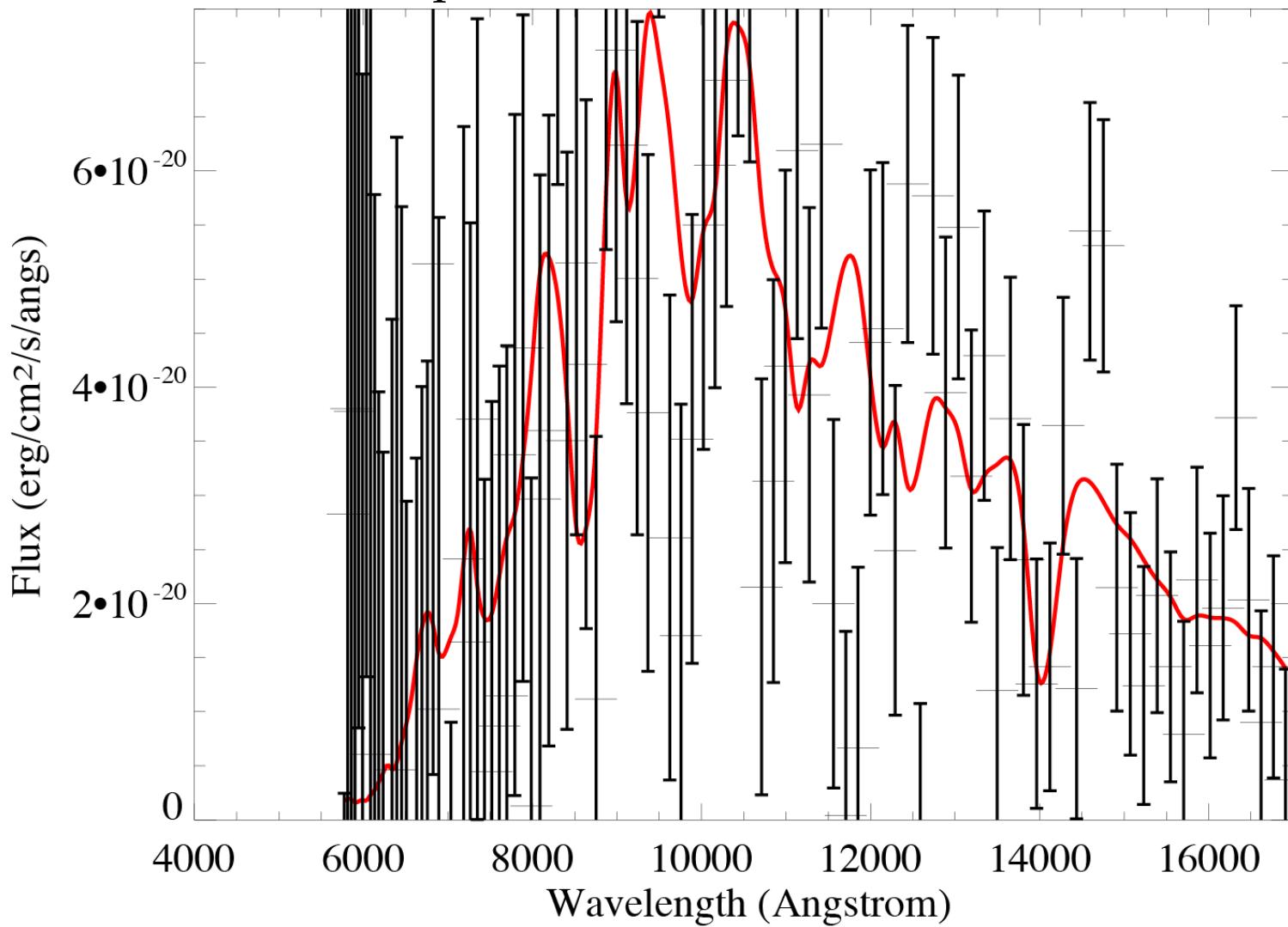


SN has greatest leverage in FoM

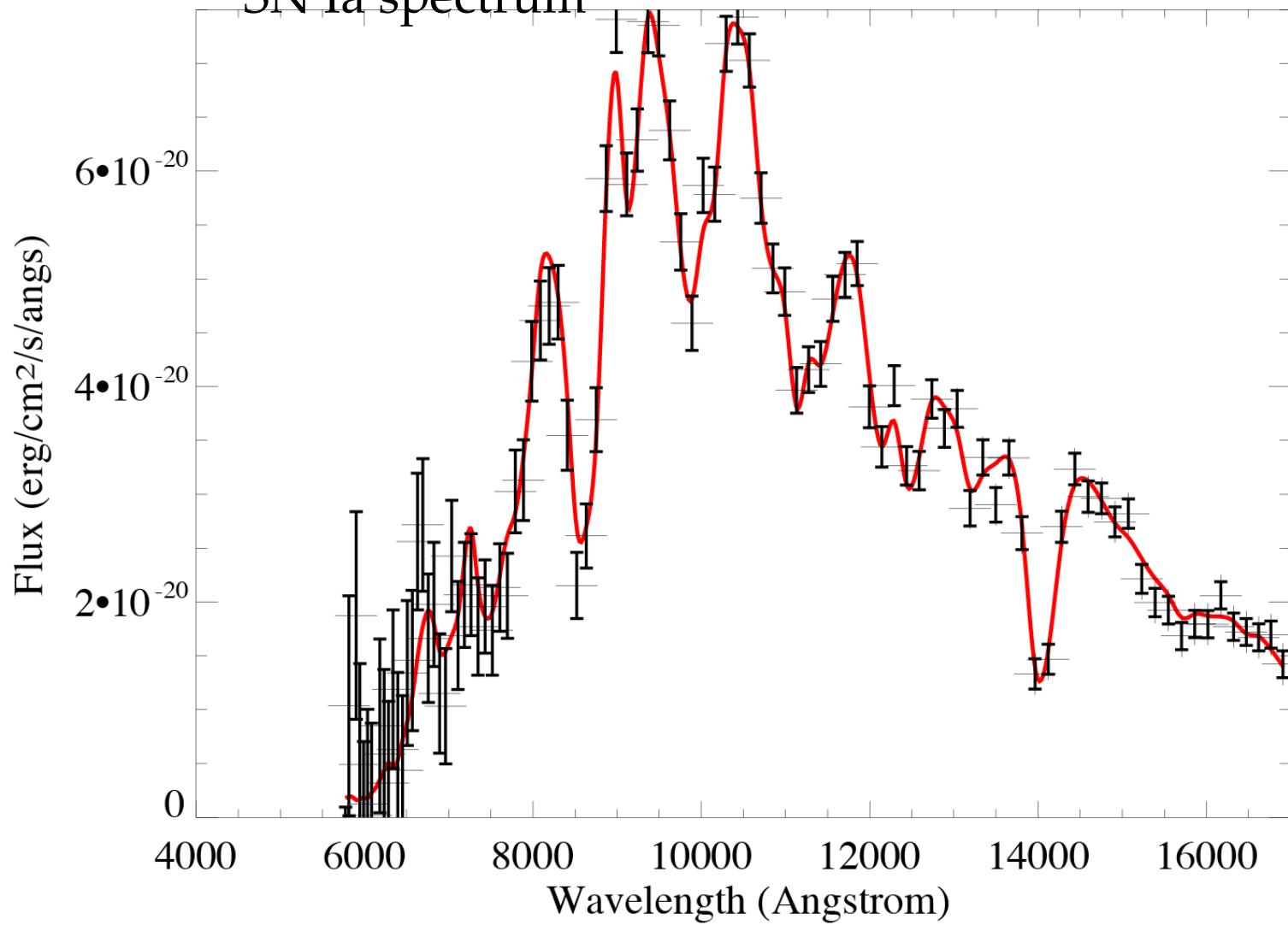
# Supernova Survey Comparisons

Feature	IDRM	WFIRST2.4
Total no of SNe	1200	2750
Z Range	0.2 – 1.2	0.2 – 1.7
Lightcurves from	Filters	IFU Spectra
Spectroscopy	Prism	Integral Field Unit
R(2 pixel)	75	75
Peak S/N *	15	47
$\sigma(\text{dist})$ at best z	0.007-0.010	0.0045
FoM(AFTA)/FoM(IDRM) **	1.0	2.3 – 3.4

# Signal-to-Noise of 1 SN Ia spectrum



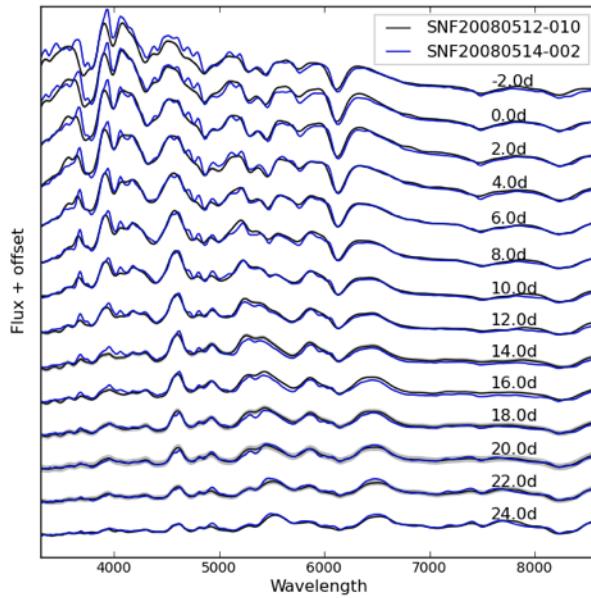
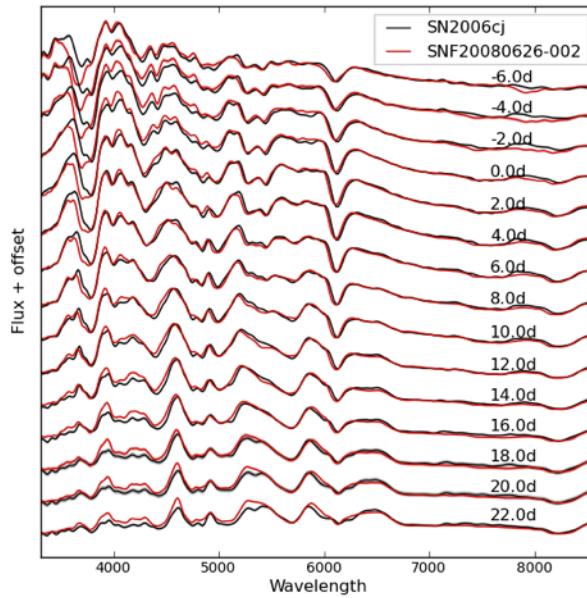
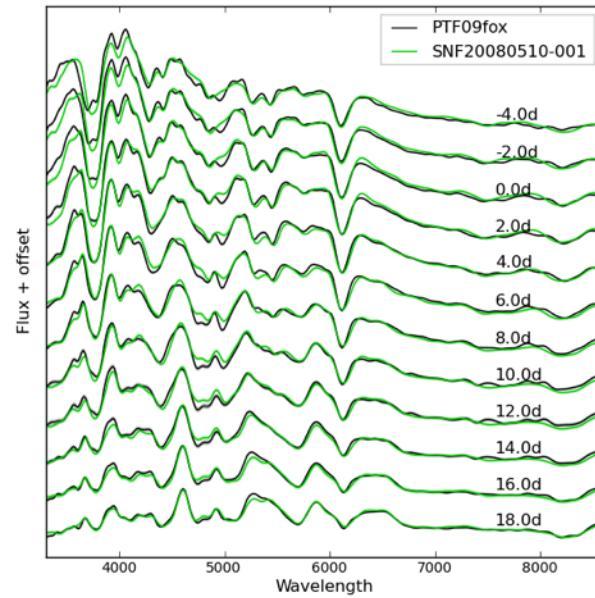
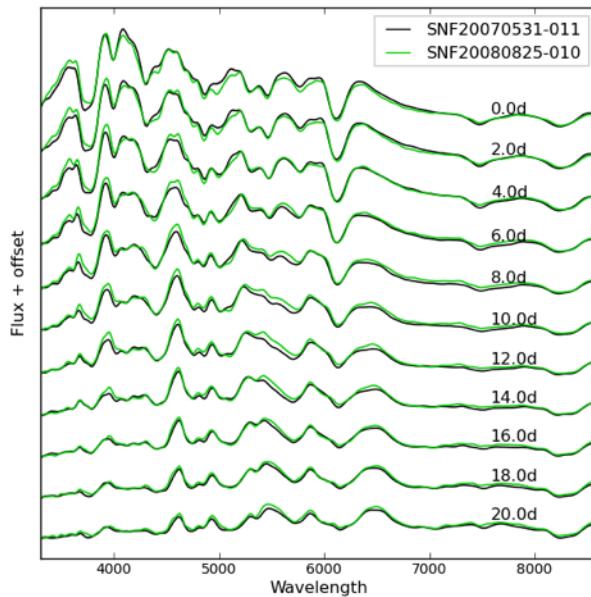
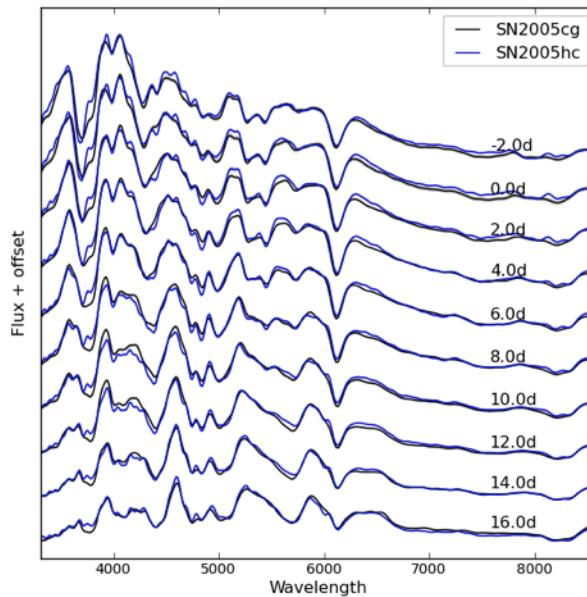
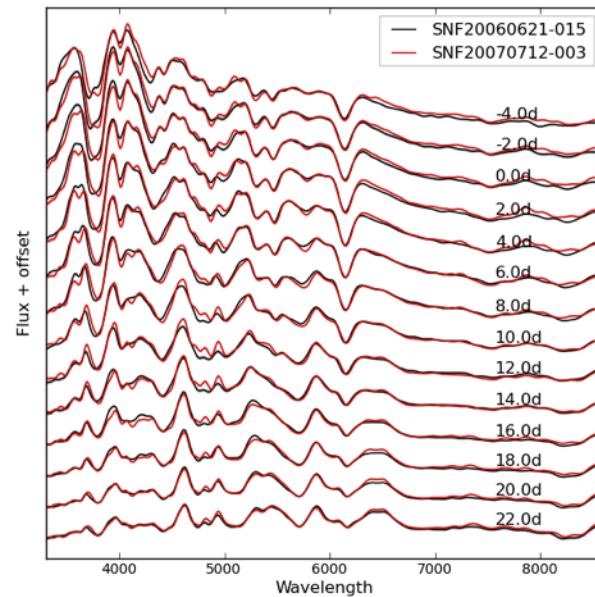
## Signal-to-Noise of 7 SN Ia spectrum

