

High Contrast Imaging from Space and the WFIRST Coronagraph Instrument

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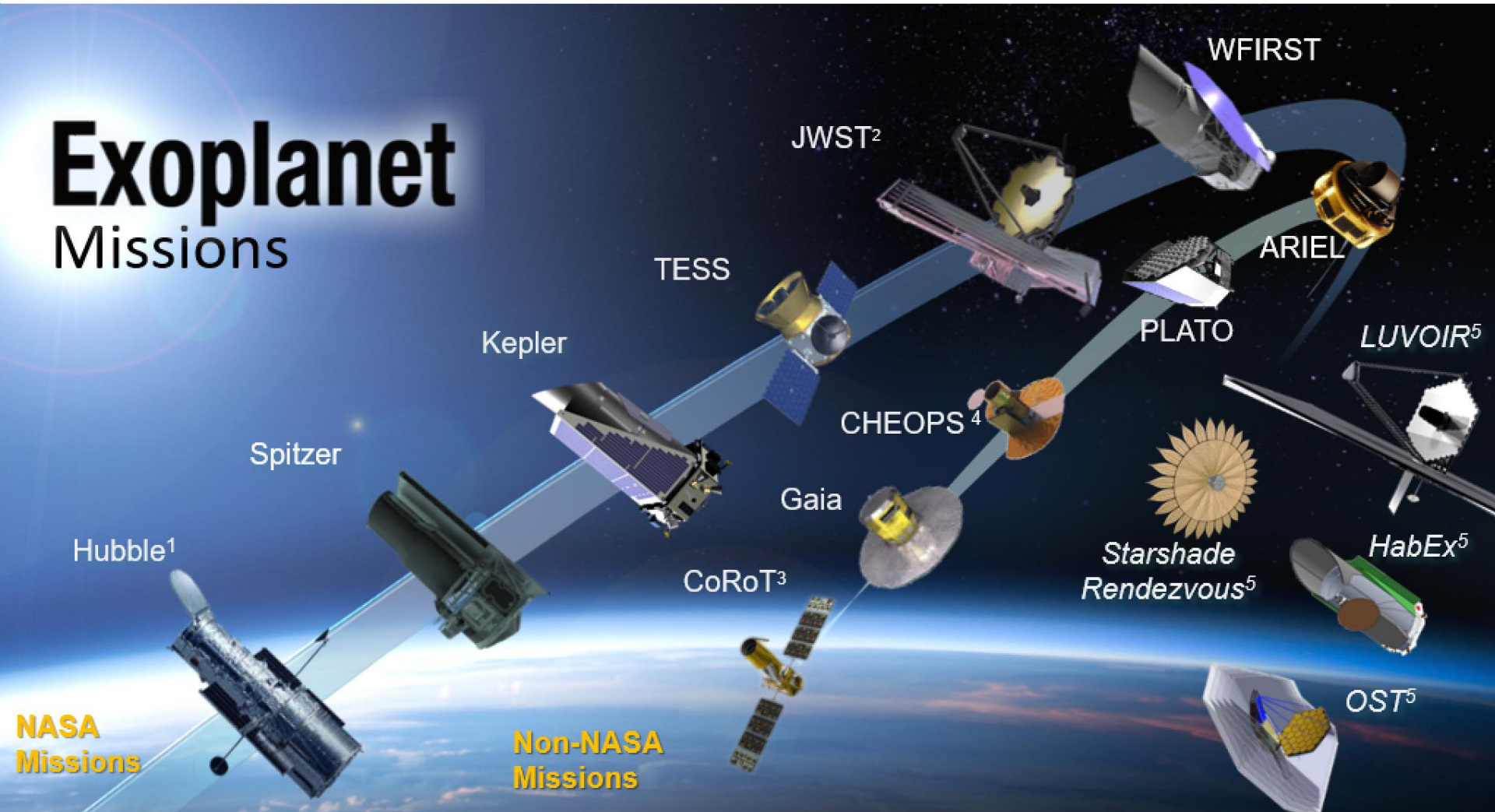
Sara Seager, Andrew Grey, Andrew Romero-Wolf, Doug Lisman, Stuart Shaklan, and the Starshade Rendezvous team.

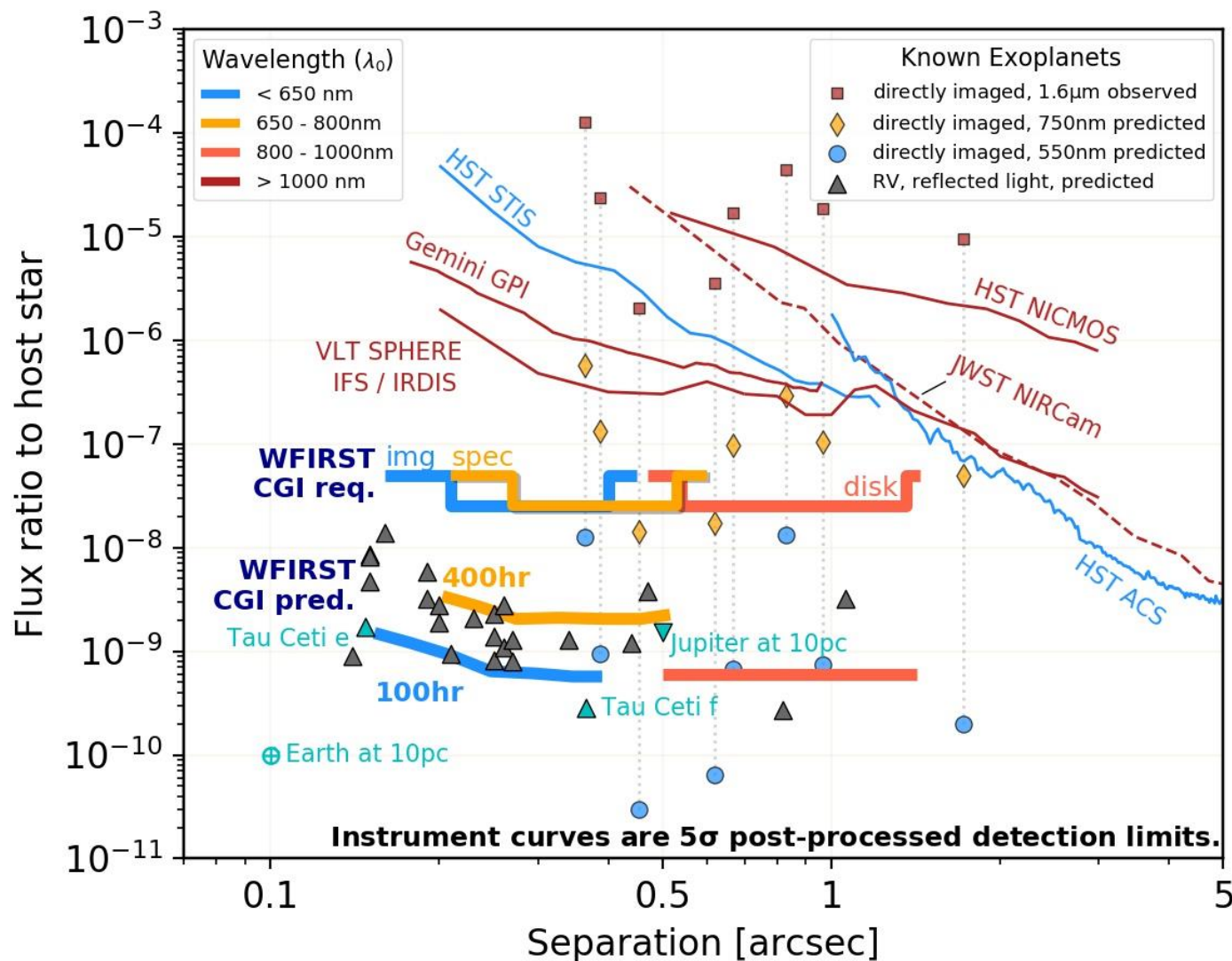
My students and postdocs: Christian Delcroix, Jessica Gersh-Range, Anthony Harness, Leonel Palacios Moreno, Mia Hu, Leonid Pogorelyuki, He Sun.

WFIRST

WIDE-FIELD INFRARED SURVEY TELESCOPE
ASTROPHYSICS • DARK ENERGY • EXOPLANETS

Exoplanet Missions





Giant Planet
Imaging
Photometry

Narrow-band
Spectroscopy of
Self-luminous &
RV Planets

New Planet
Discovery

Exozodiacal Disk
Imaging

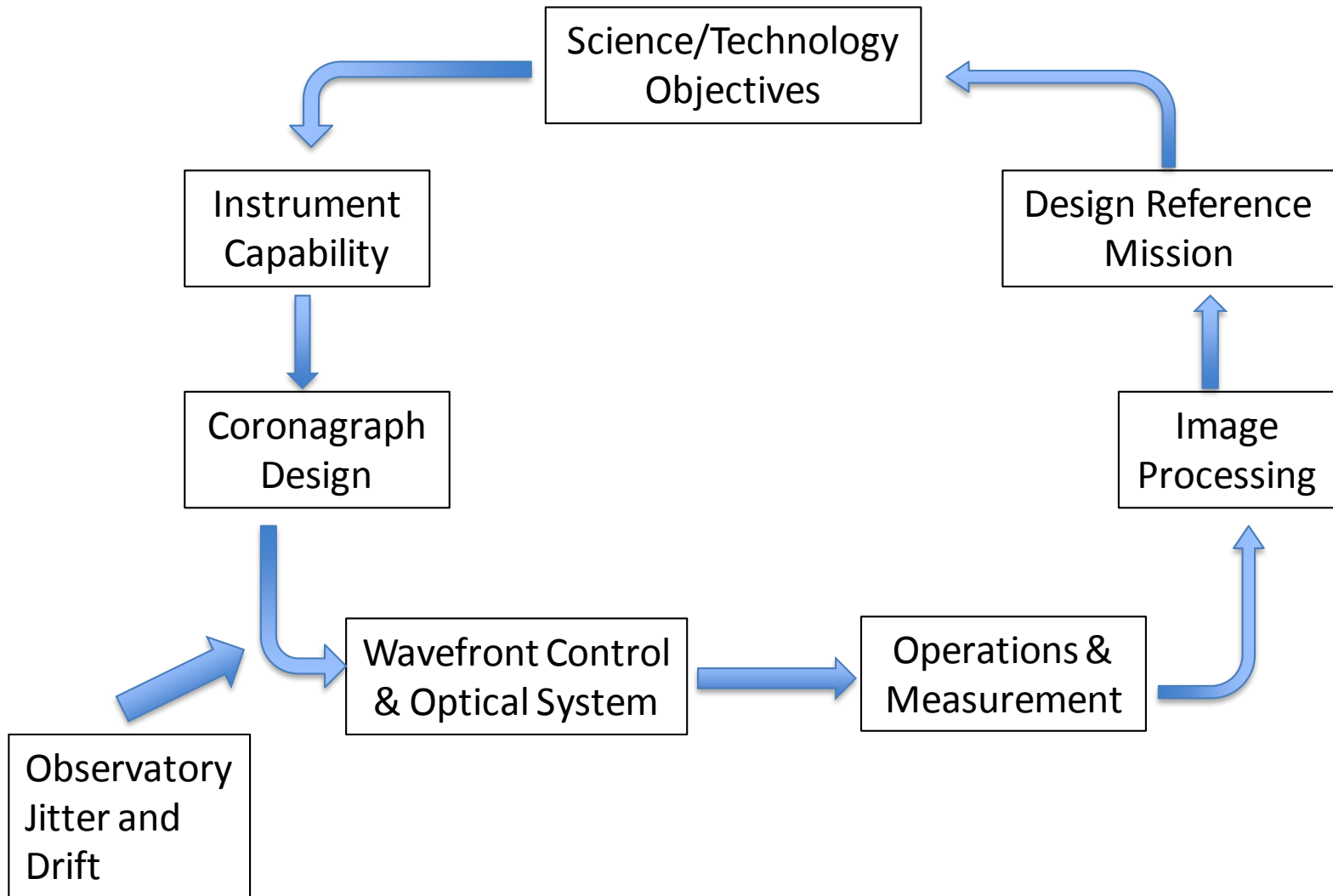
Visible light
characterization
of Debris Disks

- The Coronagraph Instrument is a technology demonstration only
- Requirements established using standard engineering practice
- Reduction in modes and science center role
- If successful, "Participating Science Program" following tech demo
- Design to support possible starshade (pending Decadal recommendation)

Notional CGI Program

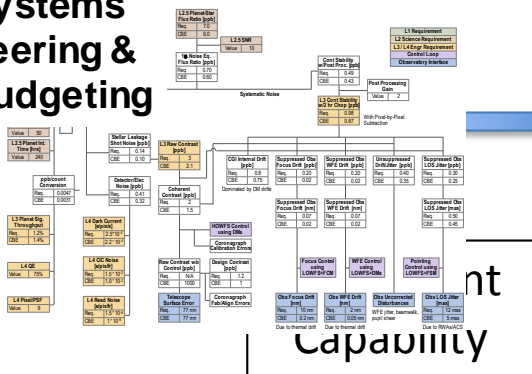
- 3 months of technology demonstration observing in first 1.5 years of WFIRST mission
- If meet success criteria, 1 year Participating Science Program
- If successful, follow-on 2.5 year science program

Realizing a Coronagraph Mission



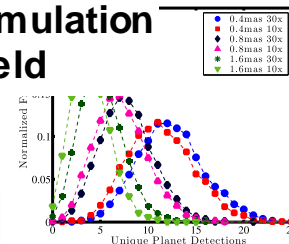
WFIRST as a Pathfinder

Full Systems
Engineering &
Error Budgeting



Science/Technology
Objectives

Mission Simulation
& Yield



Design Reference
Mission

Stable Space
Telescope &
Observatory

High Contrast
Coronagraph
Elements

Image Processing
at Unprecedented
Contrast Levels

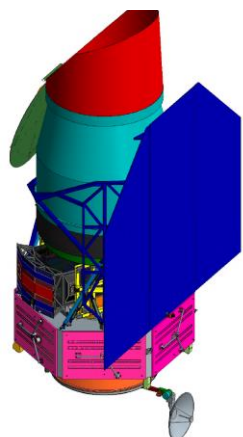
First Use of
Deformable
Mirrors in Space

Wavefront

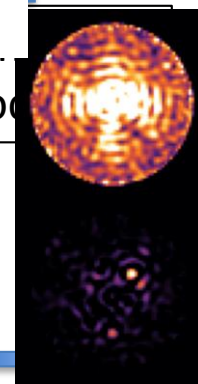
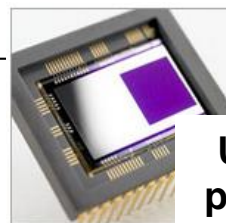
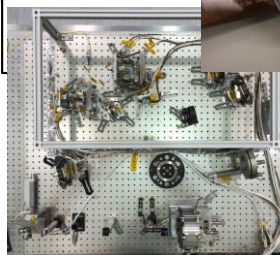
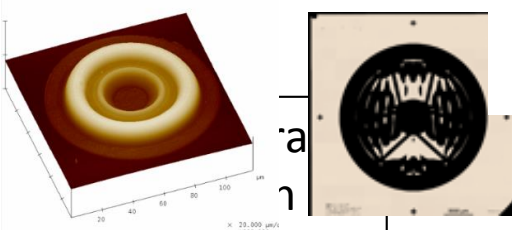
Operations &
Maintenance

Autonomous
Precision
Wavefront
Sensing & Control

Ultra-low noise
photon counting
Visible Detectors



DRIFT



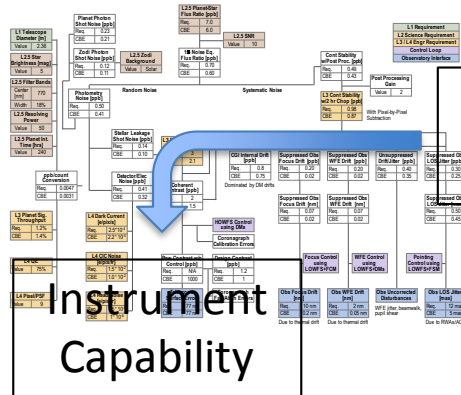
CGI Will

- Demonstrate in space critical coronagraph technology and state of the art wavefront control.
- Advance the state of the art in direct imaging and spectra toward future missions.
- Characterize the in-flight interactions between coronagraph and observatory.
- Prototype systems engineering for space coronagraph.
- Validate end-to-end data analysis for space coronagraph.
- Potentially perform important science in spectral retrieval, direct imaging of RV planets, blind searches, and zodi and debris disk characterization.