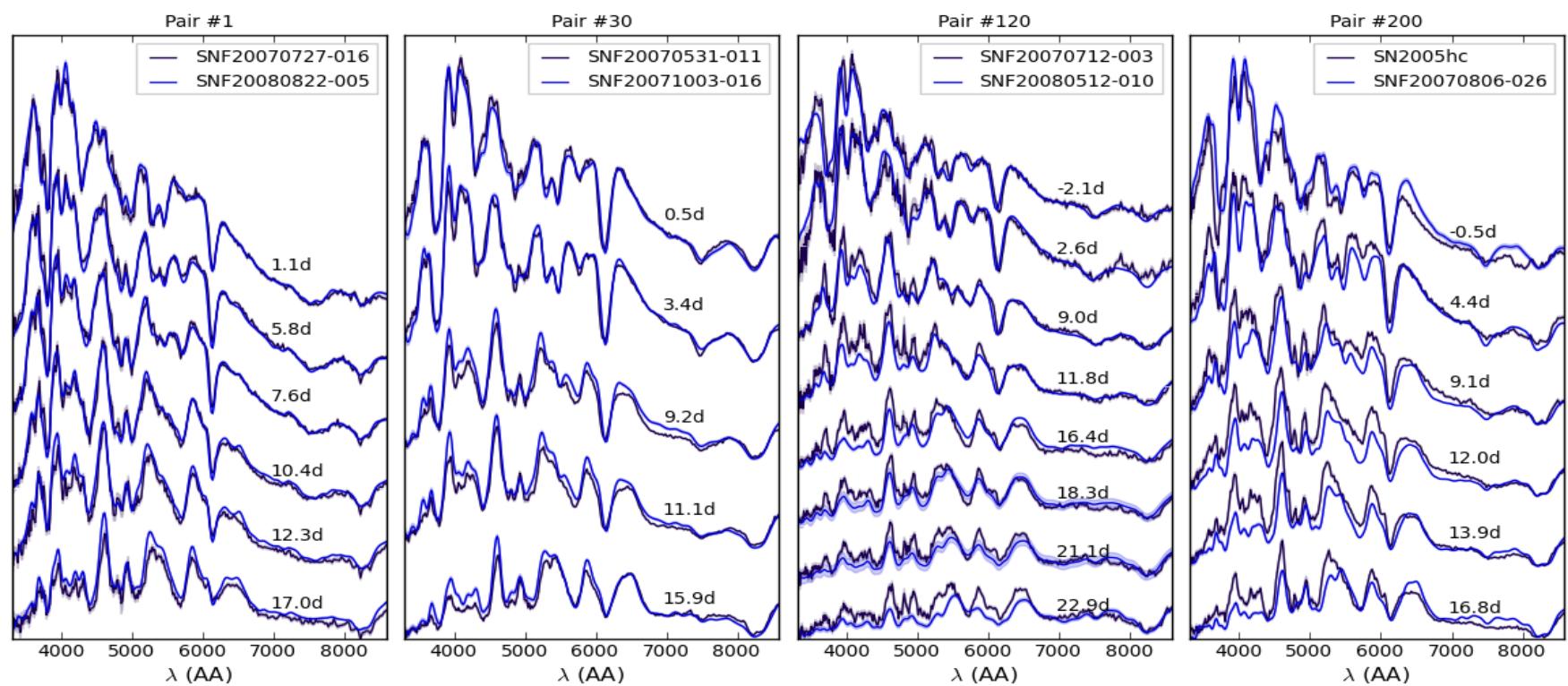
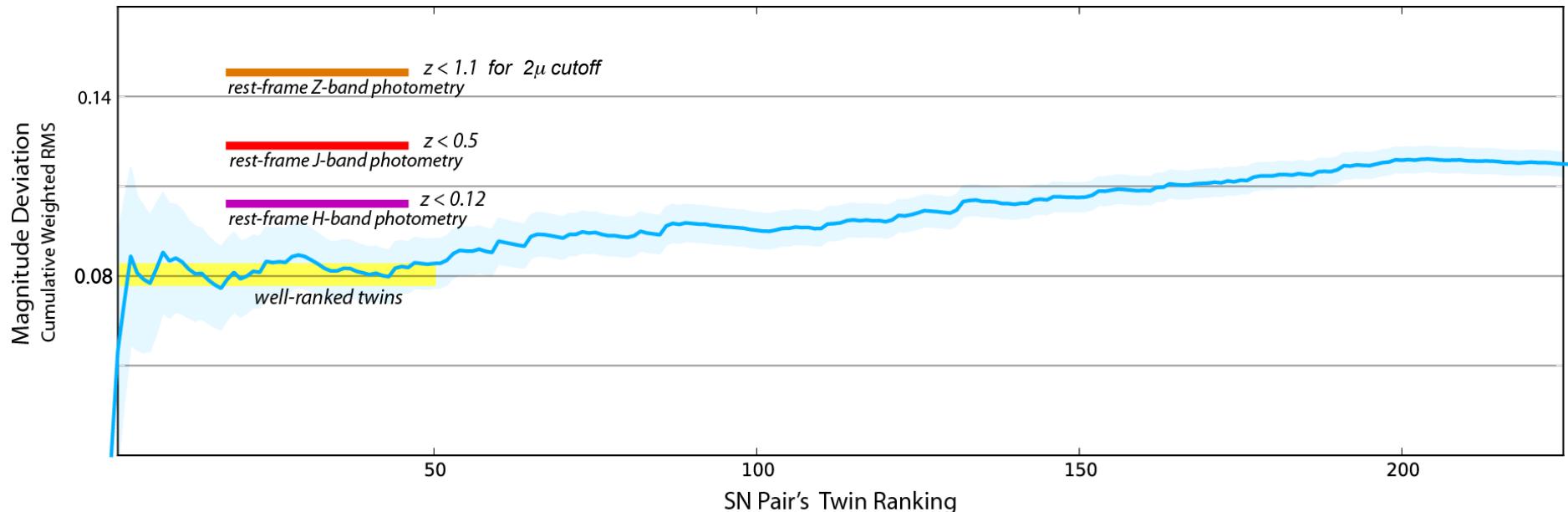


High quality SN spectra will  
also produce insights into SN  
progenitors

# SN Twins

Nearby Supernova Factory





# Weak Lensing Comparison

## Comparison to DRM1

- + Smaller survey area ( $2000 \text{ deg}^2$  vs.  $2700 \text{ deg}^2$ ) but higher  $n_{\text{eff}}$  ( $74 \text{ arcmin}^{-2}$  vs.  $36 \text{ arcmin}^{-2}$  when stacked) leads to  $1.5\times$  increase in galaxy number, corresponding to about  $1.5\times$  improvement in FoM contribution.
- + Higher  $n_{\text{eff}}$  makes higher order statistics much more powerful, allows detailed dark matter maps, greater gains in extended survey
- + STOP analysis shows best performance of all designs studied (PSF stability)

## Comparison to Euclid

- Euclid has lower  $n_{\text{eff}}$  ( $20\text{-}35 \text{ arcmin}^{-2}$ ) but larger area ( $15,000 \text{ deg}^2$ ) with 6 years devoted to dark energy, with more shape measurements and thus higher statistical precision
- + AFTA-WFIRST has *much tighter control and cross-checks of systematics*: 8-9 exposures in 3 shape measurement filters (allowing 6 auto/cross correlations) vs. 3-4 exposures in a single wide optical filter

**AFTA-WFIRST much more likely to achieve statistics-limited accuracy**

WFIRST-2.4 IFU in Parallel Mode will provide 10-25 K spectroscopic measurements. Without large spectroscopic sample, weak lensing FoM is reduced significantly.

# Weak Lensing comparison

	Euclid	IDRM	AFTA
<b>Shape bands</b>	<b>1 [Vis]</b>	<b>2 [J/H]</b>	<b>3 [J/H/F184]</b>
<b>PSF EE50</b>	<b>0.13" [Vis]</b>	<b>0.16" [J]</b>	<b>0.12" [J]</b>
<b>Galaxy density <math>n_{\text{eff}}</math> (gal/am<sup>2</sup>)</b> [Cuts: Res>0.4, S/N>18, $\sigma_e < 0.2$ ]	<b>35</b> [21 with $N_{\text{exp}} \geq 3^*$ ]	<b>26/28</b> [36 stacked]	<b>54/61/44</b> [74 stacked]
<b># Exposures per galaxy</b>	<b>3—4</b>	<b>10</b>	<b>16</b>
<b># Observing passes per field<sup>§</sup></b>	<b>1</b>	<b>4</b>	<b>6</b>
<b>Sky coverage (deg<sup>2</sup>)</b>	<b>15,000</b> [primary mission]	<b>2,700</b> [in 1 year]	<b>2,050</b> [in 1.17 years]
<b>Statistical error on amplitude of matter fluctuations</b>	<b>0.08%</b>	<b>0.13%</b>	<b>0.10%</b>
<b>Median source redshift</b>	<b>0.8</b>	<b>1.0</b>	<b>1.2</b>

\* Defined as 3 exposures with no cosmic ray within 3 pixels of the galaxy center (the same cut as used in the WFIRST forecasts).

§ The number of passes differs from the number of exposures in that small-step dithers are not counted as separate. This determines the number of repeat observations available for null tests.

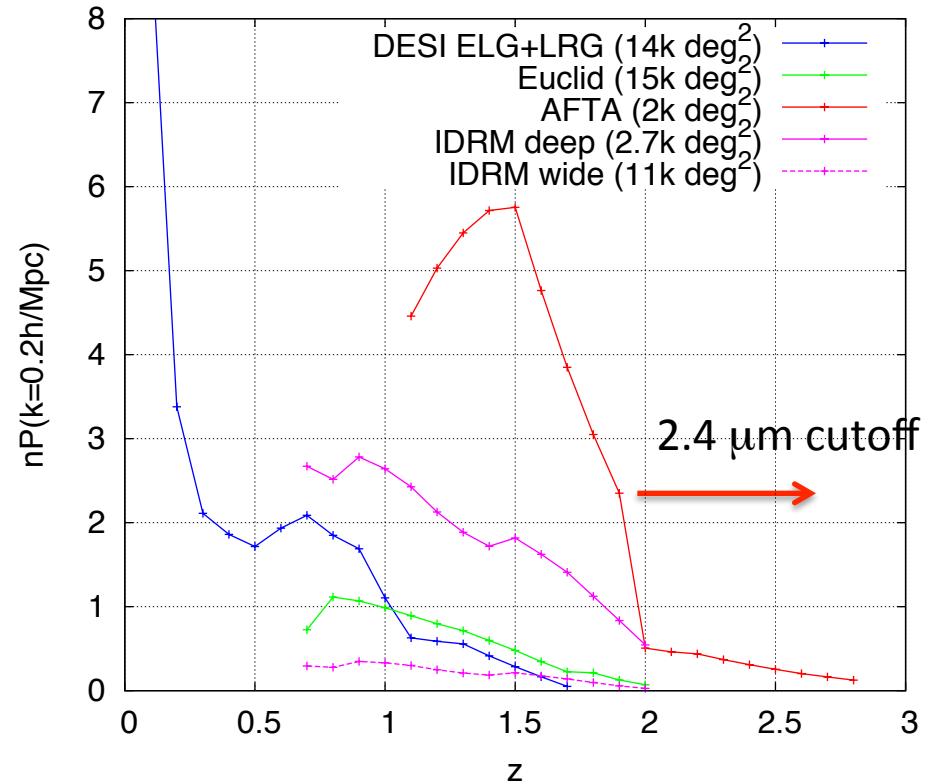
# Redshift Survey/BAO Comparison

## Comparison to IDRM

- H $\alpha$  redshift range  $z = 1-2$  (2.7) instead of  $z=0.7-2$
- Smaller survey area ( $2000 \text{ deg}^2$  vs.  $2700 \text{ deg}^2$ ) but much higher galaxy space density
- FOM ratio = 0.99 for full sample. AFTA is a 1.6x improvements for  $z > 1$
- [OIII] emitters provide sparsely sampled tracers for BAO and RSD at  $z=2-3$