Results will inform requirements (particularly stability) and design of future missions such as HabEx and LUVOIR.

Realizing a Coronagraph Mission

Full Systems
Engineering &
Error Budgeting



Science/Technology
Objectives

Instrument
Capability

Coronagraph
Design

Wavefront Control
& Optical System

Operations &
Measurement

Design Reference
Mission

Image
Processing

Observatory
Jitter and
Drift

- **Demonstrate Coronagraphy with Active Wavefront Control in space**
- **Advance Engineering & Readiness of Coronagraph Elements**
- **Development and Demonstration of Advanced Coronagraph Algorithms**
- **Integrated Observatory Performance Characterization**
- **Demonstration of Advanced High-Contrast Data Processing**

In short, WFIRST will validate our models and assumptions for the entire system, including data processing, in a space environment.

CGI Level 2 Requirements

- High-Contrast Direct Imaging
- High-Contrast Imaging Spectroscopy
- Extended Source Imaging with Large FOV
- Polarization Measurements of Disks
- Exoplanet Astrometric Accuracy
- Wavefront Sensing and Control Telemetry
- Telescope Polarization
- Measure Pointing Jitter
- Measure Slow Wavefront Aberrations

1) High-Contrast Direct Imaging

WFIRST CGI shall be able to measure the brightness of an astrophysical point source to an SNR of 10 or greater within 10 hours of integration time on the target in CGI Filter Band 1 for an object with a source-to-star flux ratio as faint as $1e-7$ at separations from 0.16 arcsec to 0.21 arcsec, $5e-8$ at separations from 0.21 arcsec to 0.4 arcsec, and $1e-7$ at separations from 0.4 arcsec to 0.45 arcsec.

2) High-Contrast Imaging Spectroscopy

WFIRST CGI shall be able to measure spectra of an astrophysical point source with $R = 50$ or greater spectral resolution with a wavelength accuracy of 5 nm or smaller (TBR) to an SNR of 10 within 100 hours of integration time on the target in CGI Filter Band 3 for an object with a source-to-star flux ratio as faint as $1e-7$ at separations from 0.21 arcsec to 0.27 arcsec, $5e-8$ at separations from 0.27 arcsec to 0.53 arcsec, and $1e-7$ at separations from 0.53 arcsec to 0.60 arcsec.

*Level 2 requirements specify **system level performance** independent of instrument design.*

- Direct Imaging
- Spectroscopy
- Extended Sources
- Polarization Measurements
- Astrometry
- Telemetry
- Polarization errors
- Pointing Jitter

Level 2 Technology Requirements

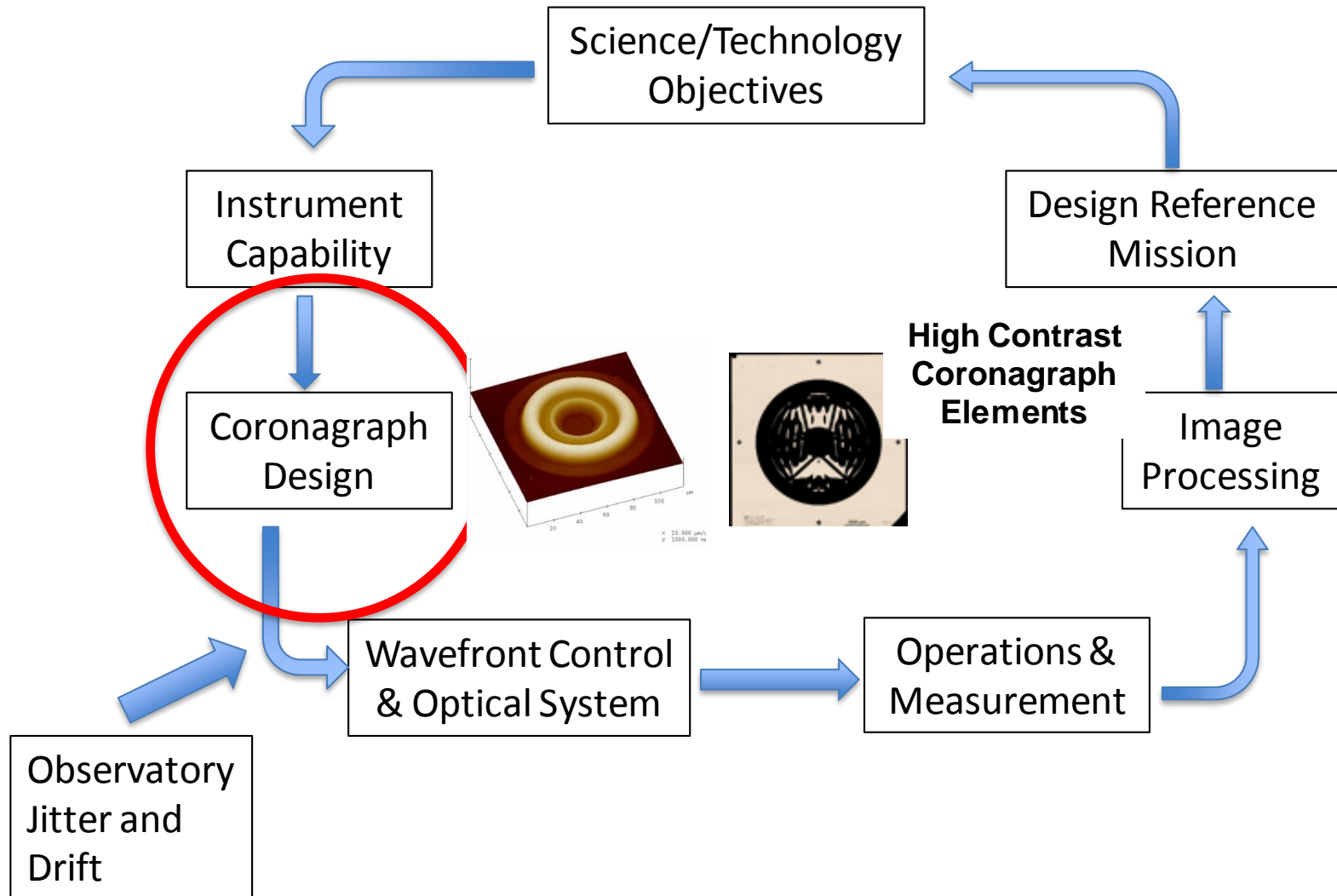
WFIRST is pioneering the entire systems engineering process.



Level 3/4 Requirements

- Instrument Contrast
- Stability
- Pointing
- Throughput
- Polarization
- Detector
- Post-Processing
- Operations

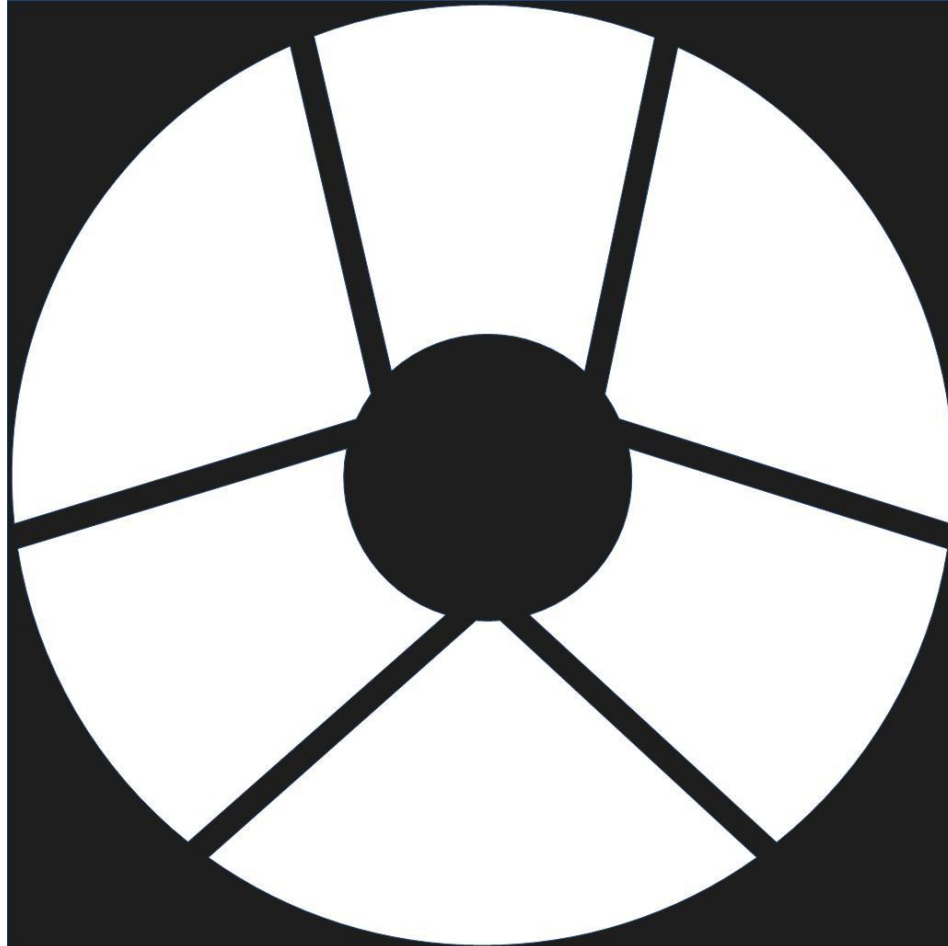
Coronagraph Design



Coronagraph Metrics

- **Contrast:** The ratio of the peak of the stellar point spread function to the halo at the planet location.
- **Inner Working Angle:** The smallest angle on the sky at which the needed contrast is achieved and the planet is reduced by no more than 50% relative to other angles.
- **Throughput:** The ratio of the open telescope area remaining after high-contrast is achieved.
- **Bandwidth:** The wavelengths at which high contrast is achieved.
- **Sensitivity:** The degree to which contrast is degraded in the presence of aberrations.

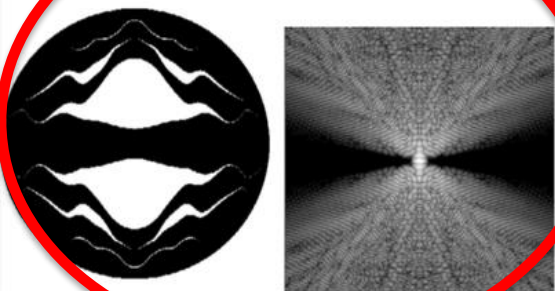
Coronagraph performance also differs depending upon aperture. All previous coronagraphs were for open apertures (off-axis telescopes).



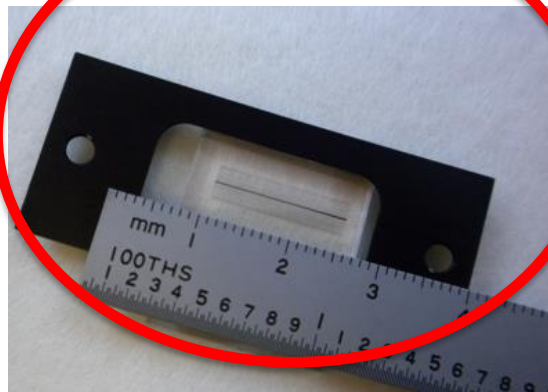
Highest
Instrument
Risk is a
Change to the
Pupil.

Coronagraph Selection

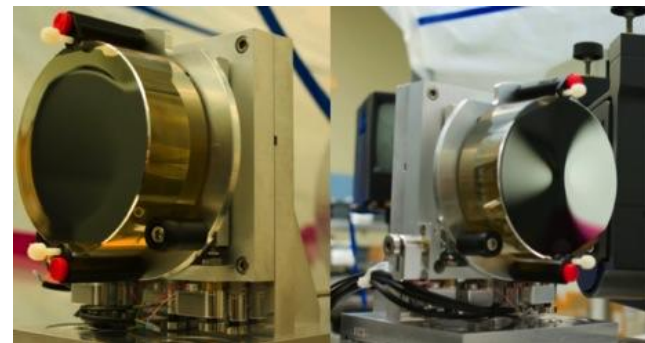
SPC



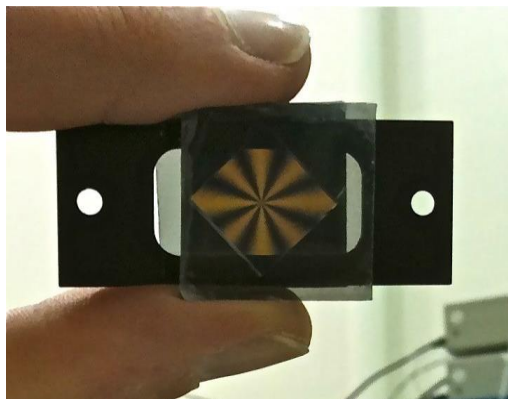
HLC



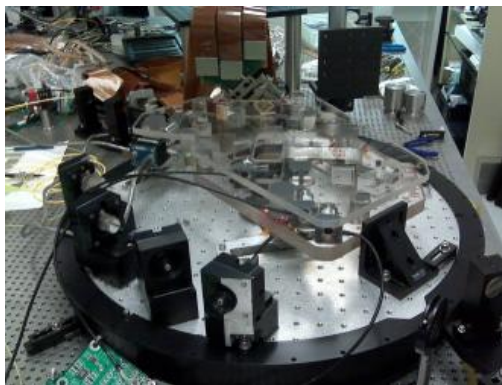
PIAA-CMC



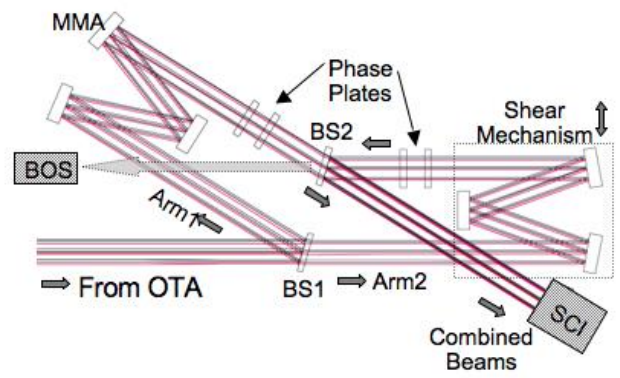
VVC



VNC-Davinci

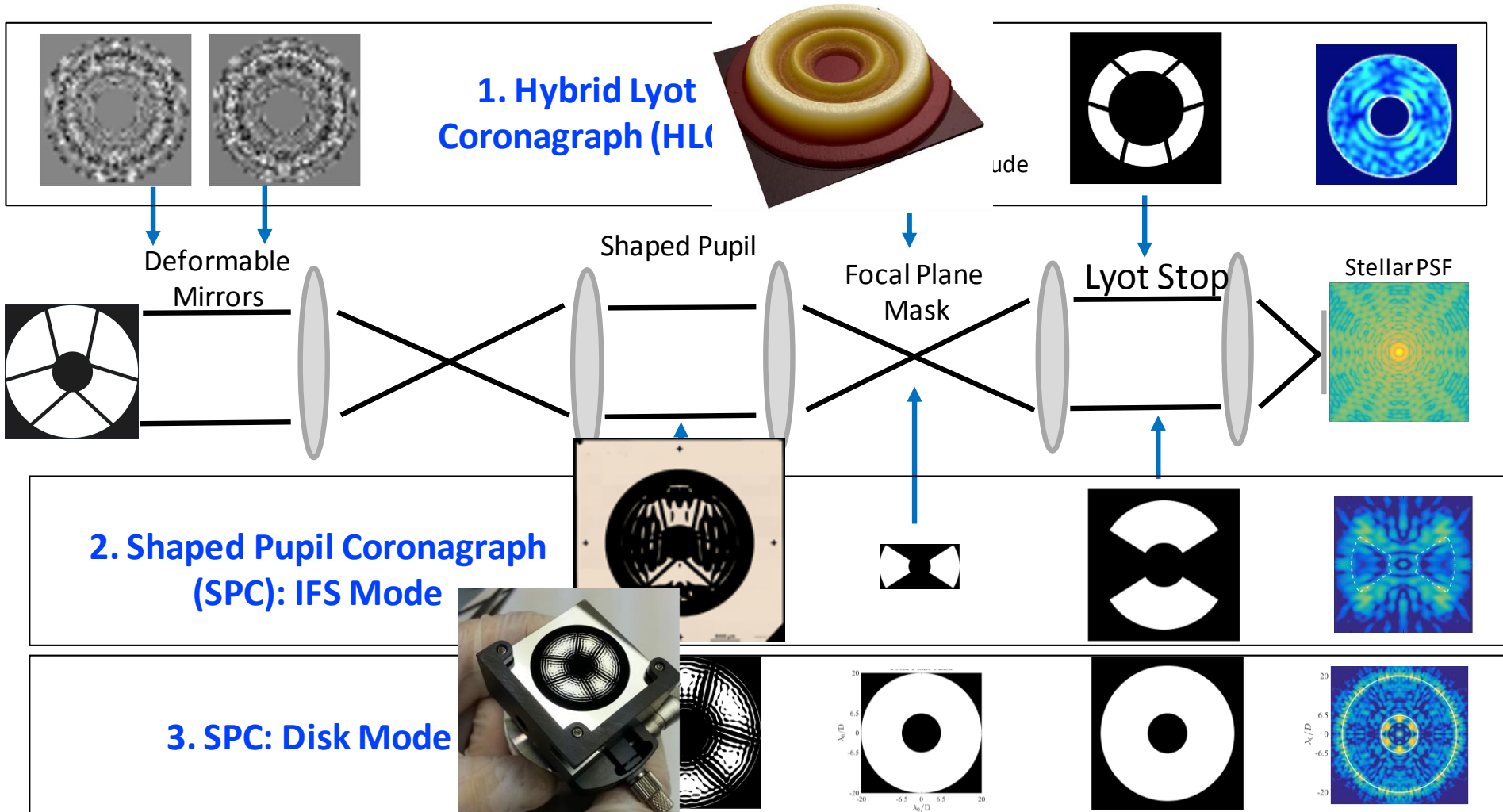


VNC-PO



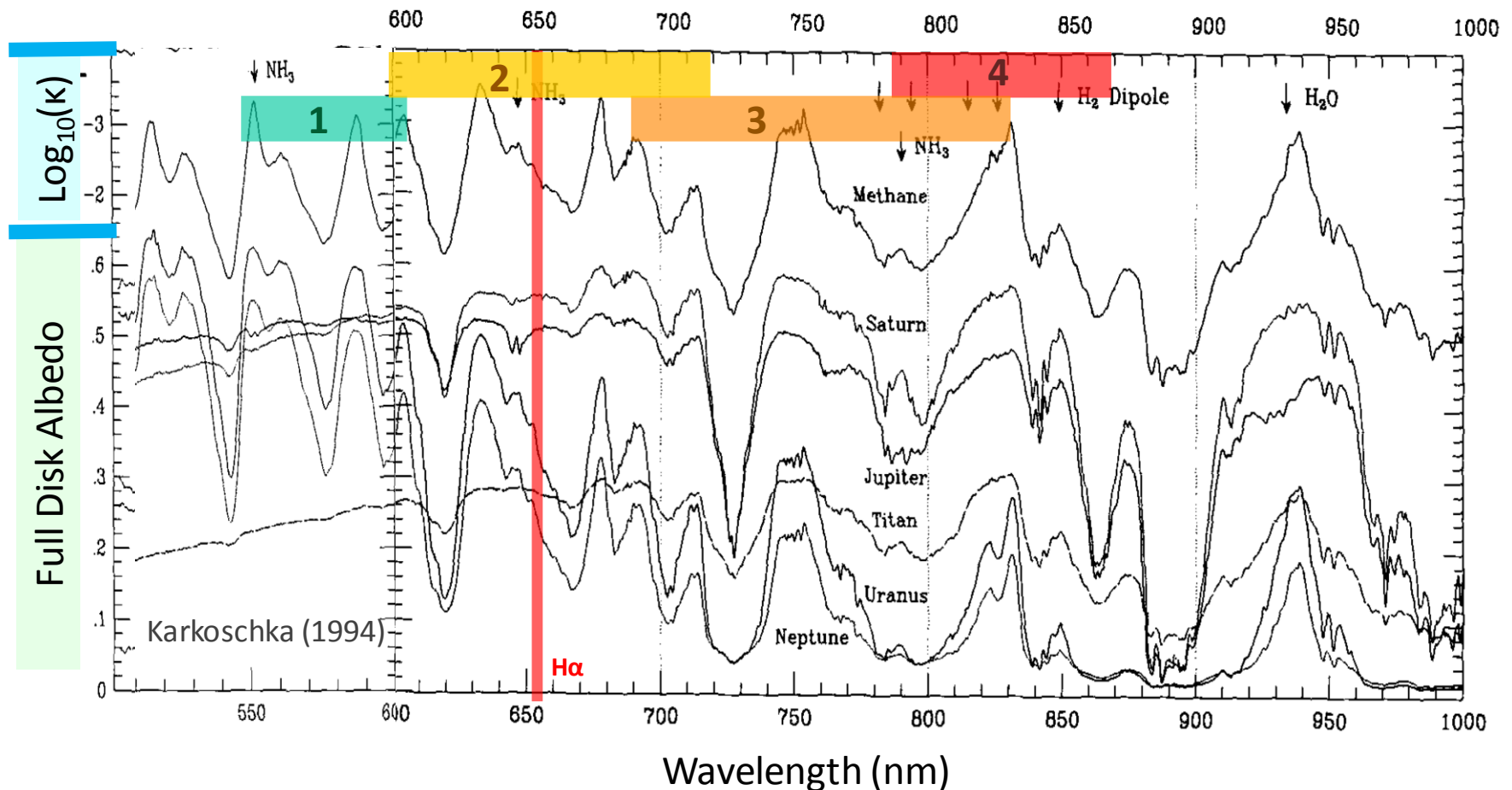
- Three interchangeable coronagraph observing modes via mask selection mechanisms

Courtesy AJ Riggs.



Filters and Modes

3 Tested Modes: 575nm HLC Imaging (10%), 760 nm SPC IFS (18%, R50), 825 SPC Disk Imaging (10%)



Hybridization

WFIRST design jump-started the trend toward hybridizing, or combining, different coronagraph features.

Modern design efforts now incorporate DMs, apodizers, focal plane masks, and Lyot Stops into the design process. Resulting optimization is challenging. (ACAD, HLC, Ring Vortex, SPLC)

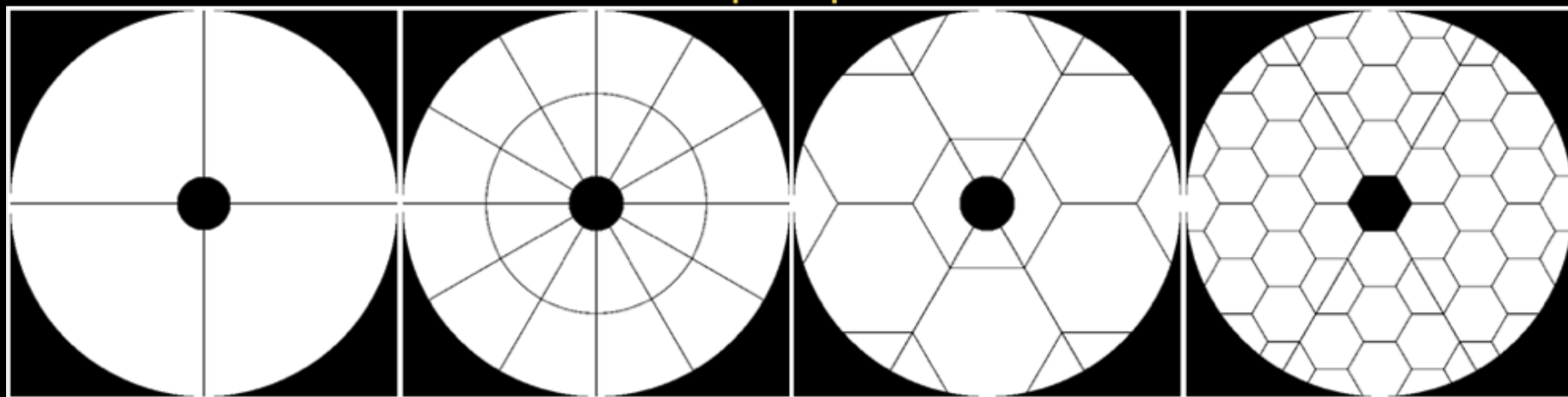
As a result, it has become possible to consider coronagraphs for on-axis and segmented telescopes. This has been enabling for large mission concepts such as HabEX and LUVOIR.

SCDA—Segmented Coronagraph Design & Analysis

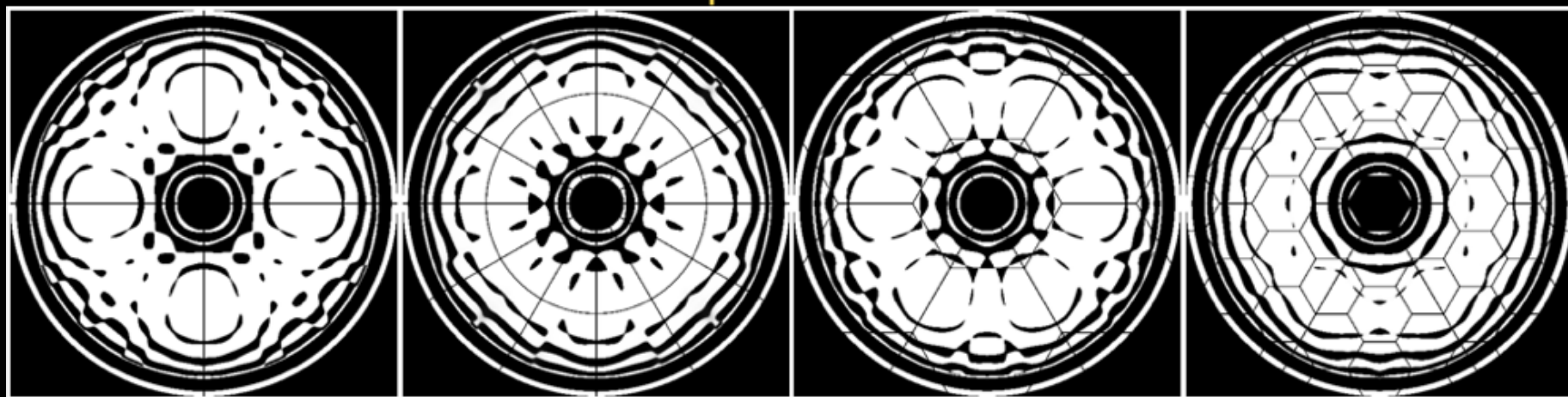
Apodized/Shaped Pupil Lyot Coronagraph

Courtesy Neil Zimmerman

Telescope apertures



Apodizers

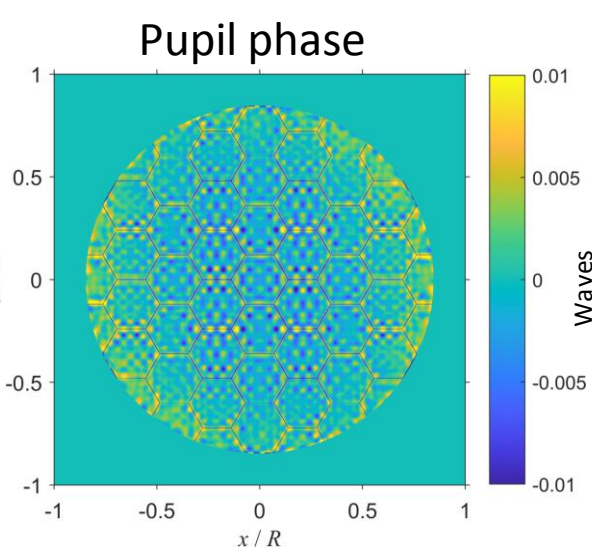
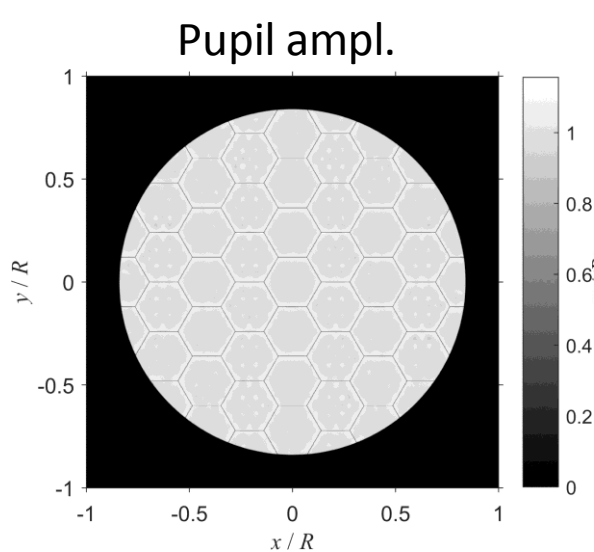
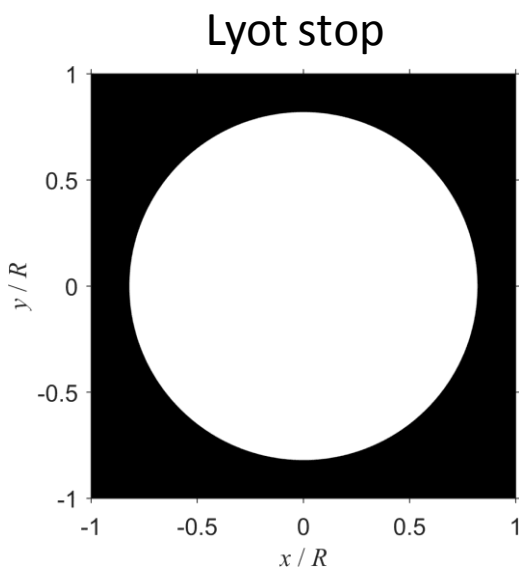
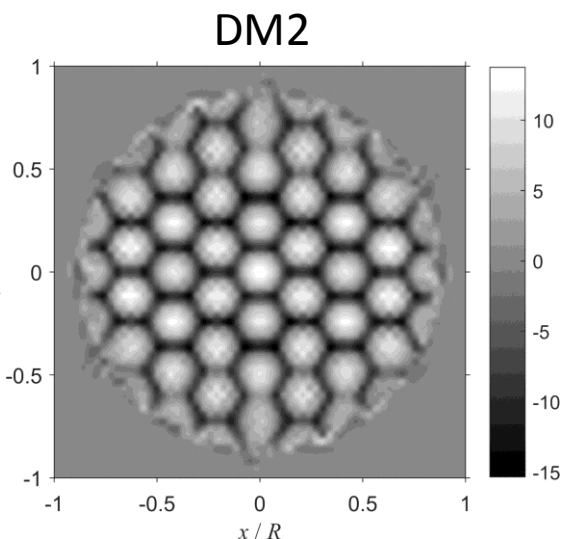
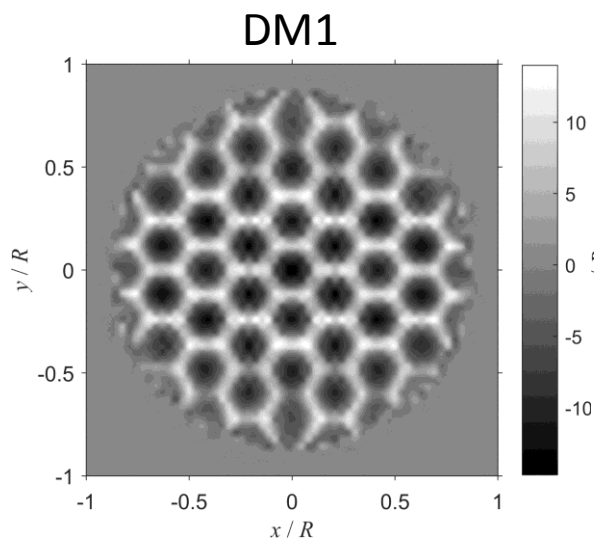
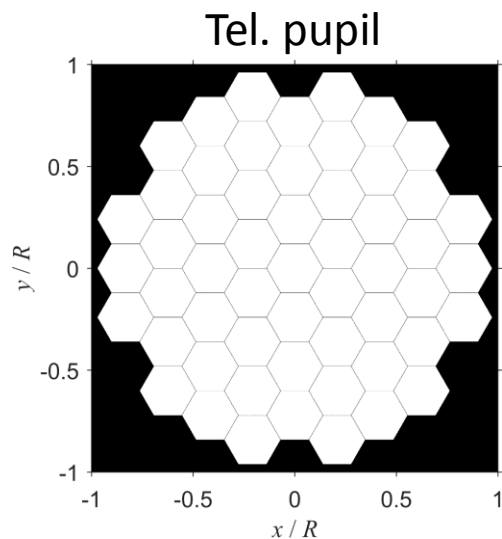