## Comparison to Euclid

- Euclid has larger area but 10x lower space density.
- DESI numbers



Forecast aggregate precision: 0.40% in  $D_A$ , 0.72% in  $H$ , at  $z=1-2$   
1.3% in  $D_A$ , 1.8% in  $H$ , at  $z=2-3$  ([OIII] emitters)  
1.2% in  $\sigma_m(z)f(z)$  at  $z=1-2$  (from RSD)

# Redshift Survey Comparison

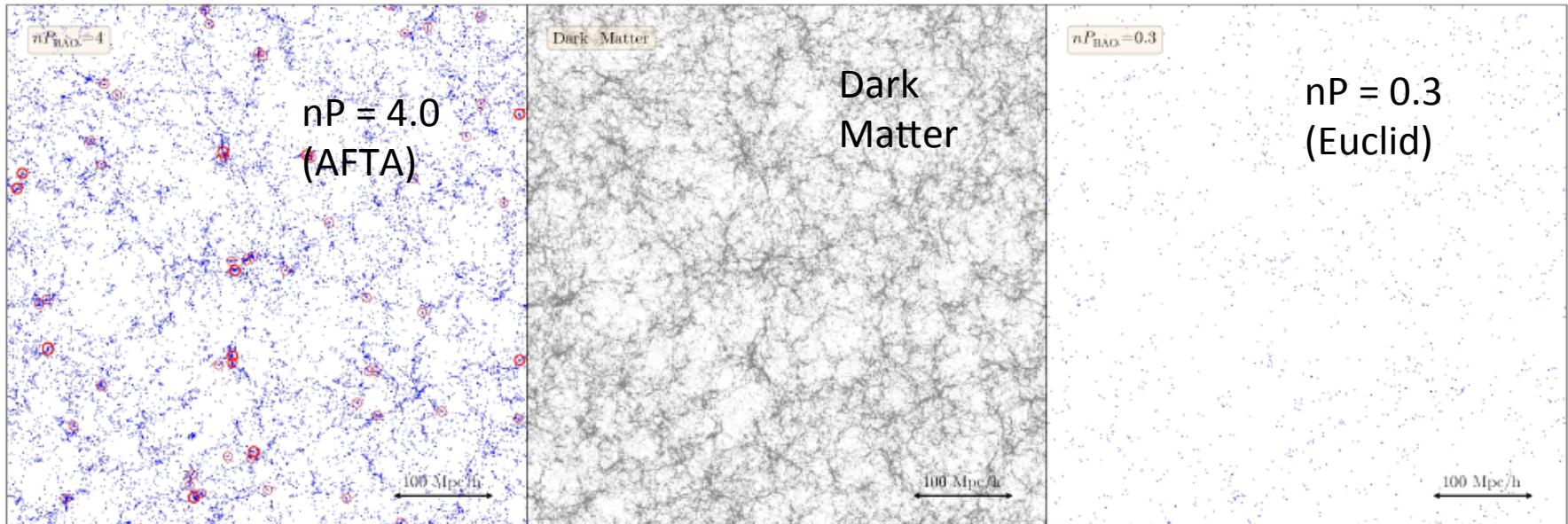
	DESI	Euclid	IDRM	AFTA 2 $\mu\text{m}$ cutoff	AFTA 2.4 $\mu\text{m}$ cutoff
Redshift range	[OII], [OIII]: 0.1 < z < 1.7  LRG: 0.1 < z < 1	H $\alpha$ : 1 < z < 2	H $\alpha$ : 0.7 < z < 2	H $\alpha$ : 1 < z < 2  [OIII]: 1.7 < z < 2.9	H $\alpha$ : 1 < z < 2.7  [OIII]: 1.7 < z < 3.8
Main gal. # /( $\text{deg}^2$ )	1,300	1,700	9,300	11,600	TBD
2 <sup>nd</sup> gal. # /( $\text{deg}^2$ )	300	0	0	> 1,000	TBD
Survey time / 1000 ( $\text{deg}^2$ )	~118 days	~122 days	135 days	118 days	TBD

# Complementarity in Redshift Range and Depth enables Richer Science

Compared to Euclid and DESI: smaller survey area but much denser sampling.  
Focused on redshift range  $z>1$  that is most difficult from ground.

Density important for higher order clustering measurements, allows splits of sample to test for systematics (should get same cosmology from different galaxies).

Simulated slices at  $z=1.5$ . Circles mark clusters of  $5\text{e}13$  and  $1\text{e}14$ .



# DETF-FOM Improvement

	Norm. to IDRM
Supernova	2.3-3.4
BAO (for $z > 1$ )	1.6
Weak lensing	1.5 (x 1-1.7 for IFU redshifts)

The FoM comparison underestimates improvement :

- Significantly improved control of systematics (particularly for SN)
- Significantly improved higher order statistics (WL)
- Improved complementarity to other surveys (higher median redshift)
- Increased flexibility

# The WFIRST-2.4 Dark Energy Roadmap

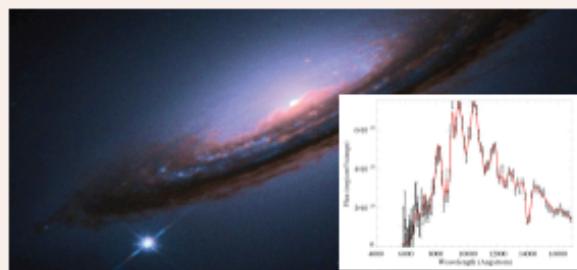
## Supernova Survey

wide, medium, & deep imaging  
+  
IFU spectroscopy

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2700 type Ia supernovae  
 $z = 0.1\text{--}1.7$

standard candle distances  
 $z < 1$  to 0.20% and  $z > 1$  to 0.34%



## High Latitude Survey

spectroscopic: galaxy redshifts

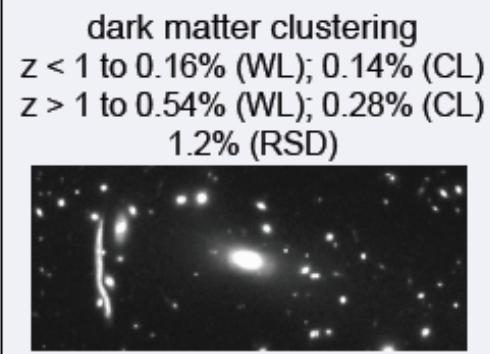
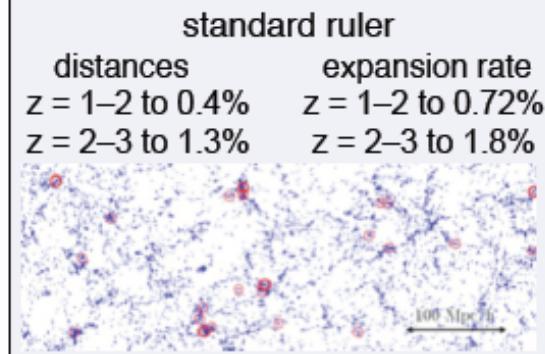
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imaging: weak lensing shapes

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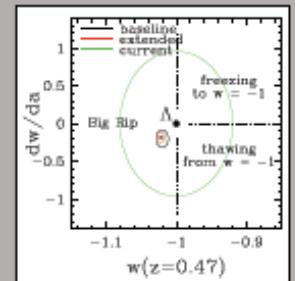
500 million lensed galaxies  
40,000 massive clusters



history of dark energy  
+  
deviations from GR

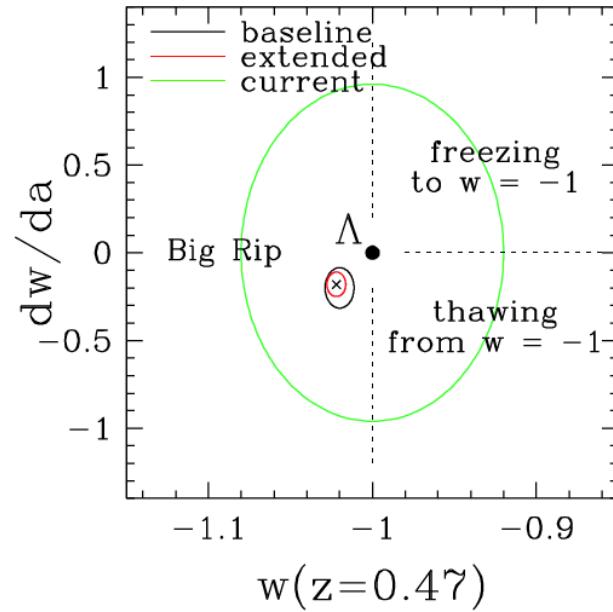
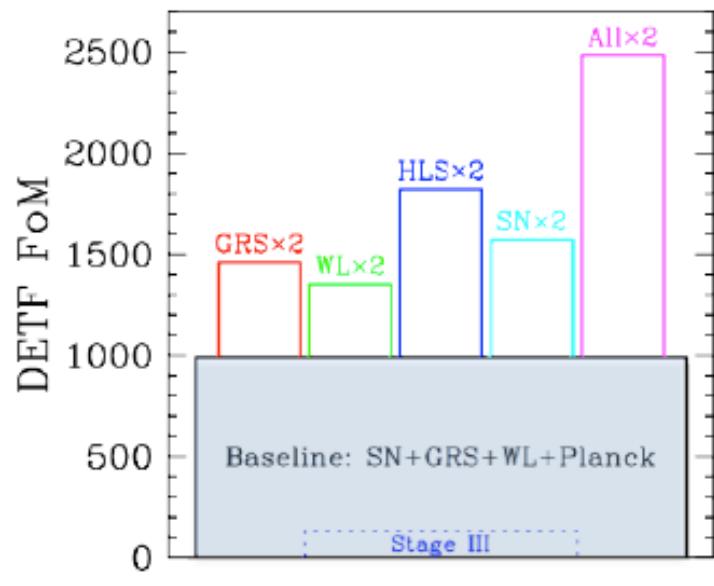
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$w(z)$ ,  $\Delta G(z)$ ,  $\Phi_{\text{REL}}/\Phi_{\text{NREL}}$



# BACKUP SLIDES

- Supernova
- Increased Flexibility
- Weak Lensing
- IFU
- BAO
- Dark Energy
- Planck
- Euclid



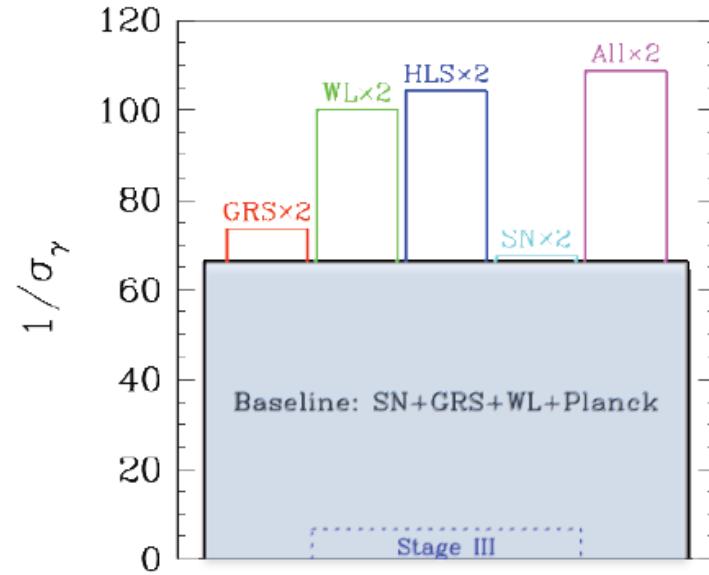
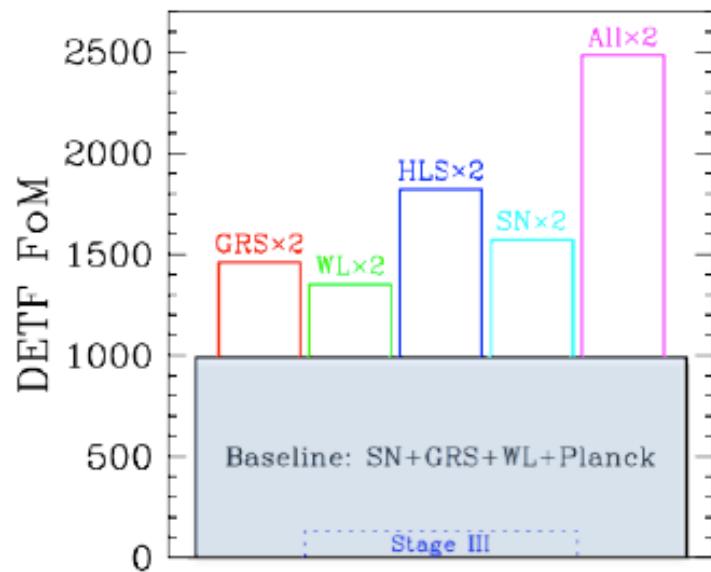
$\text{FoM} = [\sigma(w_p) \times \sigma(w_a)]^{-1}$  for baseline case is 7.5 $\times$  increase over “Stage III” forecast.