$$T_{0.7/circ} = 23.6\%$$

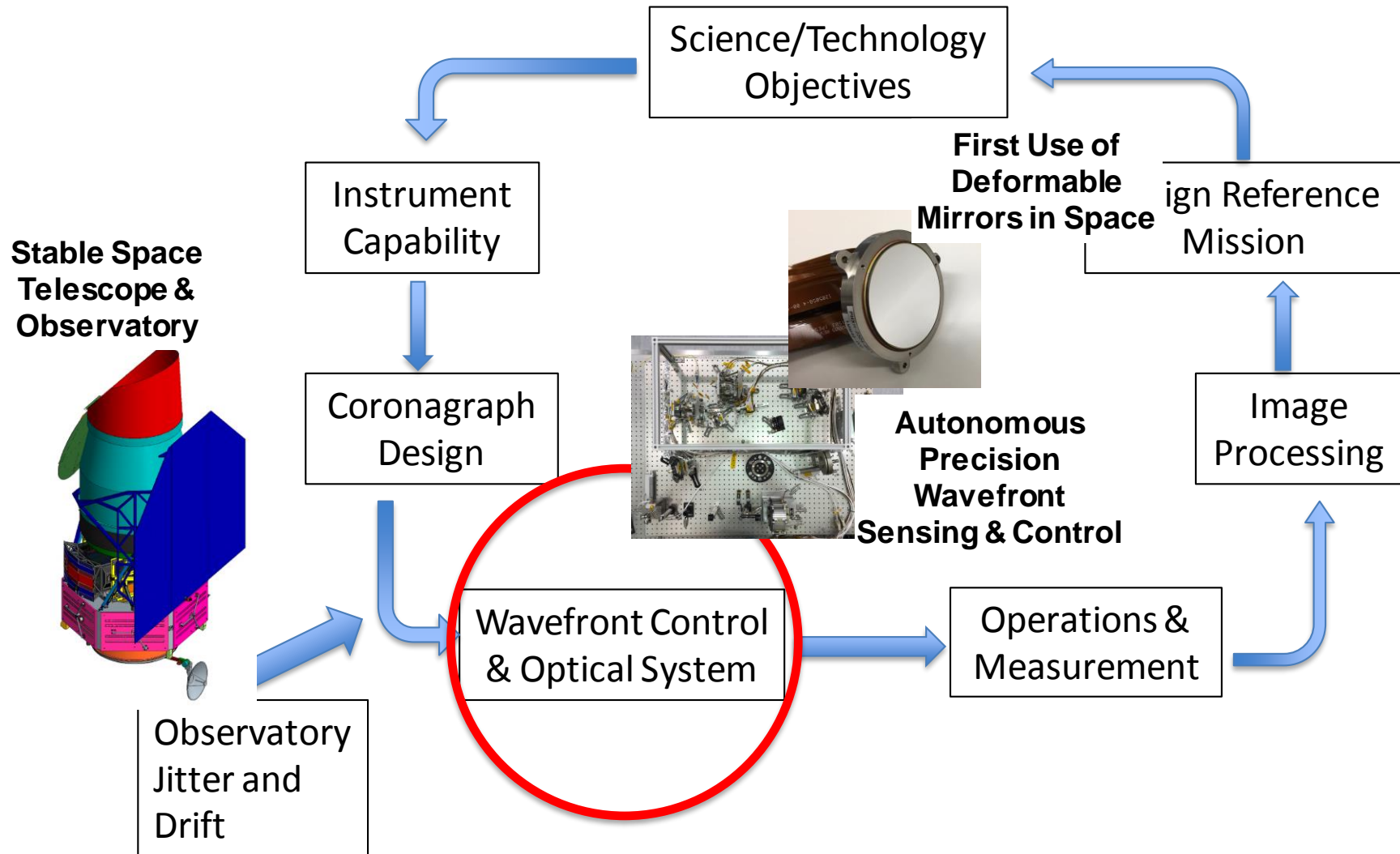
$$T_{0.7/circ} = 21.8\%$$

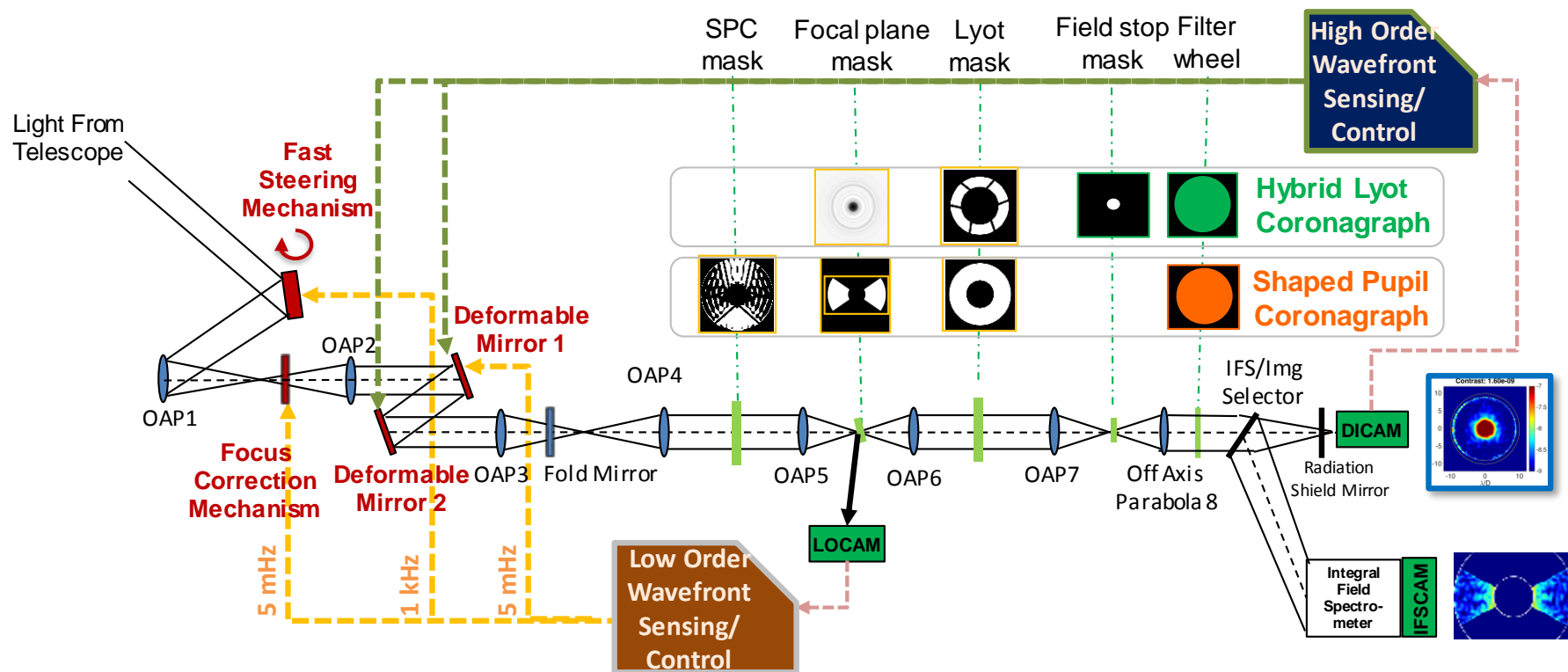
$$T_{0.7/circ} = 23.6\%$$

$$T_{0.7/circ} = 22.0\%$$



Coronagraph Design

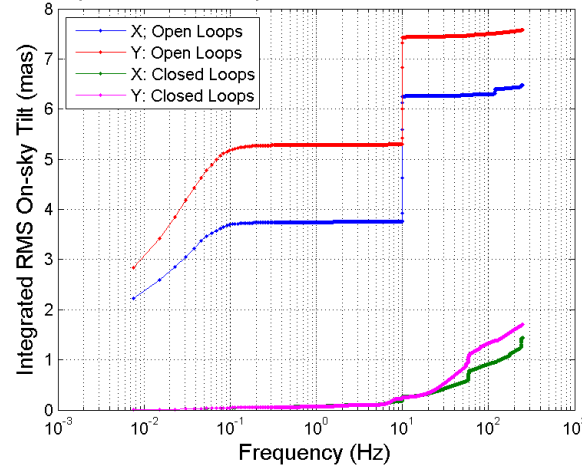
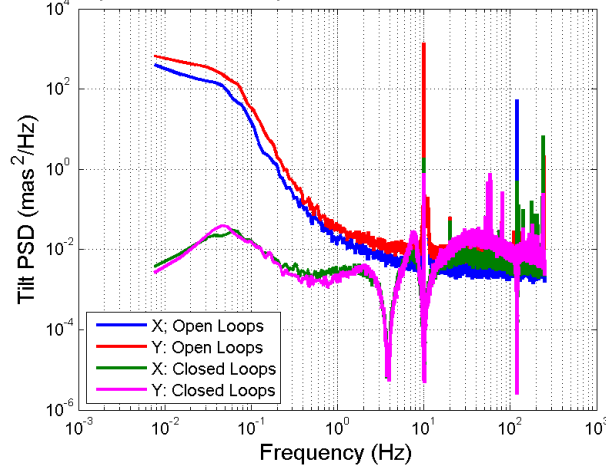




WFIRST will pioneer space based active wavefront control with both high-order (slow) and low-order (fast) correction and large format DMs. **DMs 2nd Highest Risk.**

Line-of-Sight Control

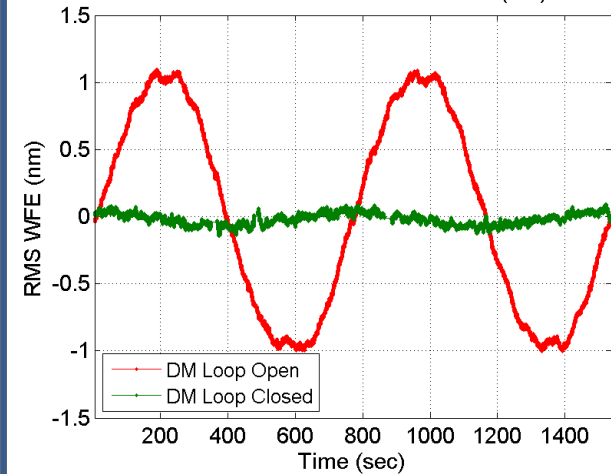
SPC Open & Closed Loops w/ OTA Disturbances: 2017-01-2 SPC Open & Closed Loops w/ OTA Disturbances: 2017-01-



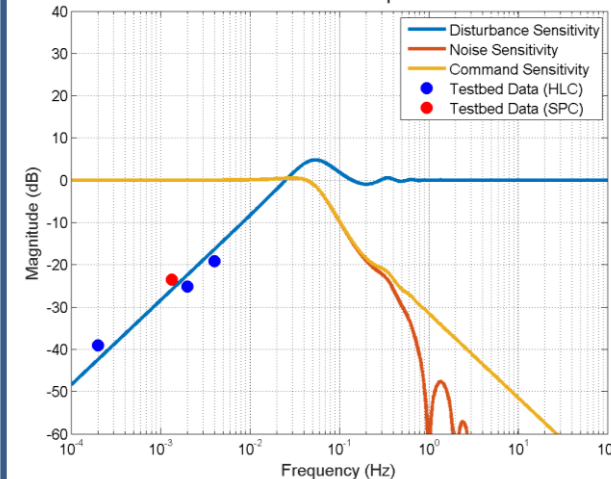
Corrects Tip/Tilt, Focus and lower order Zernike errors from telescope interface on fast timescales.

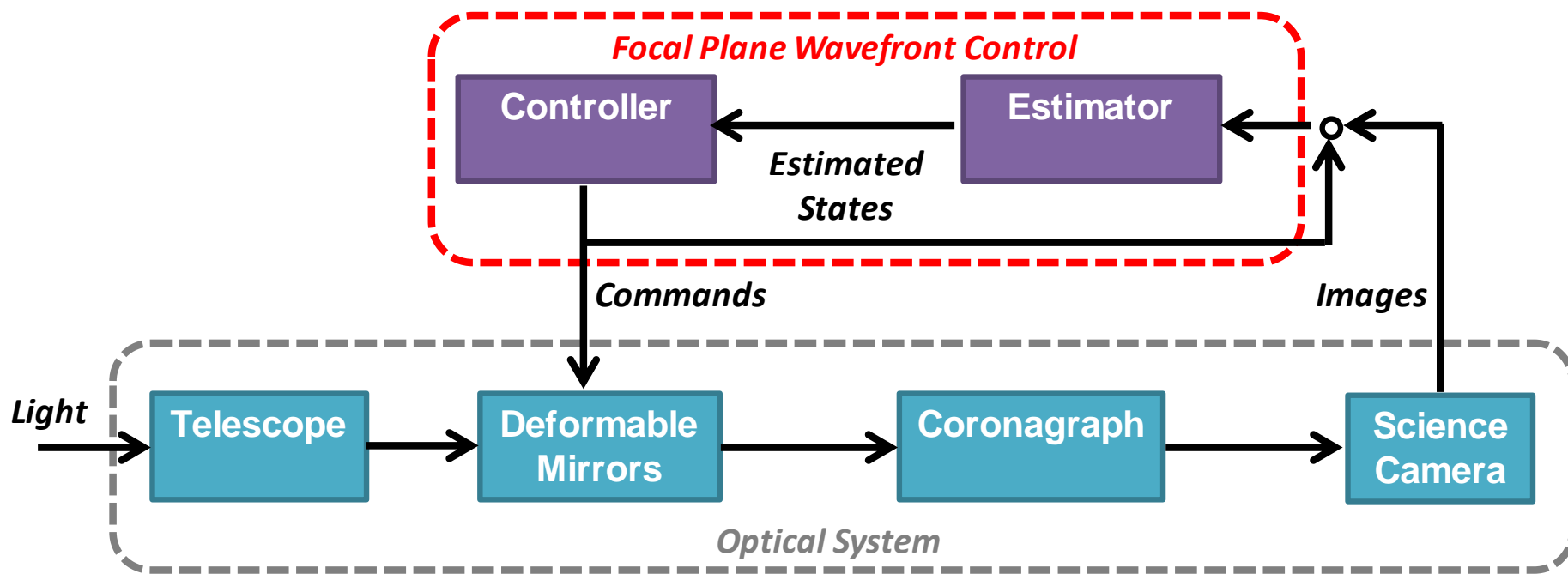
Focus Control

SPC LOWFS Sensed Focus (Z4)



Testbed Focus Correction Loop Model and Data





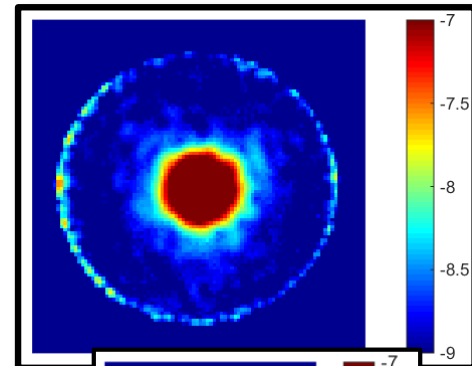
Corrects quasi-static aberrations at high spatial frequencies to create “dark hole”. Aberration changes assumed slow compared to correction and observation times. Source of stability requirement on future telescopes (currently assumed at 10-100 pm rms).

HOWFS Performance

Imaging with Narrow FoV Initial Static Raw Contrast

	Initial contrast vs. working angle		
Working angle	3-4 λ/D	4-8 λ/D	8-9 λ/D
Band 1 (575 nm)	1×10^{-8}	0.7×10^{-8}	1×10^{-8}

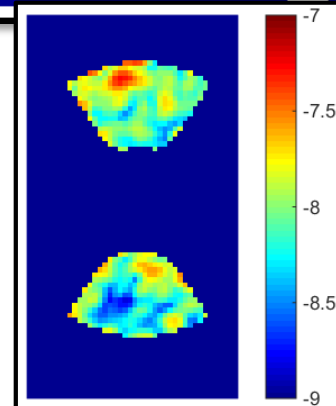
Best testbed
result: 1.6×10^{-9} in
10% at 550nm



Spectroscopy Initial Static Raw Contrast

	Initial contrast vs. working angle		
Working angle	3-4 λ/D	4-8 λ/D	8-9 λ/D
Band 3 (760 nm)	2×10^{-8}	1.5×10^{-8}	2×10^{-8}

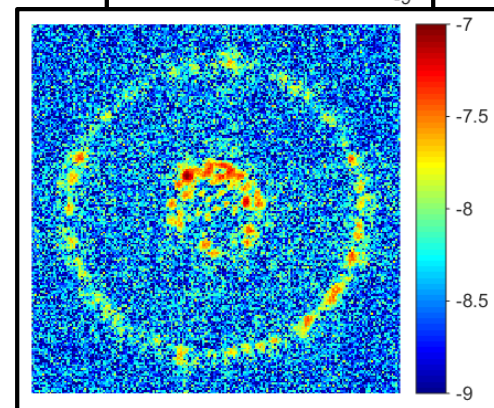
Best testbed
result: 1.1×10^{-8} in
18% at 660nm



Imaging with Wide FoV Initial Static Raw Contrast

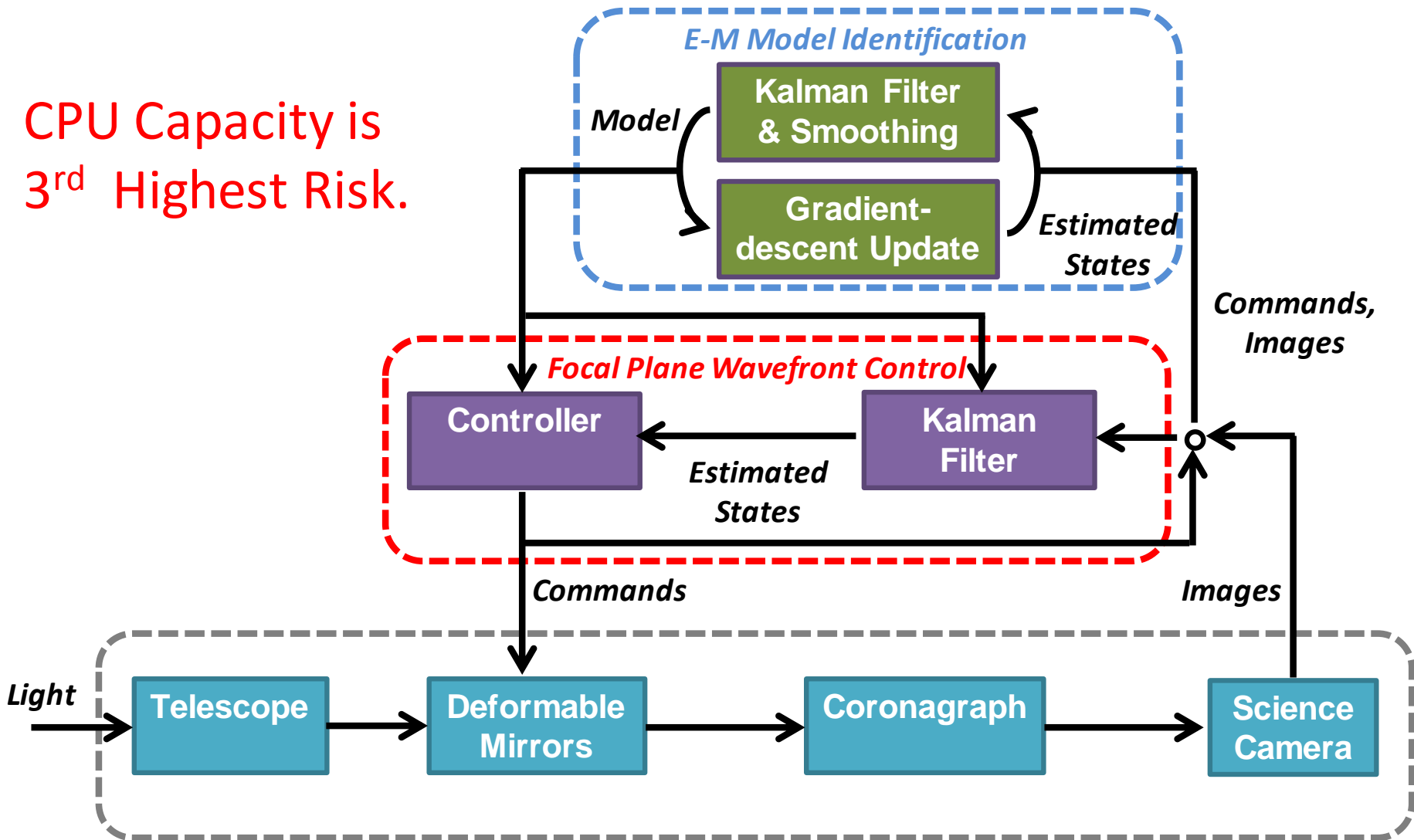
	Initial contrast vs. working angle		
Working angle	6.5-7.5 λ/D	7.5-19 λ/D	19-20 λ/D
Band 4 (825nm)	2×10^{-8}	1.5×10^{-8}	2×10^{-8}

Best testbed
result: 4.3×10^{-9} in
10% at 565nm

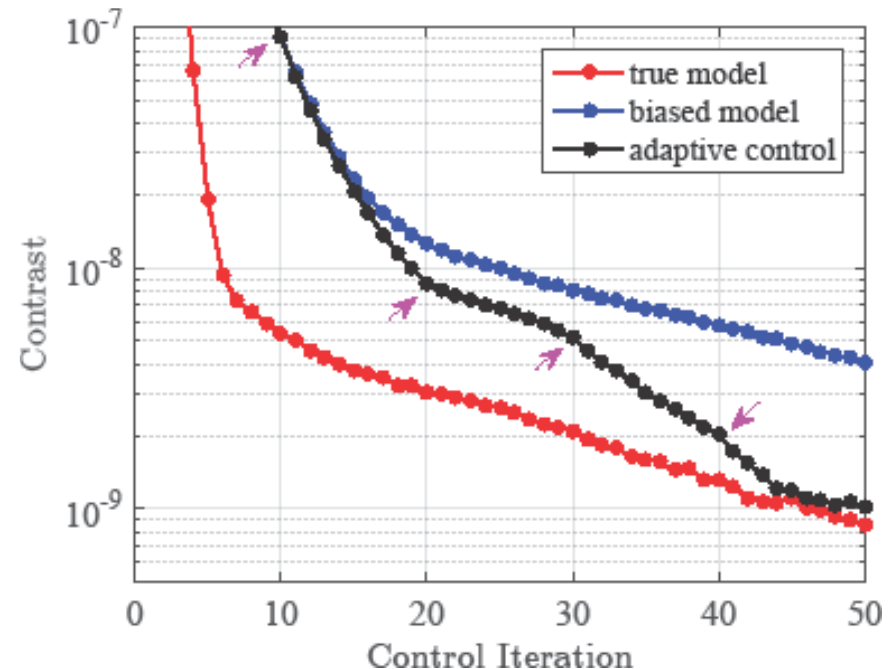
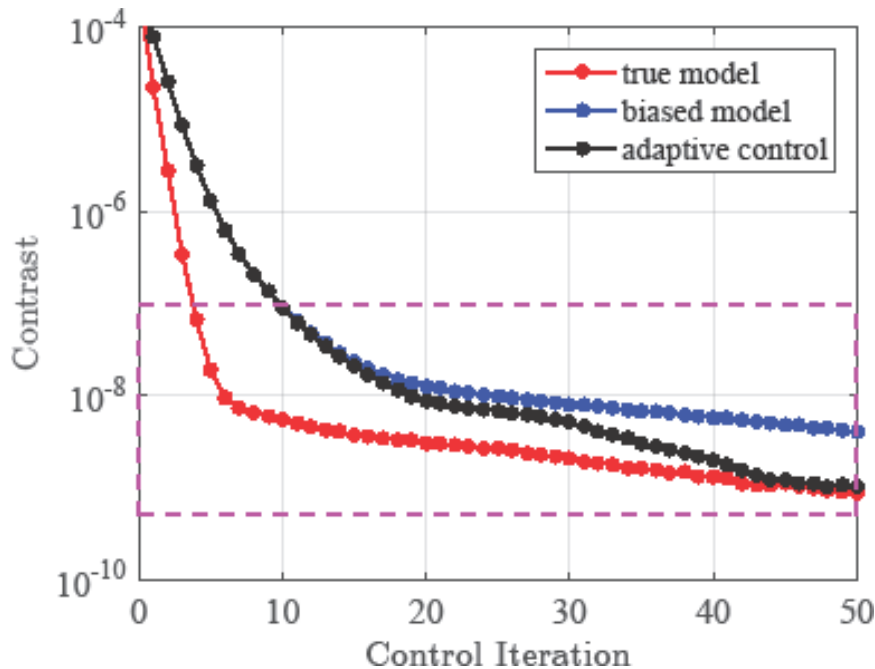


Adaptive High-Order Wavefront Control

CPU Capacity is
3rd Highest Risk.

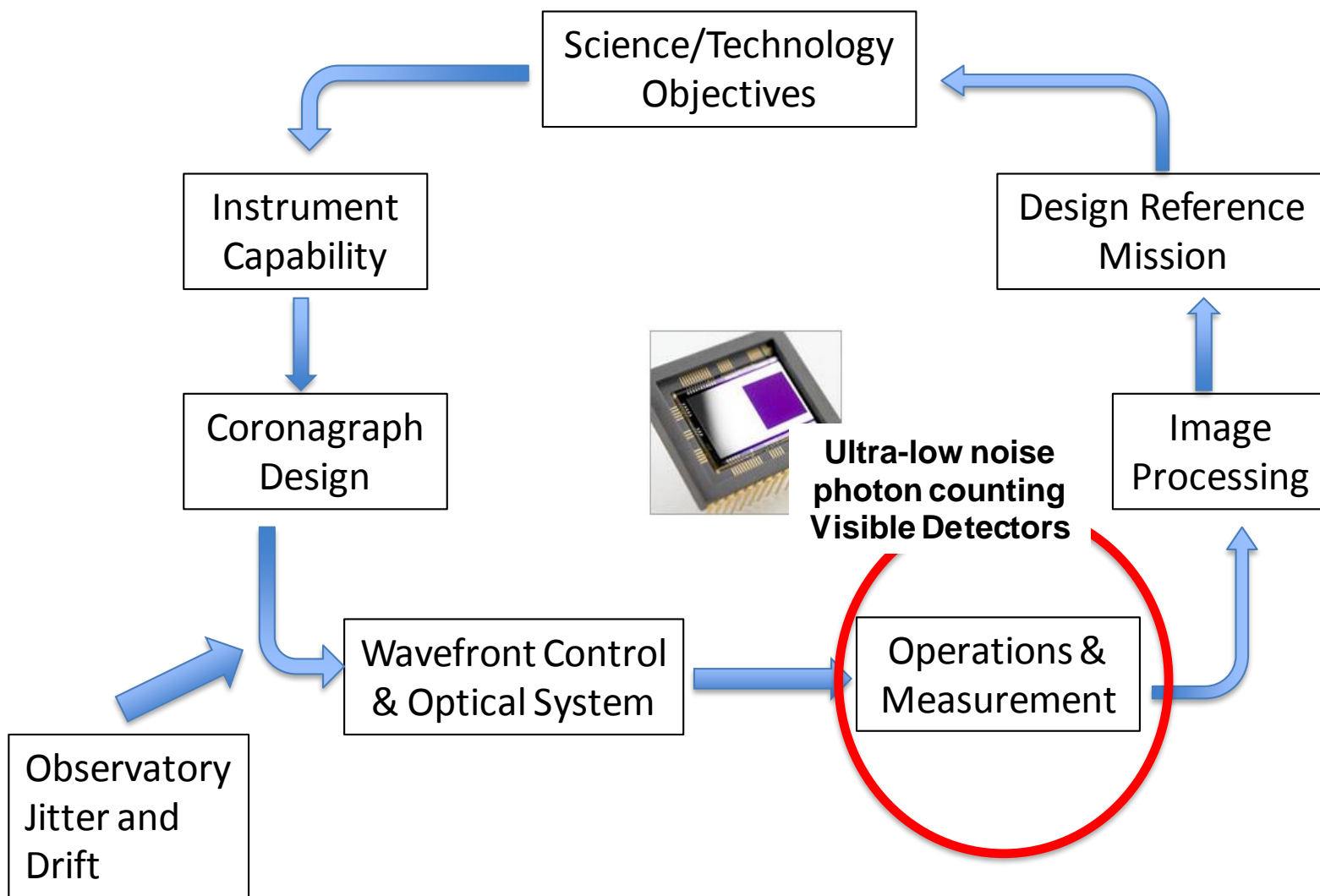


Simulation Results

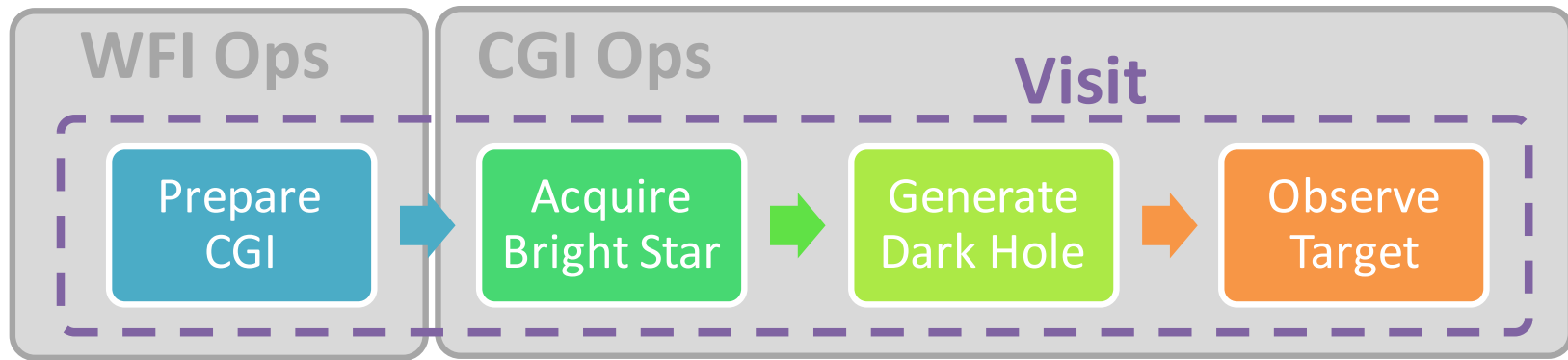


- The DM actuators' influence functions are biased by 20% in amplitude; optical aberrations are added to the shaped pupil plane and DM planes;
- Three test cases: true model control, biased model control, and adaptive control with biased model;
- Adapt the model after every ten iterations;