This represents big advance in ability to distinguish physically interesting models.

All elements of program contribute, as one sees by doubling precision of any one of them; such doubling might be achieved by further tightening systematics, increasing survey area in extended mission, better theoretical modeling.

Calculation includes AFTA-WFIRST, Planck, local SN calibrators, BOSS.

Doesn’t include cluster-galaxy and galaxy-galaxy lensing; forecasts for these are more uncertain, but likely to improve constraints significantly.



Major advance in testing modified gravity explanations of cosmic acceleration, here parameterized by deviation of growth index  $\gamma$ .

With baseline assumptions, WL dominates these constraints; cluster-galaxy and galaxy-lensing likely to improve them by significant factor.

Comparison of WL and RSD is itself an important test of modified gravity models; affected by different gravitational potentials that are equal in GR.

AFTA-WFIRST RSD also probes higher redshift.

# Why did the IFU become baseline in AFTA-WFIRST?

## *Lower systematics*

Better calibration:

- Each pixel on detector illuminated by light of fixed wavelength for both source and backgrounds

- Total # of pixels to calibrate is small; feasible to scan standard star along length of each slice in IFU

No K-corrections; compare SNe at fixed rest-frame wavelength (slitless spectra have much higher background noise)

Spectral diagnostics for sub-typing SNe; reduce evolutionary systematics and add cross-checks by comparing like-to-like across redshift.

## *Better statistics*

More efficient than wide-field slitless spectroscopy because exposure time tailored to each individual SN. More SNe measured.

Redshift distribution can be tailored to be optimal.

This gain is much larger for the 2.4m than 1.3m aperture.

*See Perlmutter slides for much further detail and additional benefits of IFU.*

## Why did the IFU become baseline in WFIRST-AFTA?

<b>SN data quality</b>	<p>“Clean” SN spectrum now available: Host galaxy light contamination can be removed from SN spectrum by image-subtraction algorithm.</p> <p>Each SN observation now has full wavelength range of WFIRST.</p>
<b>Systematic error control</b>	K correction systematic error now removed: each observation performed with spectrophotometry.
	SN evolution (population drift) can now be controlled by matching high-S/N spectrum to low-redshift SN standards. Feasible with 2.4m telescope.
	Photometry calibration systematic errors now controlled wavelength-by-wavelength at $R \sim 100$ .
Observing efficiency	More time-efficient SN follow-up strategy now available: after discovery, faster to follow individual SN with tuned exposure times.
Science results	Can now follow $>\sim 150$ SNe in each redshift bin ( $\Delta z = 0.1$ ) from $z = 0.2$ to 1.7, with same S/N, yielding sub-percent distances.
	Dark Energy Figure of Merit (FoM=312 from SN alone) now 3.4x higher than IDRM, and SN is now the single most important contributor. Combined FoM with BAO (WFIRST or Euclid) also significantly higher, i.e., SN is complementary to BAO even when measuring distances at the same redshifts .
<b>Weak Lensing data</b>	Parallel IFU spectroscopy during imaging surveys yields 10K–25K galaxy spectra out to $z \sim 4$ , required to calibrate photo-z's for WL.
Science results	DE FoM from WL could be 1.6x higher, with these IFU photo-z calibrations.
<b>WFIRST WFC calibration</b>	The IFU would be the anchor for photometric calibration of the entire WFIRST Wide Field Camera.

# Comments on dark energy Figures of Merit

Widely used measure is  $\text{FoM} = [\sigma(w_p) \times \sigma(w_a)]^{-1}$  for forecast errors on a model in which  $w(a) = w_p + w_a(a_p - a)$ , assuming standard matter and radiation content and GR, allowing non-zero curvature. Typically  $a_p \approx 0.7$ .

Useful standard of comparison and optimization, but doesn't account for sensitivity to GR deviations or early dark energy.

Assumptions about systematic uncertainties have big impact on FoM.

We focus on FoM of combined program and variants around it; much less sensitive to external assumptions than “single-probe” FoM.

We also characterize probes by the aggregate fractional precision with which they measure their primary observable, including estimate of systematic error contribution.

More model-independent than FoM.

Contribution to FoM generally scales as  $(\sigma_{\text{agg}})^{-2}$ .

# Supernova Survey Comparison

- The better instrument enables a much better supernova survey
- More supernovae over a broader redshift range with better signal to noise at supernova peak light, which translates into a better distance measurement precision and a better Figure of Merit.
- The high signal to noise spectra enabled by the Integral Field Spectrometer (IFU) promises reduced and better control of systematic errors that allow AFTA-WFIRST2.4 to fully capitalize on the improved statistical errors of the larger sample of supernovae produced by the larger mirror.

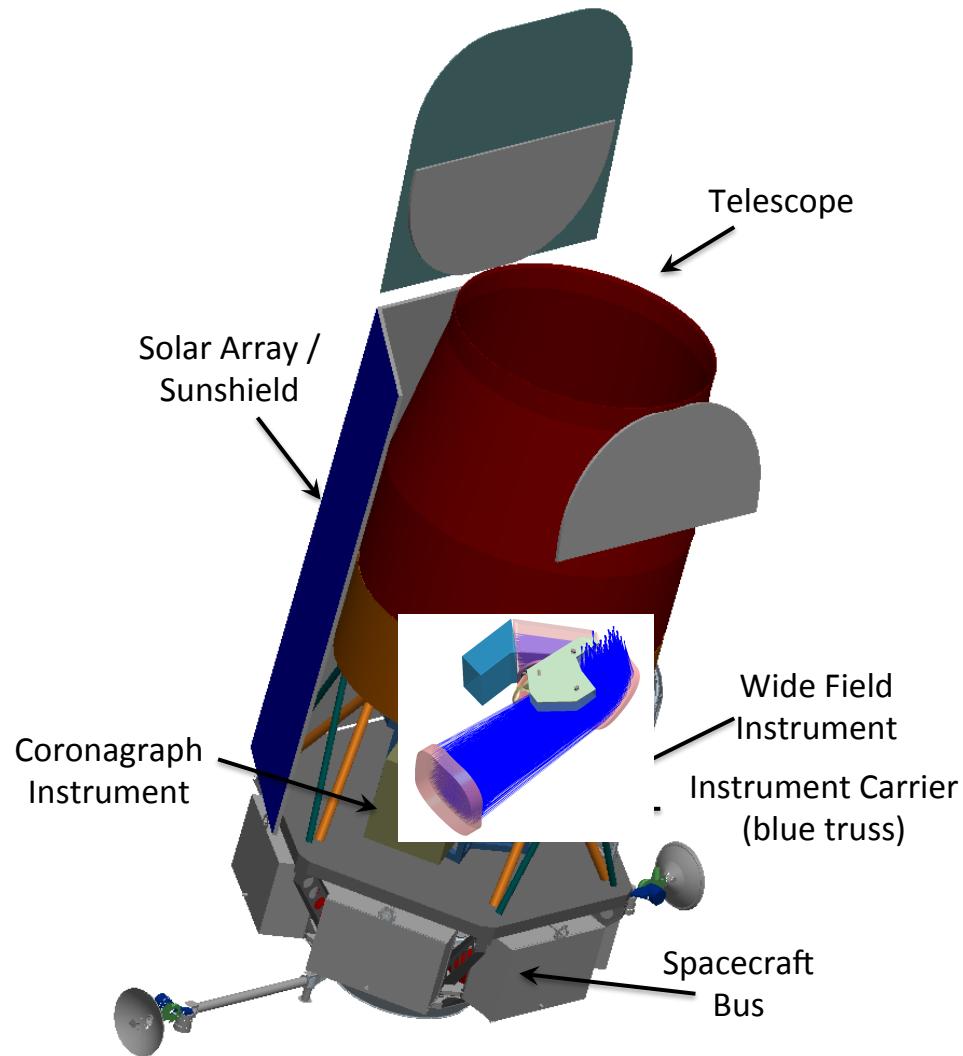
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	Much higher S/N spectra (slitless spectra had much higher background noise).
Systematic error control	K correction systematic error now removed: each observation performed with spectrophotometry.
	SN evolution (population drift) can now be controlled by matching high-S/N spectrum to low-redshift SN standards. The 2.4-m & IFU make this possible.
	Photometry calibration systematic errors now controlled wavelength-by-wavelength at $R \sim 100$ . Each pixel on detector illuminated by light of fixed wavelength for both source and backgrounds, and total # of pixels to calibrate is small enough that standard stars can be scanned along each slice of IFU.
Observing efficiency	More time-efficient IFU-follow-up strategy now available: after discovery, faster to follow individual SN with tuned exposure times – and redshift distribution can be tailored to be optimal. This gain is even larger for AFTA than IDRM.
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Weak Lensing data	Parallel IFU spectroscopy during imaging surveys yields 10K--25K galaxy spectra out to $z \sim 4$ , required to calibrate photo-z's for WL. This will feed into improved DE FoM from WL.
Mission Cost/Complexity	IFU simplifies pointing, calibration, and stability requirements.

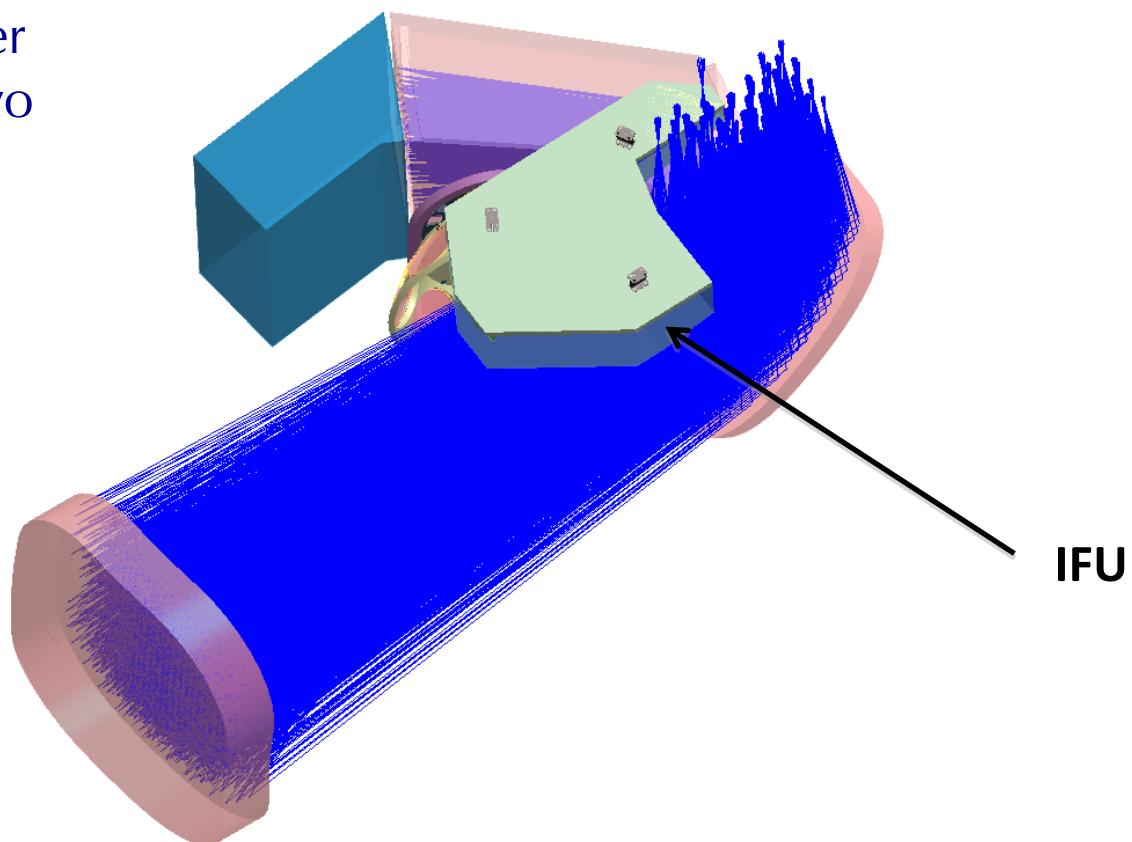
## WFIRST-AFTA Supernova Program: Improvements over IDRM