Coronagraph Design



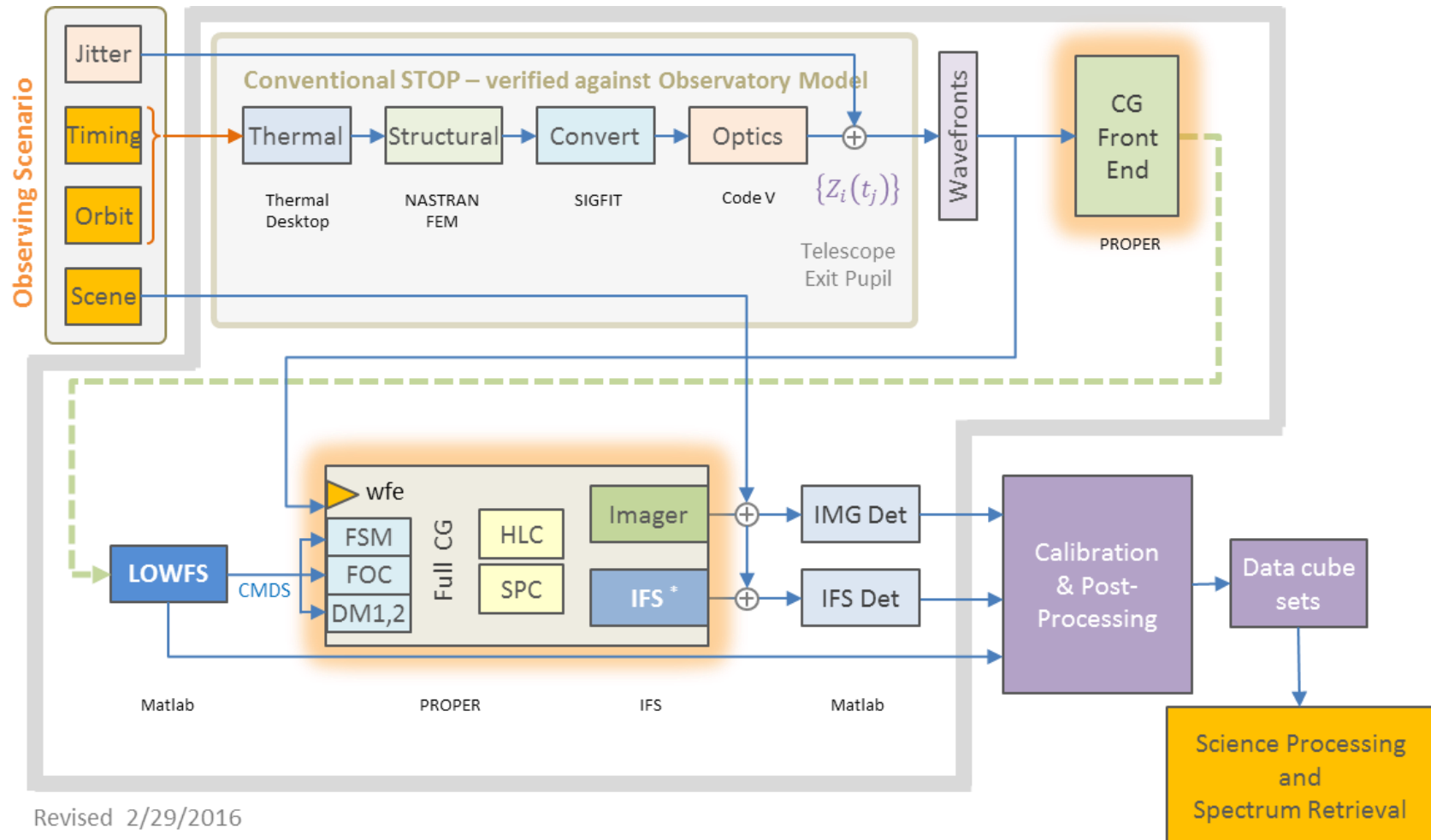
Single Observation



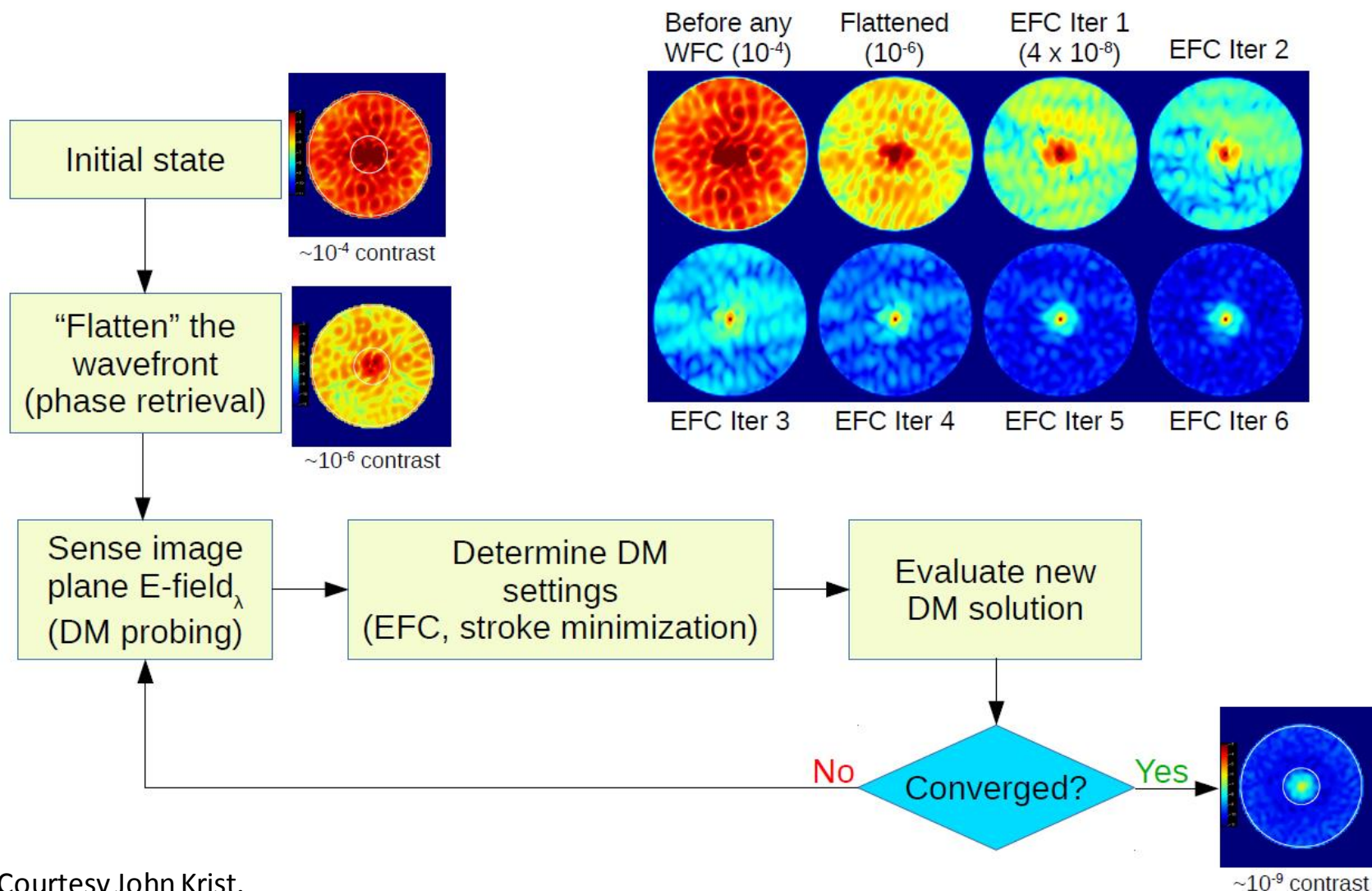
Simple single visit scenario: generate dark hole on a bright reference star, slew to target star, assume residual speckles unchanged and stable on time scale to observe target.

Integrated Modeling of Spacecraft and Coronagraph inform model for speckle level, stability, and noises.

Integrated Modeling



Integrated Modeling



Courtesy John Krist.

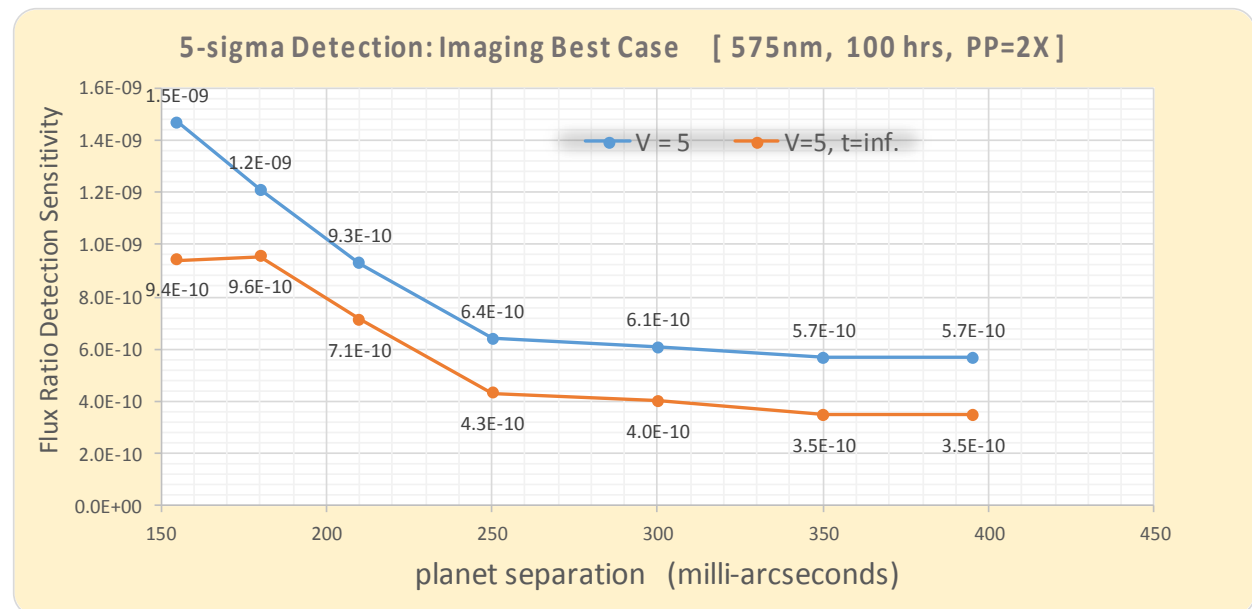
Integration Time Calculator

Models for camera noise, shot noise, and speckle stability used to calculate “detection threshold” and integration times.

What is the minimum flux ratio planet we can see with a specified SNR in the allocated integration time?

Integration time calculator was developed by Bijan Nemati for WFIRST.

See backup for information on EMCCD camera and degradation.



Courtesy Bijan Nemati

Ex.: Direct Imaging

WFIRST Exoplanet Yield Among Known Planets:

Imaging Best Case

viewed: 3/8/2018

Imaging Best Case

RDI : Dmag = 3.0

20% time on Reference, Mult= 1.3

18

Planets

Mode	CG	I , nm	DI , nm	SNR	f_pp	Mission Life	time, hrs
Imaging Best Case	HLC CG TDemo	575	57.5	5	50%	35%	100

set:

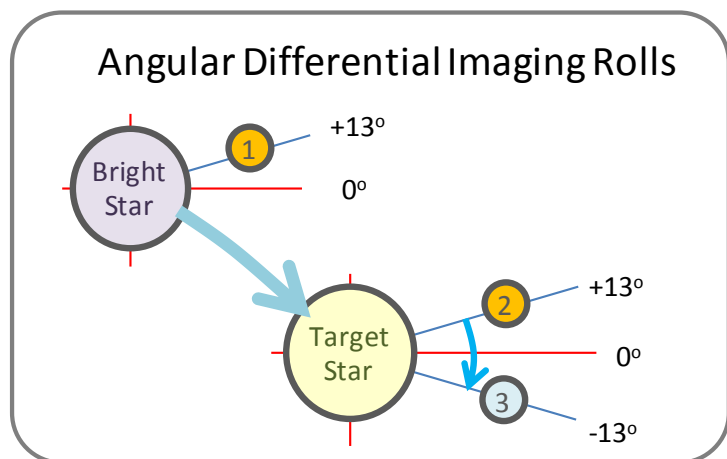
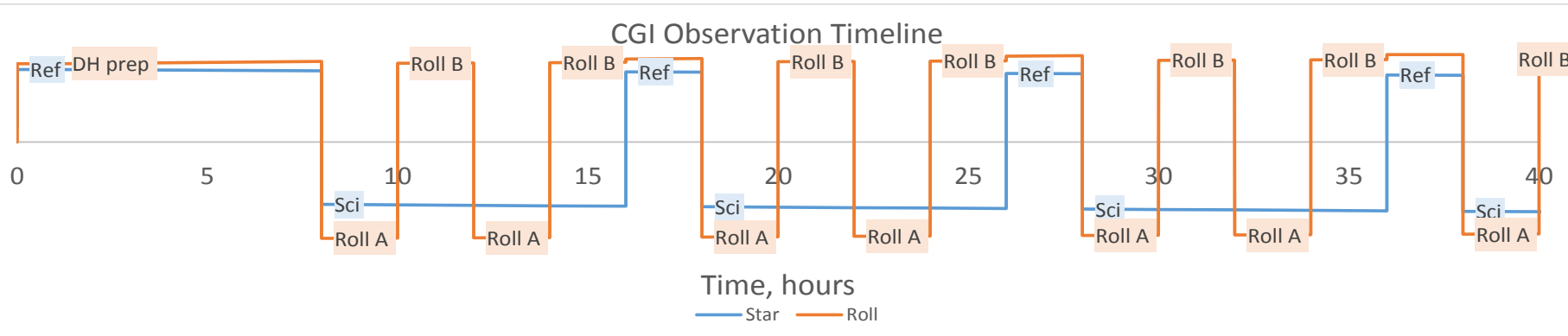
400

hrs max /pl.

571

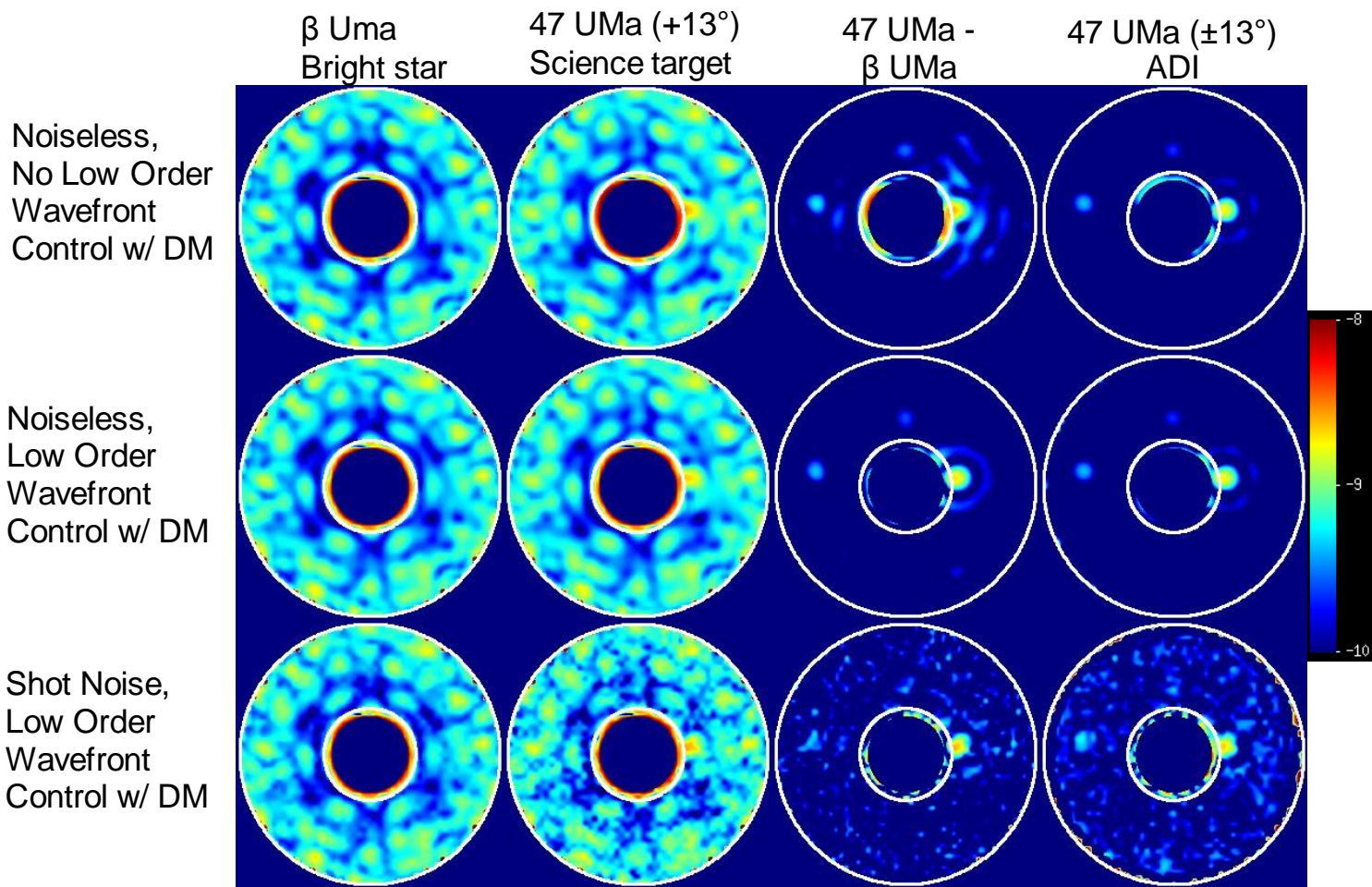
hrs all planets

No.	Pl. Name	Vmag	Sep (mas)	WA (I / D)	Critical SNR	FI Ratio, ppb	Time Margin	t (SNR), hrs	tot ph/px/fr	SMA (AU)	phase, deg	Sep, mas
2	Planet Sensitivity	5.0	200	4.00	90.4	12.9	99%	1	1.5	2.21	65	200.2
11	<i>epsilon Eri b</i>	3.7	347	6.94	141.7	11.4	100%	0.1	4.5	3.38	65	951.3
36	<i>GJ 832 b</i>	8.7	347	6.94	86.5	6.9	-100%	157.9	0.2	3.56	65	651.6
24	<i>55 Cnc d</i>	6.0	347	6.94	30.6	2.5	82%	17.9	0.3	5.47	65	402.0
7	<i>tau Cet f</i>	3.5	330	6.60	6.6	0.5	71%	28.7	0.9	1.33	65	330.2
21	<i>mu Ara e</i>	5.1	312	6.24	34.9	2.8	95%	4.7	0.5	5.34	65	312.0
38	<i>HD 142 c</i>	5.7	299	5.98	18.0	1.6	70%	30.1	0.3	6.80	65	299.2
26	<i>HD 217107 c</i>	6.2	243	4.86	18.9	2.7	74%	26.4	0.3	5.33	65	243.5
18	<i>HD 114613 b</i>	4.9	233	4.65	22.4	3.2	96%	4.0	0.8	5.31	65	232.9
16	<i>47 UMa c</i>	5.0	230	4.60	48.7	6.9	99%	1.4	1.0	3.57	65	230.2
20	<i>Gliese 777 b</i>	5.7	227	4.54	35.8	5.1	95%	5.0	0.5	3.97	65	227.1
27	<i>HD 154345 b</i>	6.8	205	4.11	32.5	4.7	74%	26.5	0.3	4.21	65	205.5
29	<i>HD 134987 c</i>	6.5	201	4.03	17.0	2.4	40%	60.4	0.3	5.83	65	201.5
40	<i>psi Dra B b</i>	5.8	182	3.64	21.3	4.1	88%	12.2	0.5	4.43	65	182.2
30	<i>HD 87883 b</i>	7.6	178	3.56	32.5	6.3	25%	74.8	0.2	3.58	65	178.0
10	<i>upsilon And d</i>	4.1	170	3.39	58.9	11.3	100%	0.4	2.6	2.52	65	169.6
17	<i>HD 39091 b</i>	5.7	166	3.31	31.2	6.0	94%	6.2	0.5	3.35	65	165.6
8	<i>beta Gem b</i>	1.2	154	3.07	130.7	24.6	100%	0.01	54.1	1.76	65	153.8
22	<i>14 Her b</i>	6.6	151	3.02	45.3	8.5	81%	19.1	0.3	2.93	65	151.3
12	<i>47 UMa b</i>	5.0	135	2.71	-1.0	17.5	-100%	-1.0	-1.0	2.10	65	135.4
6	<i>tau Cet e</i>	3.5	148	2.96	-1.0	1.8	-100%	-1.0	-1.0	0.54	90	147.9



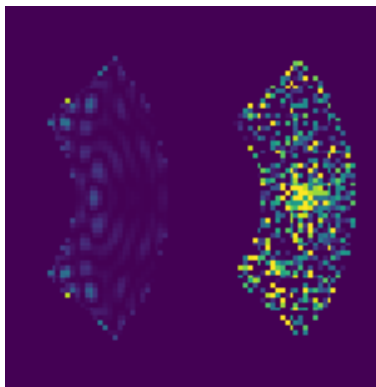
- Use both Roll-chop and Star-chop to mitigate drift on long integrations
- CGI dark hole prepared while pointed at Reference star
- 2-hour cadence of roll-chop maneuvers on target star
- 10-hour cadence of revisits to Reference star

OS6 Example Post-Processing

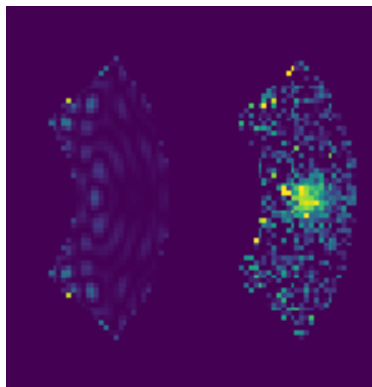


Comparison of RDI with perfect stability (top) and wavefront drift (bottom)

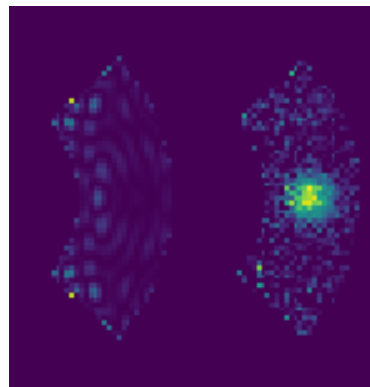
K=100



K=500



K=2000

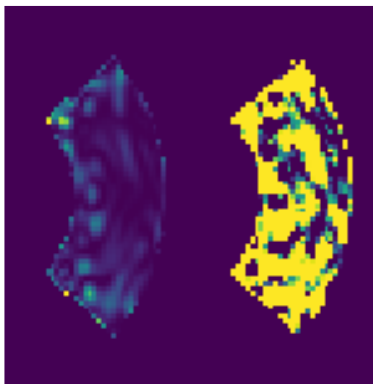


100s
Frames

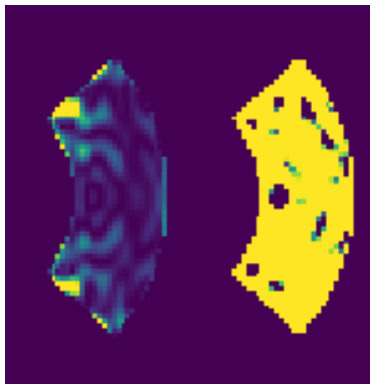
10 planet
photons
per frame

Left: Measurement, Right: After PSF subtraction. Speckles x5 planet at start.

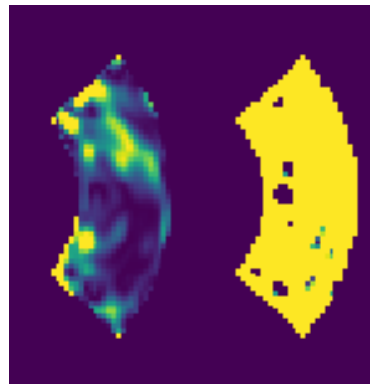
K=100



K=500



K=2000

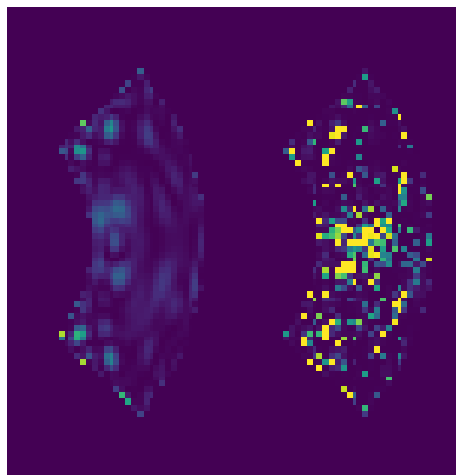


100 pm
wavefront
drift per
frame.

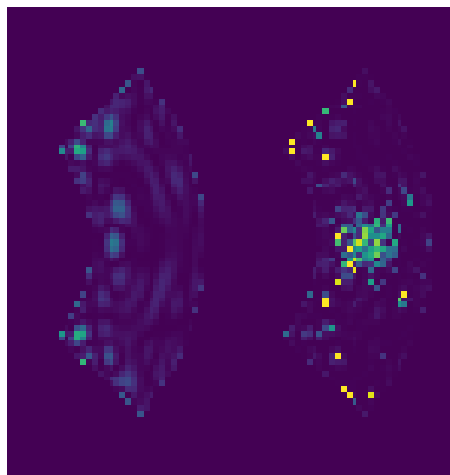
No
camera
noise.

Continuous closed-loop wavefront control during long integration using random DM dither.

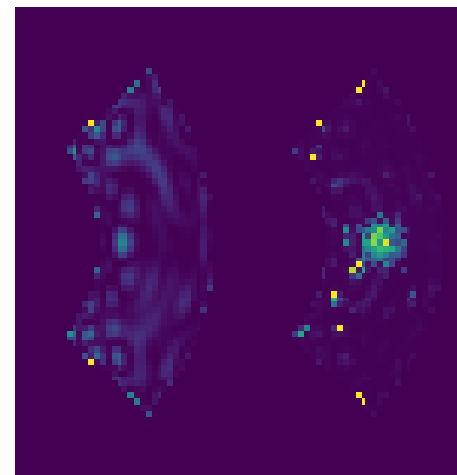
K=100



K=500

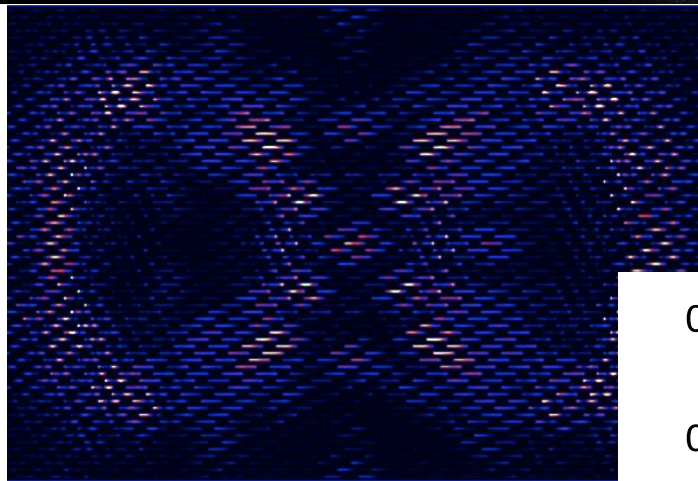


K=2000



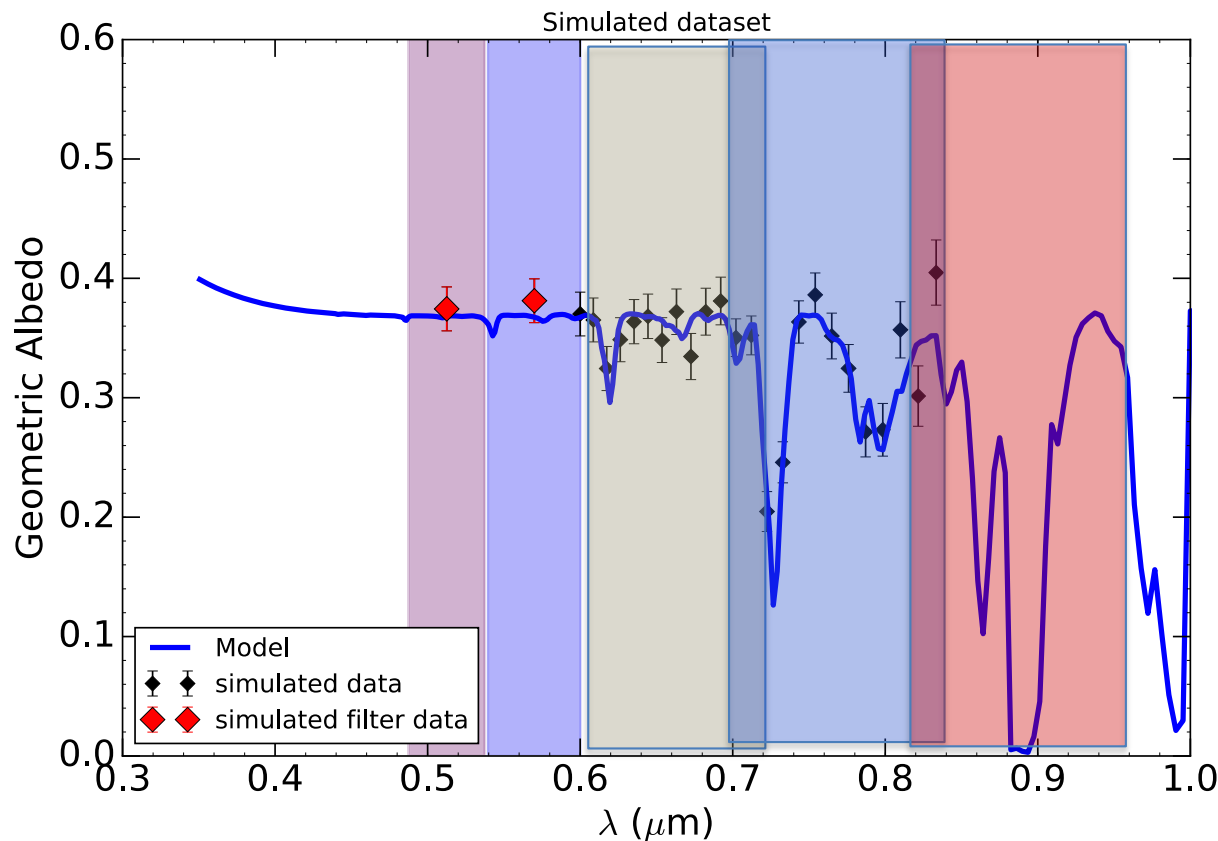
Same 100 pm per frame wavefront drift.