SN data quality	<p>“Clean” SN spectrum now available: Host galaxy light contamination can be removed from SN spectrum by image-subtraction algorithm.</p> <p>Each SN observation now has full wavelength range of WFIRST.</p> <p>Much higher S/N spectra (slitless spectra had much higher background noise).</p>
Systematic error control	<p>K correction systematic error now removed: each observation performed with spectrophotometry.</p> <p>SN evolution (population drift) can now be controlled by matching high-S/N spectrum to low-redshift SN standards. The 2.4-m &amp; IFU make this possible.</p> <p>Photometry calibration systematic errors now controlled wavelength-by-wavelength at <math>R \sim 100</math>. Each pixel on detector illuminated by light of fixed wavelength for both source and backgrounds, and total # of pixels to calibrate is small enough that standard stars can be scanned along each slice of IFU.</p>
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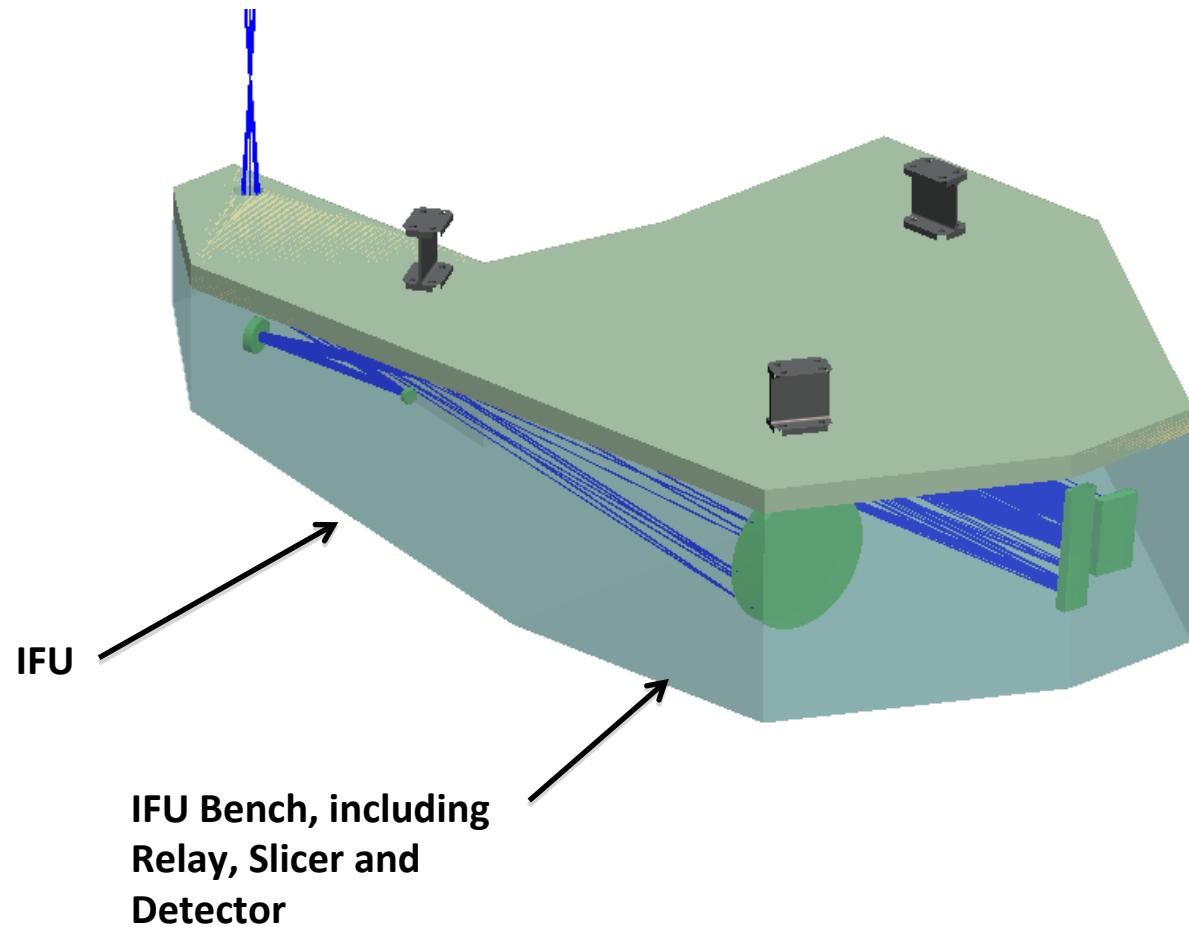


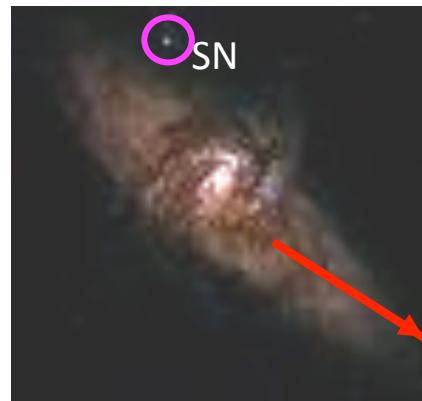
Use the 0.28 sq  
degree Wide Field  
Imager (with 0.11"  
pixels) to discover  
supernovae in two  
filter bands.



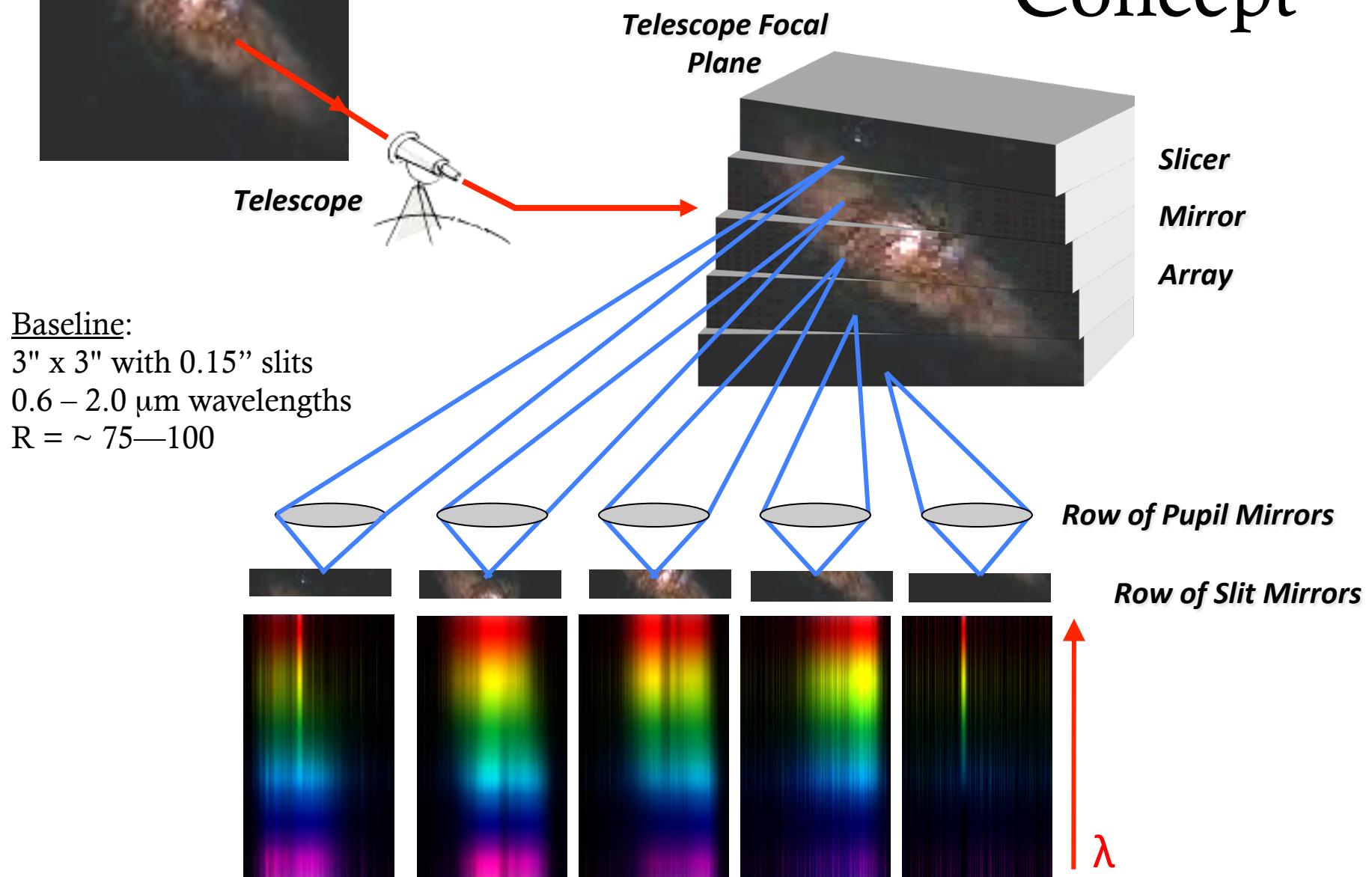
Small, compact assembly:

- ~ 6 to 7 kg
- 30 x 50 x 12.5 cm





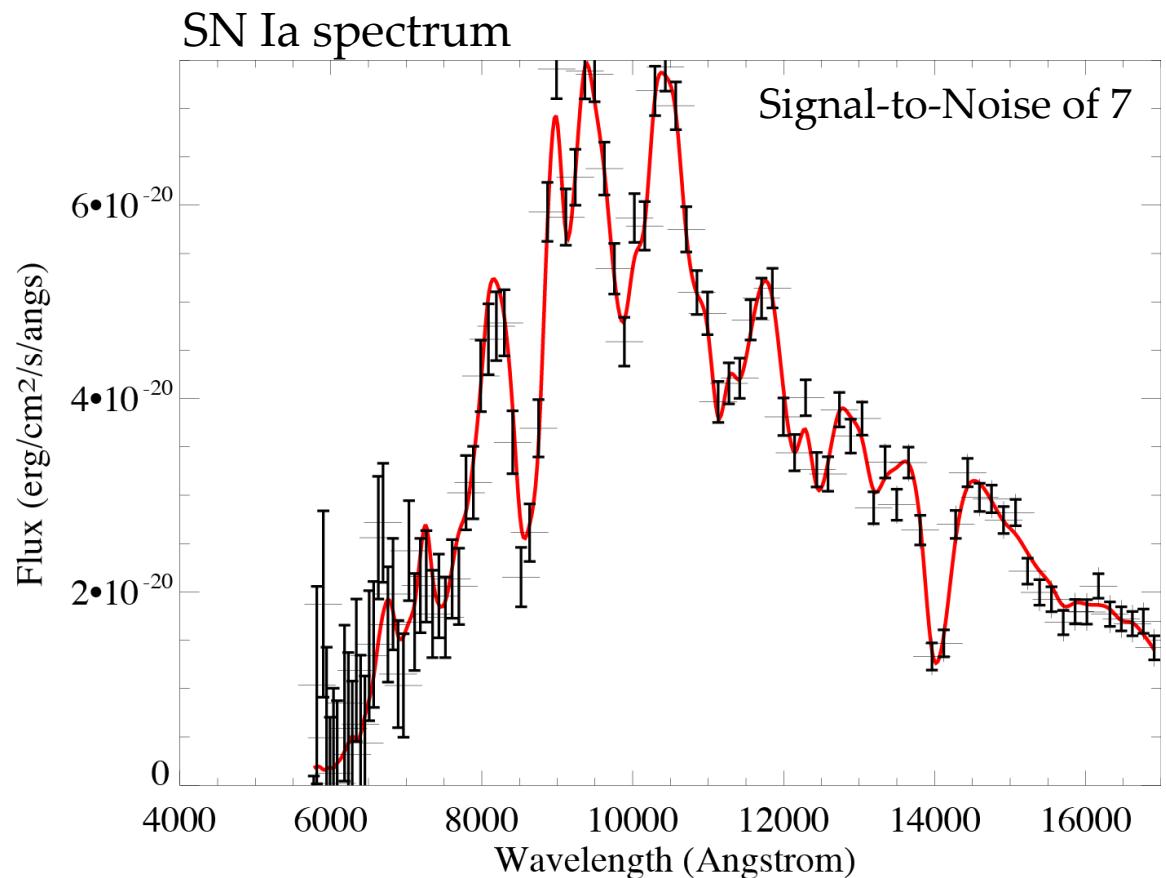
# Integral Field Spectroscopy Concept

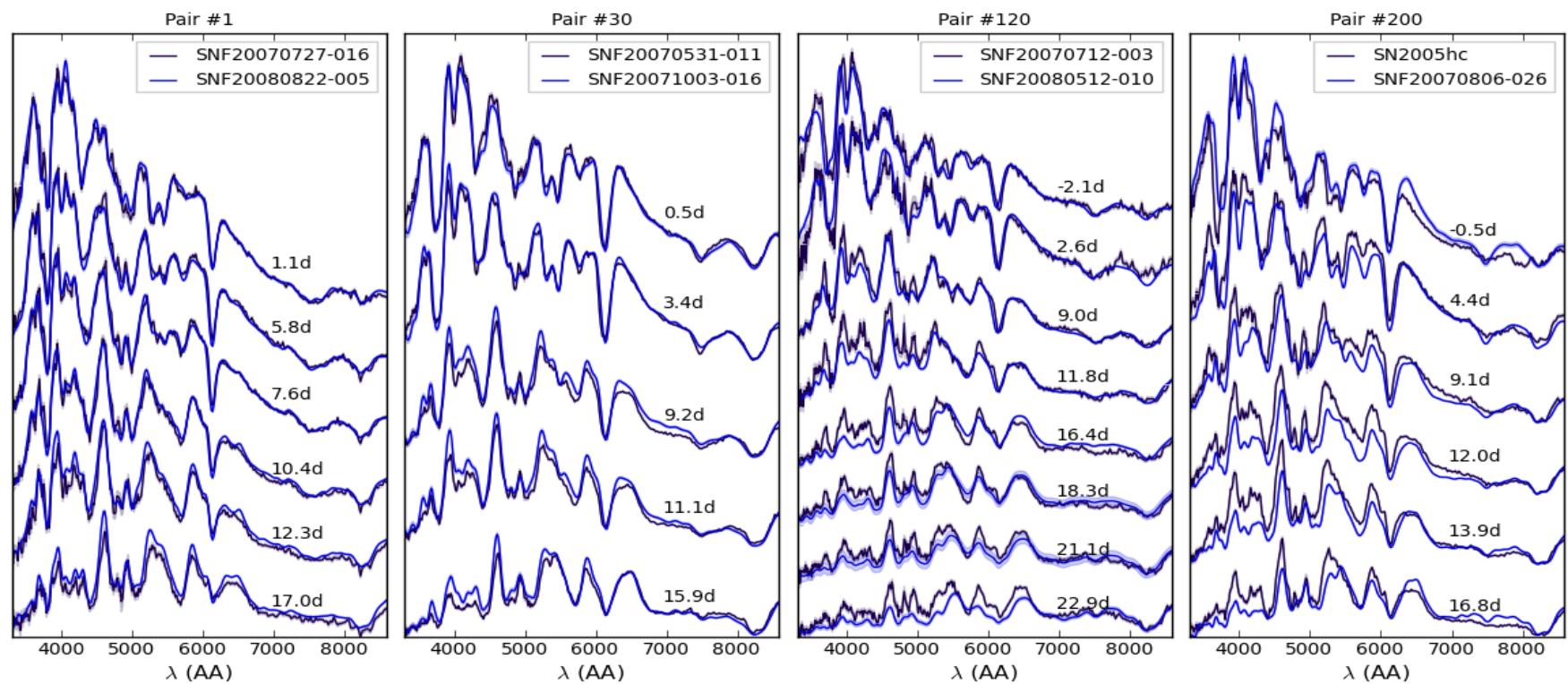
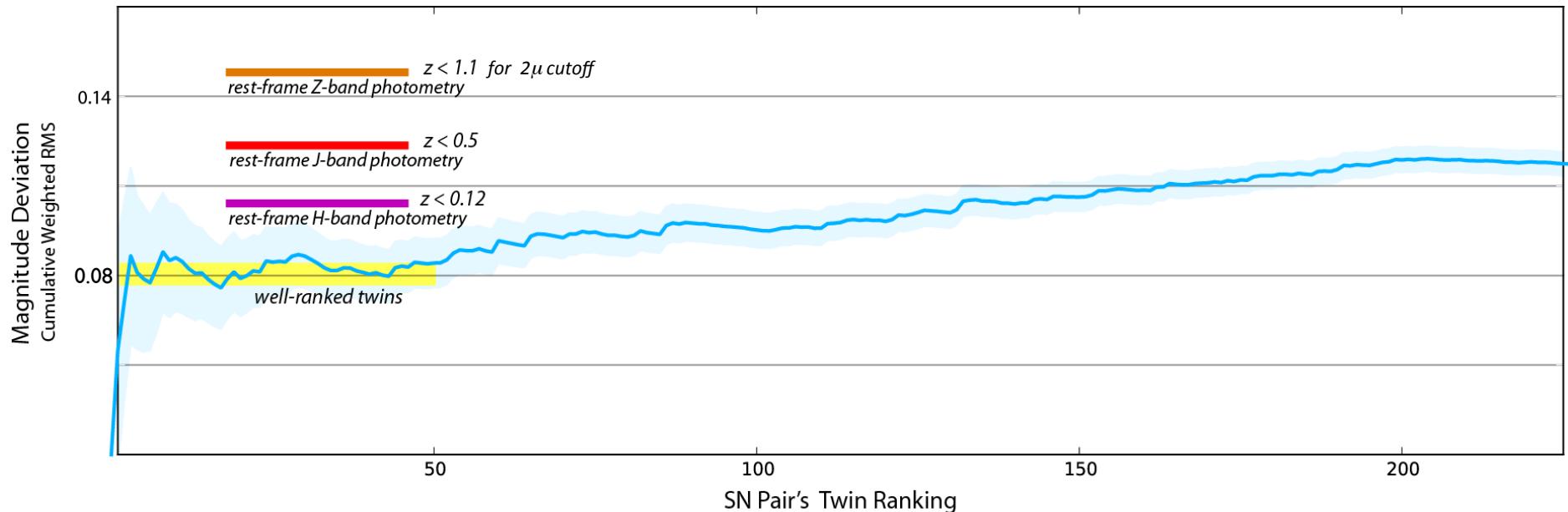


Use IFU spectra to get SN light curves with roughly a 5 day rest frame cadence.

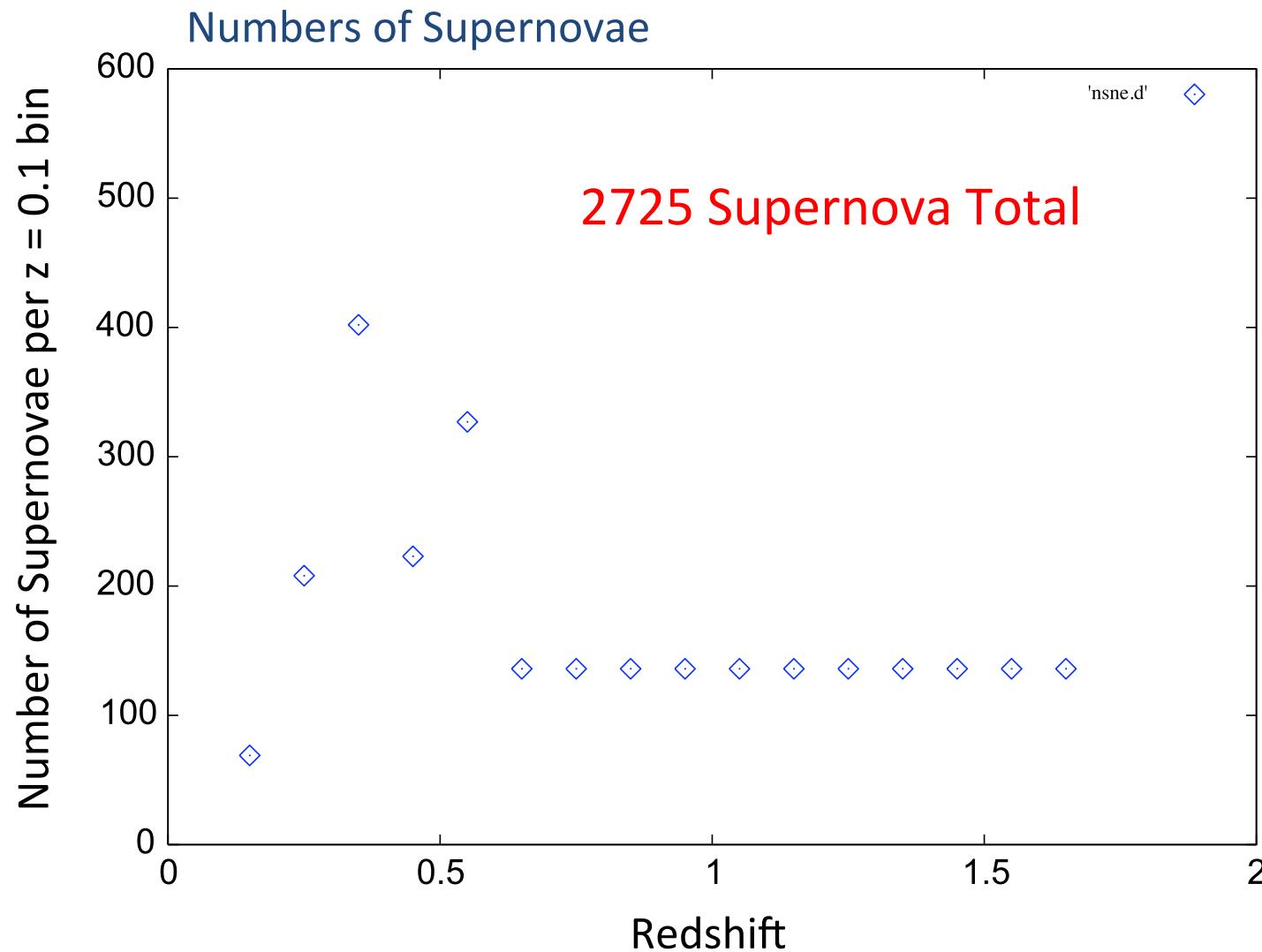
Example:

- 7 spectra on lightcurve from -10 rest frame days before peak to +25 rest frame days past peak,  $S/N = 3$  per pixel ( $S/N = 15$  per synthetic filter band)
- 1 reference spectrum after supernova has faded, for **galaxy subtraction** with  $S/N = 6$  per pixel
- 1 deep spectrum near peak for subtyping, spectral feature ratios etc. with  $S/N = 10$  per pixel

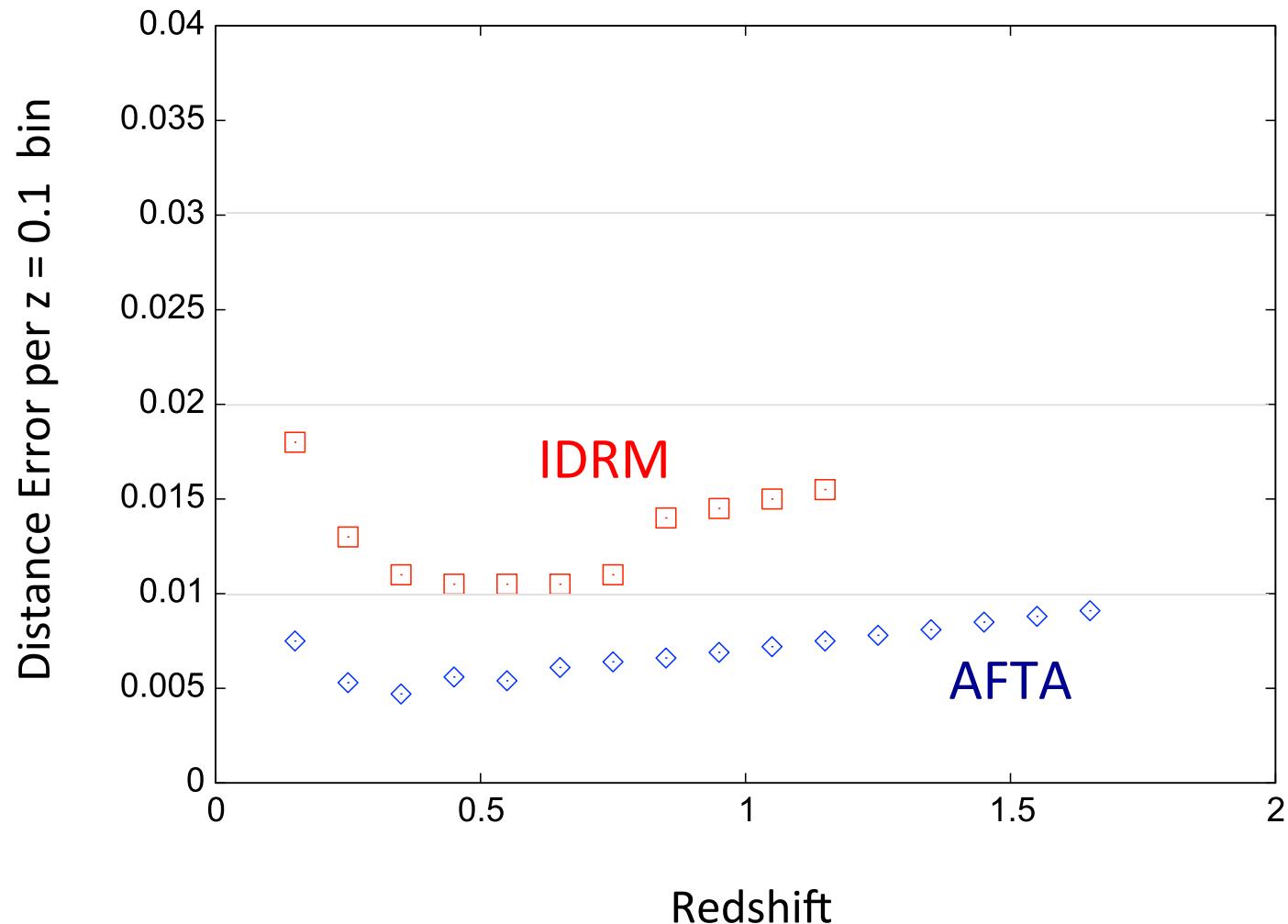




For an example: 3 tier survey, scanning different areas of sky for different redshift ranges -- for 6 months spread over 2 years calendar time – yields

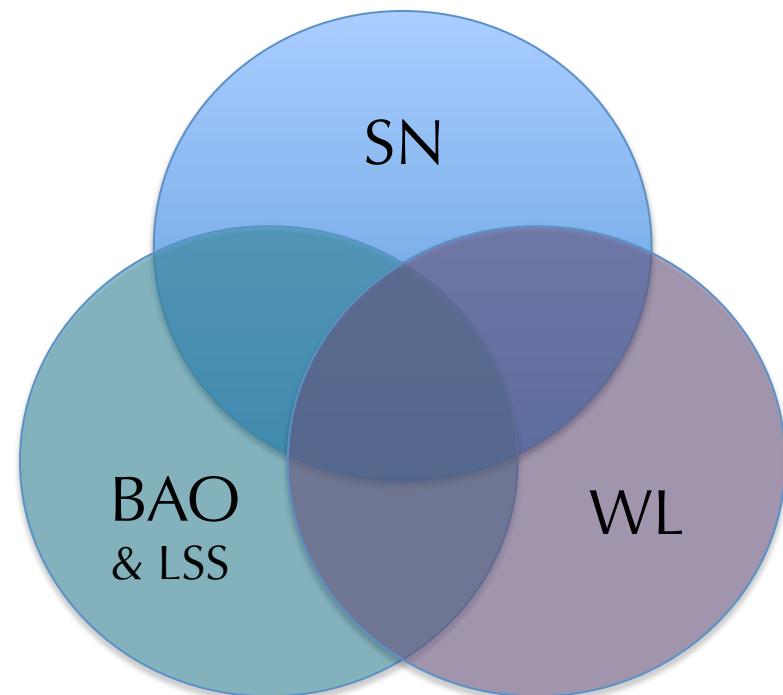


# Error on SN Distance Measurement



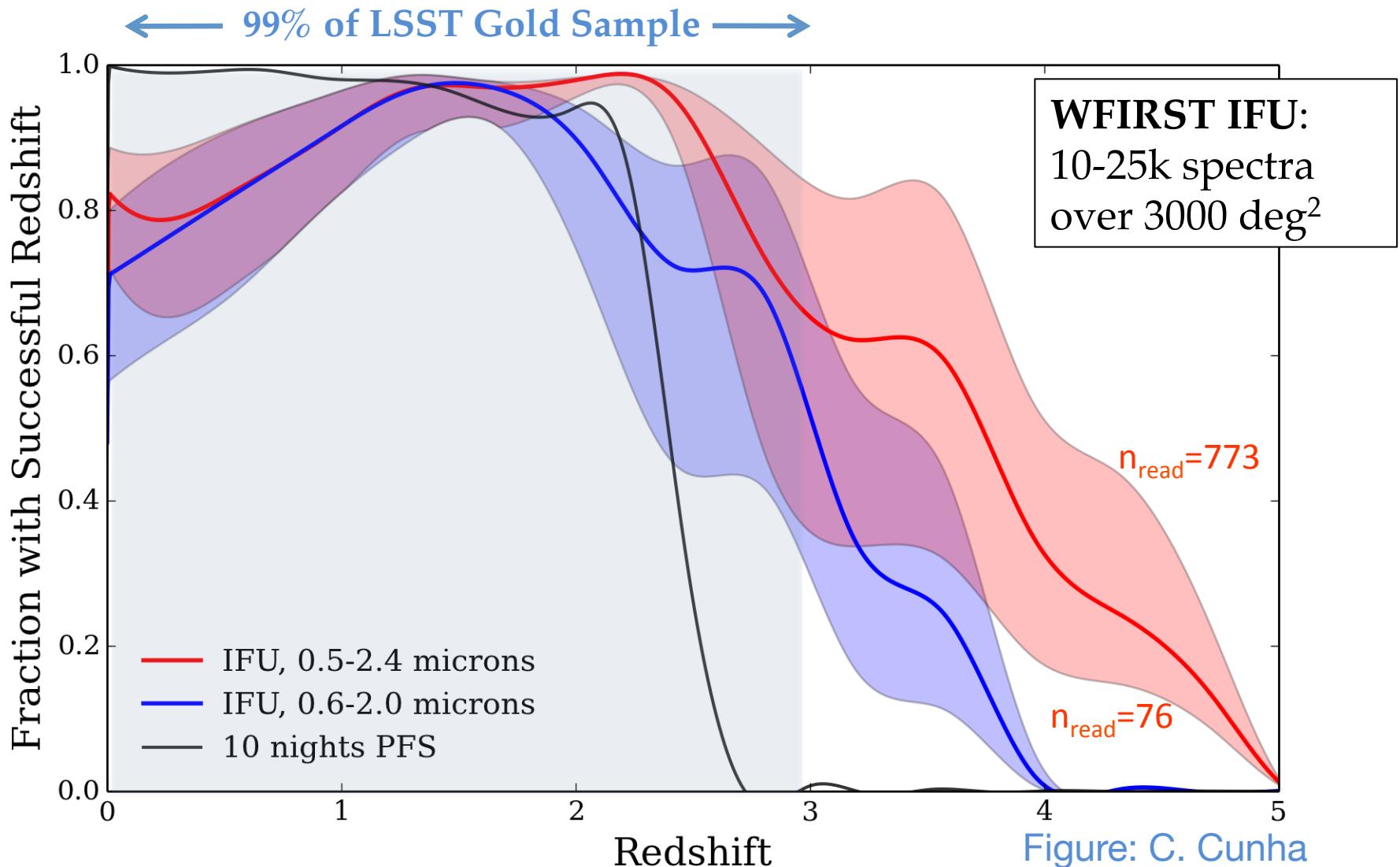
## Figures of Merit

- For the Supernova Survey only       $\text{FoM} = 312$
- Supernova with Stage III prior       $\text{FoM} = 582$

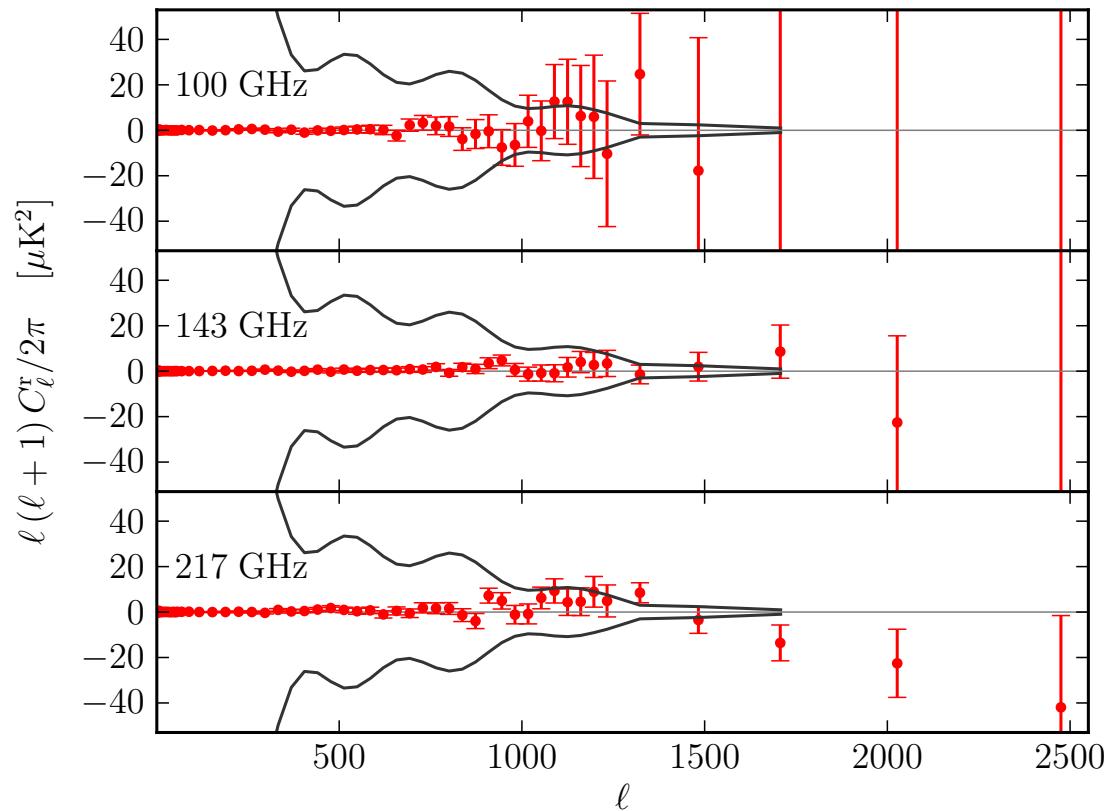


LSST &WFIRST Weak Lensing DETF FoM is  $>1.6\times$  larger if can train at  $z>2$  with IFU

A bigger issue for WFIRST WL:  $H$ -limited sample skews to higher  $z$ !



# Internal Inconsistencies in Planck



Planck Paper VI

Shows the importance  
of multiple  
measurements and  
cross-checks

## WFIRST-AFTA's Central Line of Sight (LOS) Field of Regard (FOR)

Observing Zone:

$54^\circ$  -  $126^\circ$  Pitch off Sun

Line

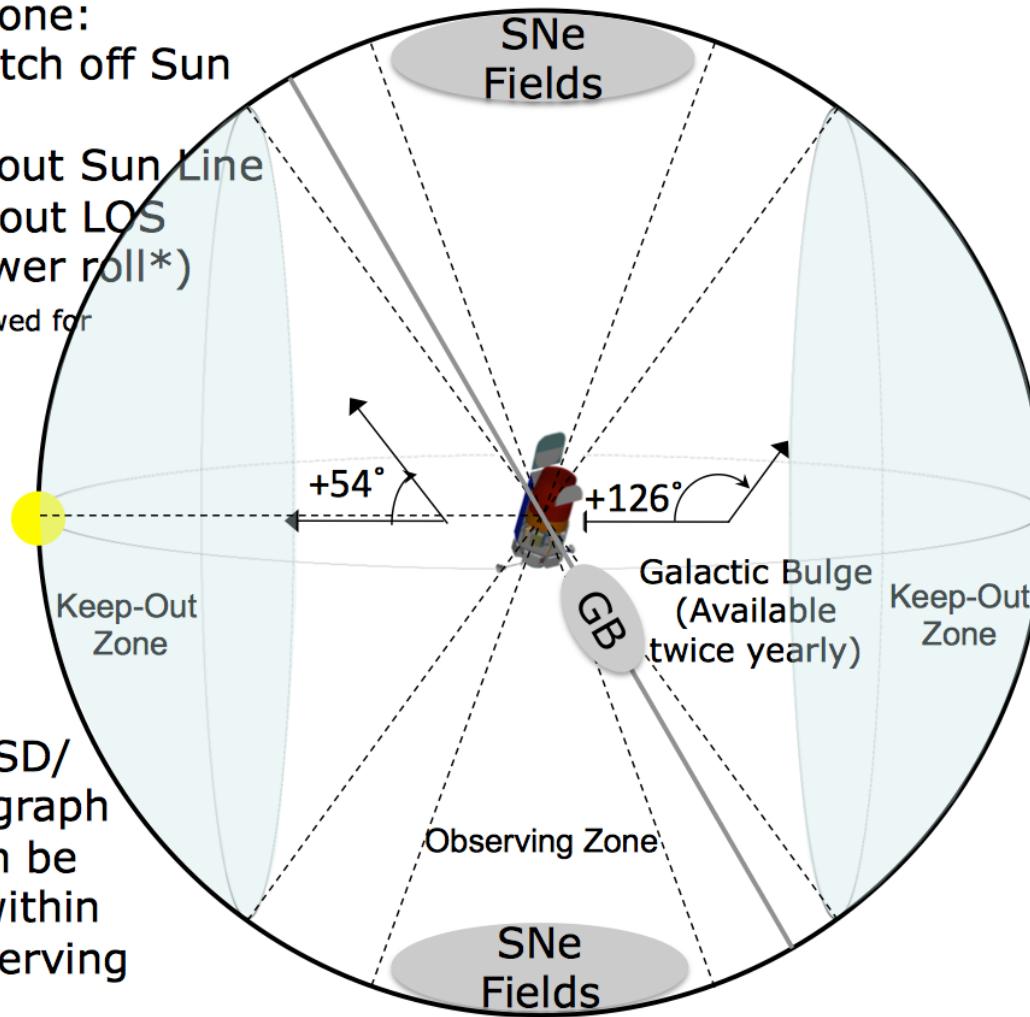
$360^\circ$  Yaw about Sun Line

$\pm 10^\circ$  Roll about LOS

(off max power roll\*)

\* Larger roll allowed for SNe

WL/ BAO-RSD/  
GO/Coronagraph  
Surveys can be  
optimized within  
the full Observing  
Zone



SNe Fixed Fields be  $\pm 20^\circ$  off one of the Ecliptic Poles,  $\pm 15^\circ$  Roll about LOS from  $90^\circ$  -  $110^\circ$

Microlensing can observe Inertially Fixed Fields in the Galactic Bulge (GB) for 72 days twice a year

# PSF Issues for WL – Part I

- Key parameters for WL are PSF size and stability.
  - Size – PSF contribution to final ellipticity scales as  $\sim(\theta_{\text{psf}}/\theta_{\text{gal}})^2$ ; exponent is 4 in the PSF ellipticity power spectrum!
    - Other aspects, such as statistical error on the ellipticity, are similarly affected, albeit with slightly different scalings.
    - For trades between PSFs of different morphologies, have used  $\frac{1}{2}$ -light radius for “size” (see next chart) – this better matches more detailed calculations than e.g. FWHM.
  - Stability – PSF must be measurable from stars before it changes.
    - Requires detailed analysis. Note that obstructed vs. unobstructed designs have different aberration patterns (e.g. dominant aberration from SM decenter is coma vs. astigmatism).
    - AFTA STOP and RWA-induced vibration analysis meets preliminary stability requirements with large margins, even in GEO. These analyses are more advanced than for previous versions of WFIRST.

# PSF Issues for WL – Part II

- See expressions for WL biases (additive and multiplicative).
  - Massey et al. paper is an update of the formalism that underlies error budgeting for weak lensing programs.
  - PSF size ( $R_{\text{PSF}}$ ) and determination errors (terms with  $\delta$ ) are key.
- A simpler PSF (off-axis) is helpful and may simplify the book-keeping for the error budget, but would not be chosen at the expense of size or stability.

$$\mathcal{A}(\ell, z_A, z_B) = \frac{1}{P_\gamma^2} \left\langle \frac{R_{\text{PSF}}^4}{R_{\text{gal}}^4} \right\rangle \langle |\delta\epsilon_{\text{PSF}}|^2 \rangle (\ell, z_A, z_B)$$

$$+ \frac{\langle |\epsilon_{\text{PSF}}|^2 \rangle}{P_\gamma^2} \left\langle \frac{R_{\text{PSF}}^4}{R_{\text{gal}}^4} \right\rangle \frac{\langle |\delta(R_{\text{PSF}}^2)|^2 \rangle}{\langle R_{\text{PSF}}^4 \rangle} (\ell, z_A, z_B)$$

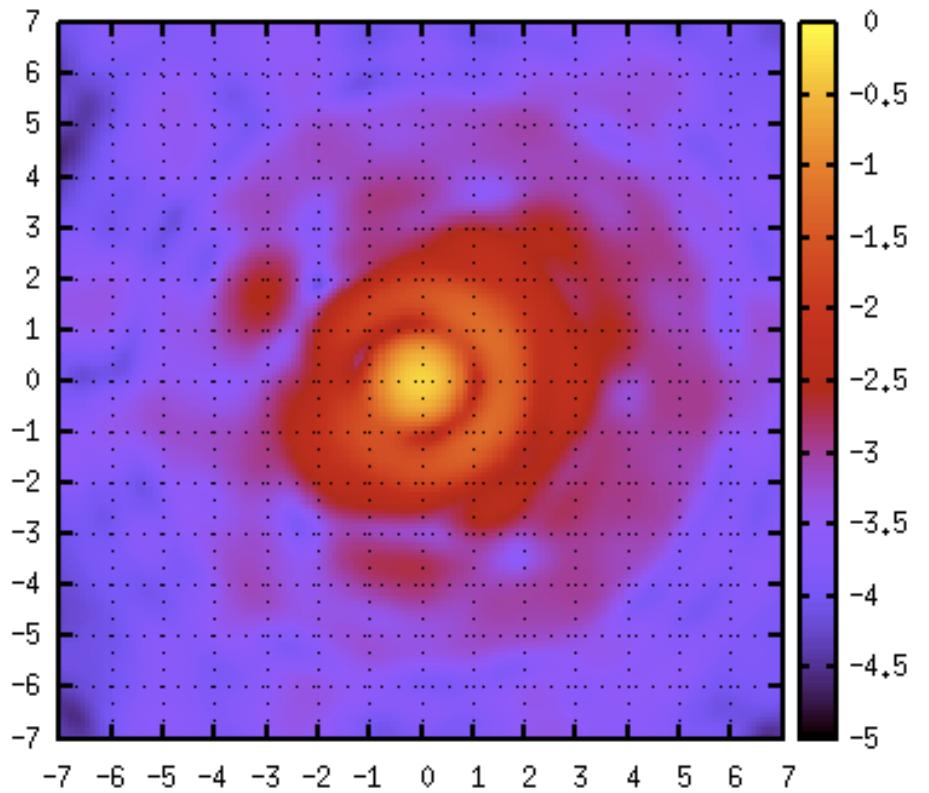
$$\mathcal{M}(\ell, z_A, z_B) = \left\langle \frac{R_{\text{PSF}}^4}{R_{\text{gal}}^4} \right\rangle \frac{\langle |\delta(R_{\text{PSF}}^2)|^2 \rangle}{\langle R_{\text{PSF}}^4 \rangle} (\ell, z_A, z_B)$$

$$+ 2 \left\langle \frac{R_{\text{PSF}}^2}{R_{\text{gal}}^2} \right\rangle \frac{\langle \delta(R_{\text{PSF}}^2) \rangle}{\langle R_{\text{PSF}}^2 \rangle} (z_A, z_B).$$

*Massey et al. 2013 (MNRAS 429, 661)*

# Obstruction Effect on PSF

- On-axis telescope leads to greater complexity:
  - More power in diffraction rings.
  - 12 spikes; complex features in inner few  $\lambda/D$  as spikes interfere with rings (see figure at right).
- Power sprayed into rings leads to worse performance than an unobstructed mirror **of the same outer diameter**.
- AFTA  $\frac{1}{2}$ -light radius is equivalent to a 1.74 m unobstructed entrance pupil (both in J band, same WFE).



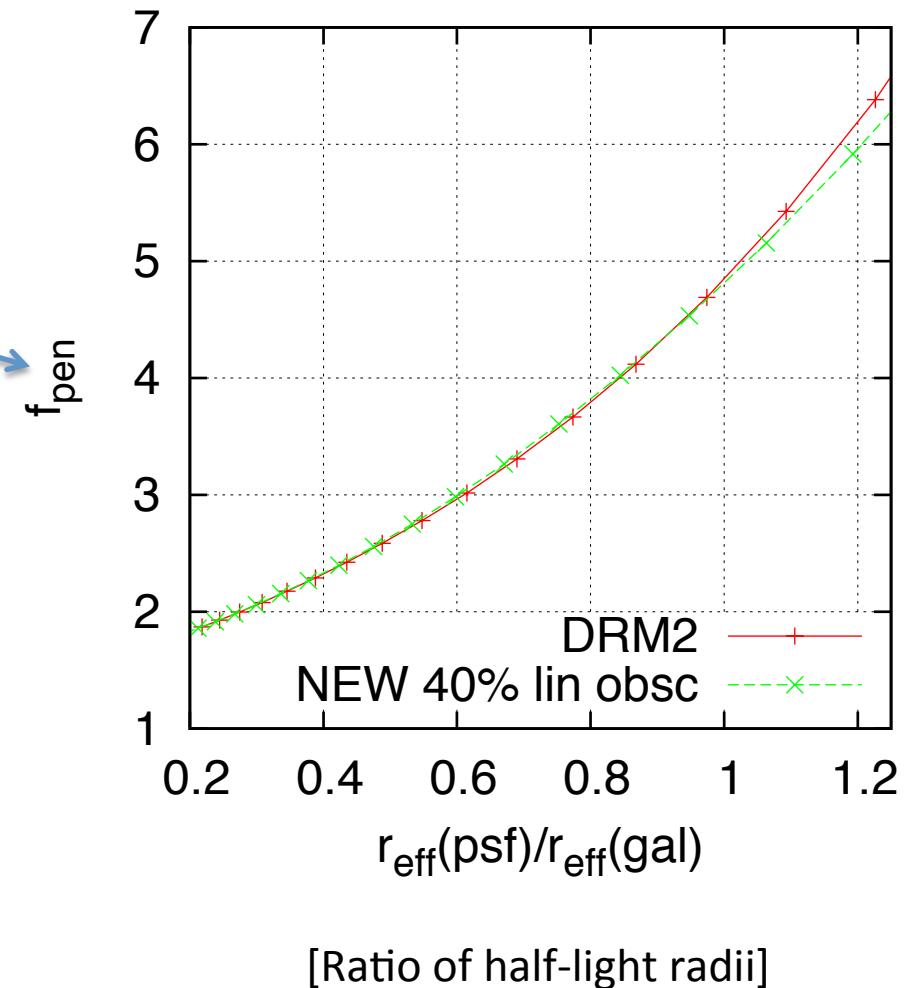
Obstructed PSF on  $\log_{10}$  intensity scale, with 90 nm aberrations; grid is in units of pixels.

# Why the PSF half light radius, $r_{\text{eff}}$ ?

- ✓ WL shape measurement depends on the SNR of a galaxy and a “penalty factor” for PSF smearing and non-Gaussian profile.

$$\sigma_e = \frac{2\sqrt{f_{\text{pen}}}}{\text{SNR}}$$

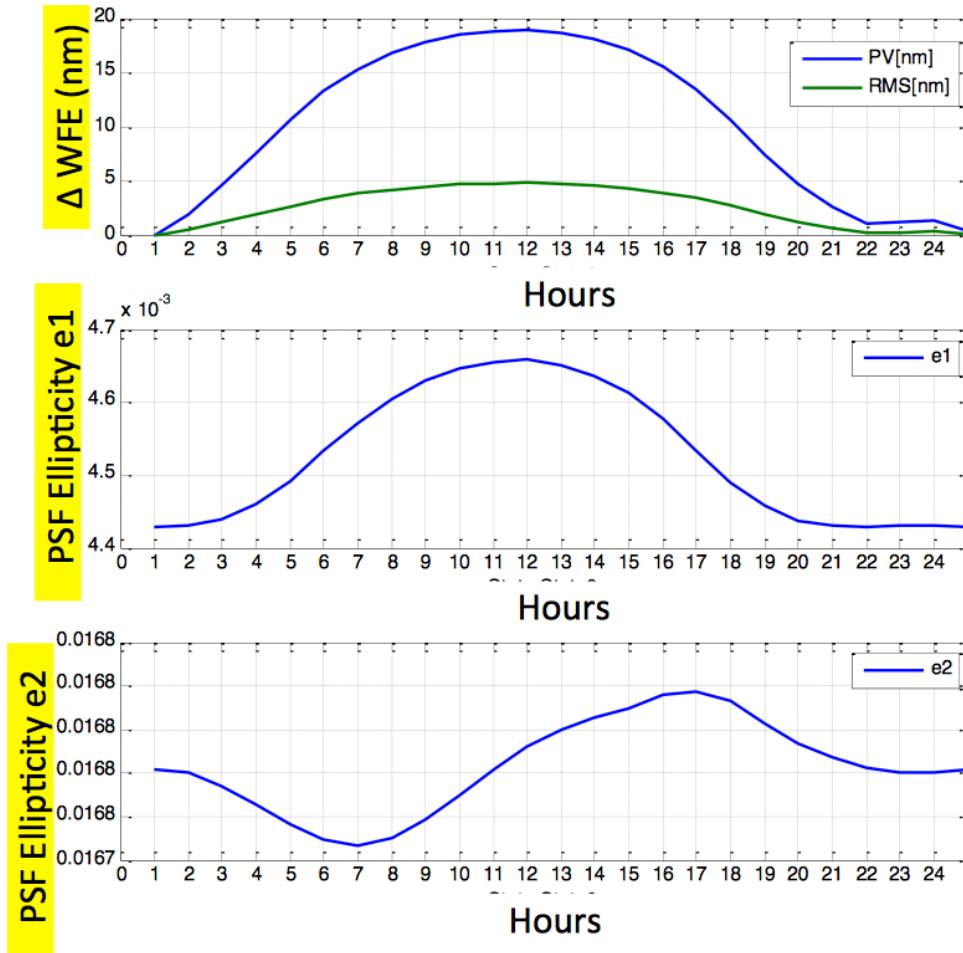
- ✓ The plot on the right shows a comparison of WL shape measurement penalty factor for DRM2 and 2.4 m on-axis (computed by the Fisher matrix integral over spatial frequencies), for an exponential profile galaxy in H band. [NOTE: This comparison is for an old pupil with bigger obstruction – 0% and 40% are bounding cases.]
- ✓ In comparing off- and on-axis telescopes, **scaling by the half-light radius is an excellent indicator of the amount of degradation.**



# WL Summary for Obstructed Telescope

- Obstructed pupil reduces AFTA performance *relative to an off-axis telescope of the same aperture.*
  - Larger PSF (by any metric).
  - Longer exposure times (even the effect of the spider is significant, up to 18% in background limited mode – this is taken into account in the ETC).
- Wavefront stability is essential in any case, and the top Zernike modes are different for the two cases.
  - There is no strong driver to “prefer” one aberration pattern over another – only to make wavefront drift small and confined to a finite set of degrees of freedom.
- Bottom Line: obstructed telescopes are at a disadvantage, but going up to a 2.4 m mirror much more than offsets these losses.
  - The off-axis IDRM was a solution to a problem: improve the PSF without increasing the mirror size. This is no longer the problem at hand.

## WFE and PSF Ellipticity Stability Margins for STOP Fixed-Attitude Case



- $\Delta \text{WFE}$  worst rate 0.041 nm/184s
- $\Delta \text{WFE}$  drift allocation (0.707 nm/184s) easily met at worst rate
- **Margin factor (worst rate) x17**
- PSF Ellipticity =  $\text{sqrt}(\text{rss}(e1, e2)) / \text{sqrt}2$
- Worst rate =  $1.6 \text{ e-}6 / 184 \text{ s}$
- Portion of total PSF Ellipticity Stability Budget ( $\leq 4.7 \text{ e-}4 / 184 \text{ s}$ ) consumed at worst rate is very small!
- **Margin factor (worst rate) = x290**



## Key Cyc-3 STOP Assessments

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- Inclined GEO Orbit introduces variable Earth thermal loads
  - Sensitive to the Observatory's Earth orbit position and attitude.
- Assess impact on the WFI PSF Ellipticity stability margins
  - Evaluate at WFI Imager focal plane
  - Evaluate at a **fixed attitude** with margin on Earth loads on WFI radiator
  - Evaluate for a **worst-slew** with worst case Earth loads on WFI radiator
- For the Coronagraph Team
  - Provide motions and shapes (Zernike's) of the T1 and T2 mirrors as a function of time
  - Provide above for a **fixed attitude** case (at worst angle for Earth thermal disturbances to the Telescope)
  - Slew cases are of much less interest, given the long (2 week?) fixed attitudes expected during CG Operations

## STOP Assessment Summary

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- The STOP results are summarized in detail on p.2
- They show excellent WFI PSF Ellipticity stability and solid WFI WFE stability margins, the best DRM results that we have seen (even for the worst-slew case)
  - x9 margins on WFI WFE drift stability rqt
    - x25 better than HST WFE variations, which can be  $\pm 30$  nm over an orbit
  - x108 margins on WFI PSF Ellipticity total stability rqt
- The T1/T2 Shape/Position Stabilities, from fixed-attitude case, are viewed positively by the Coronagraph Team
  - Zernike instability dominated by focus at a fraction of a nanometer to a few picometers range over 24 hours
  - Sub-micron rigid body motion ranges over 24 hours