Spectral Retrieval

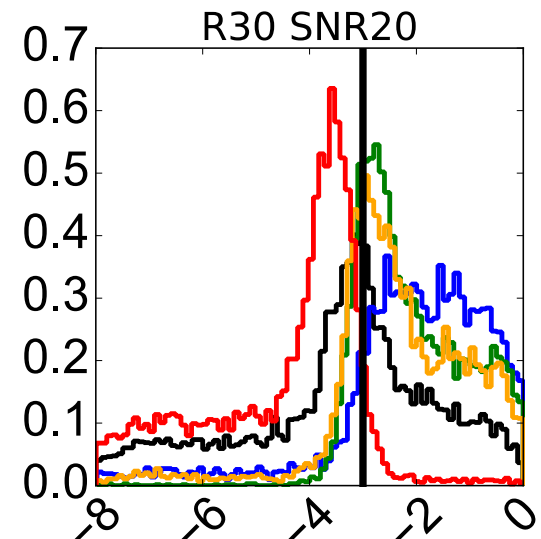
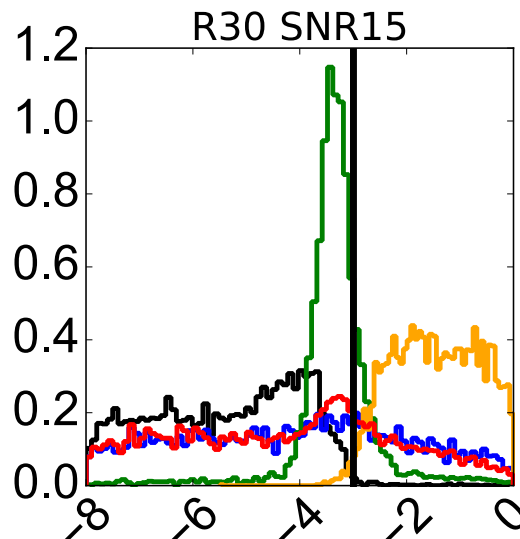
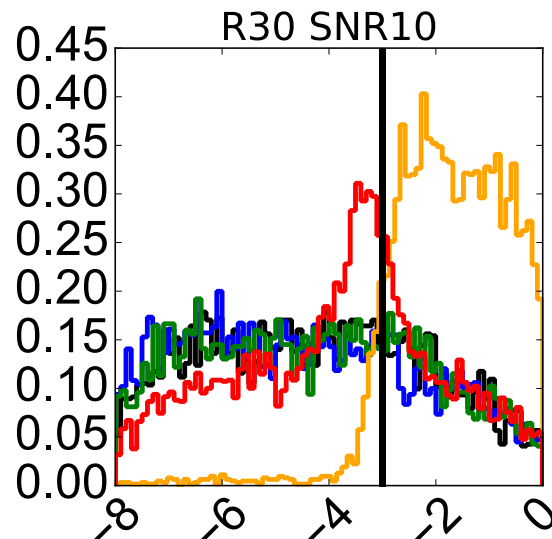
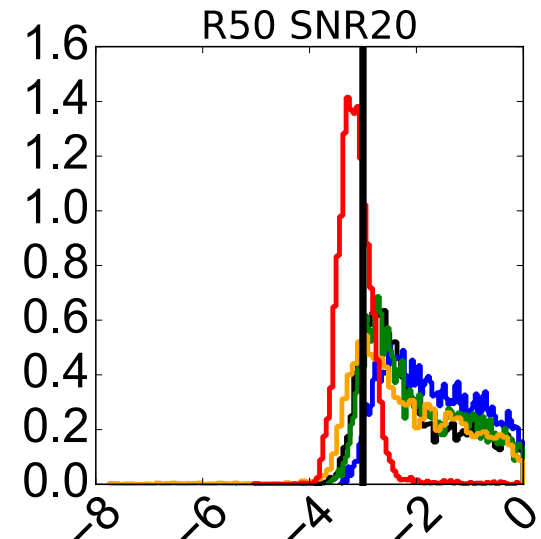
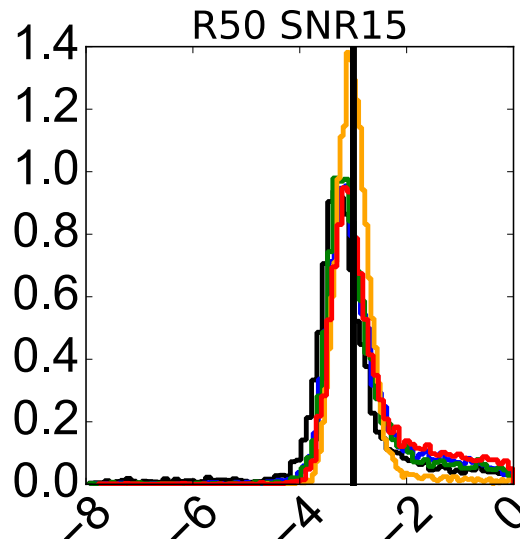
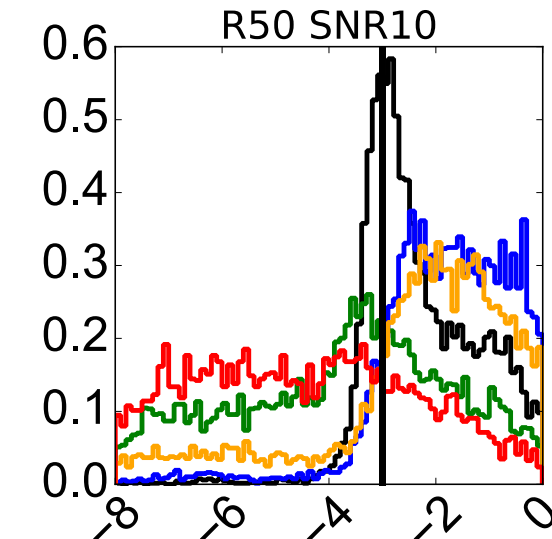


Multiple SIT
 members
 developing
 spectral retrieval
 approaches.
 Verified through
 a community
 data challenge.

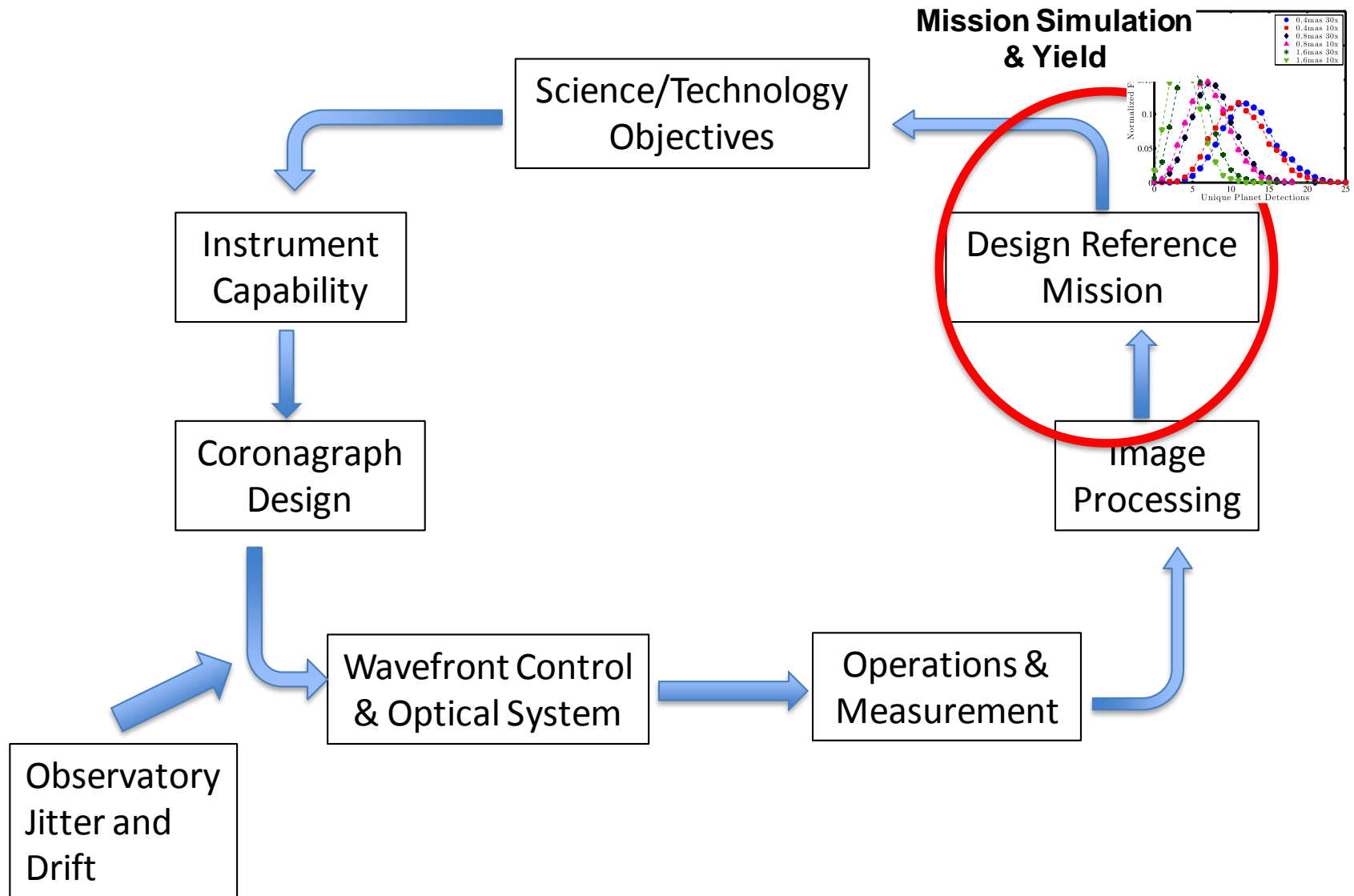
GPI / P1640 / CHARIS style IFS



Ex.: Spectral Resolution & SNR for Methane Detection



Coronagraph Design

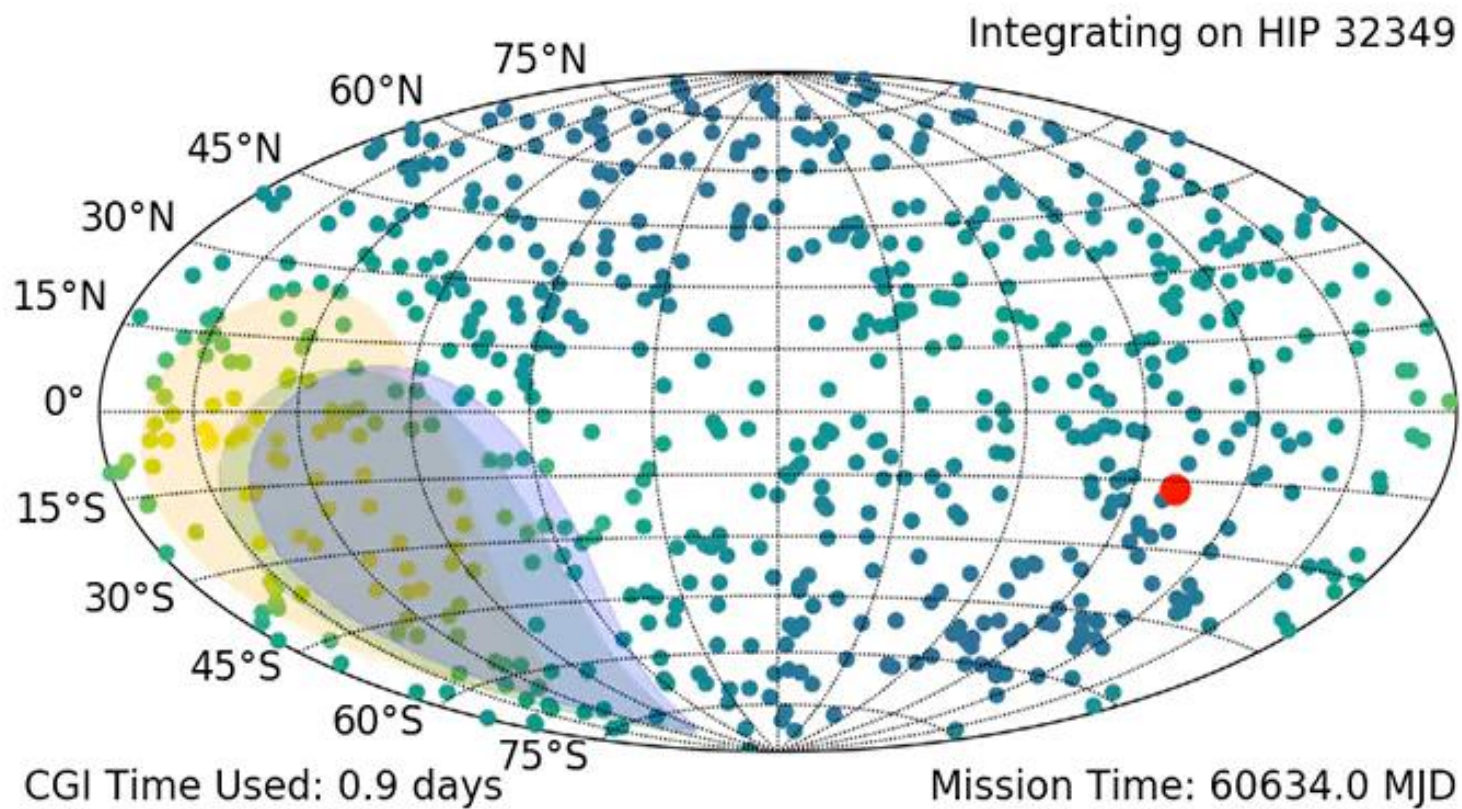


With integration time calculations can build a "Design Reference Mission", the order of observing to determine total science yield.

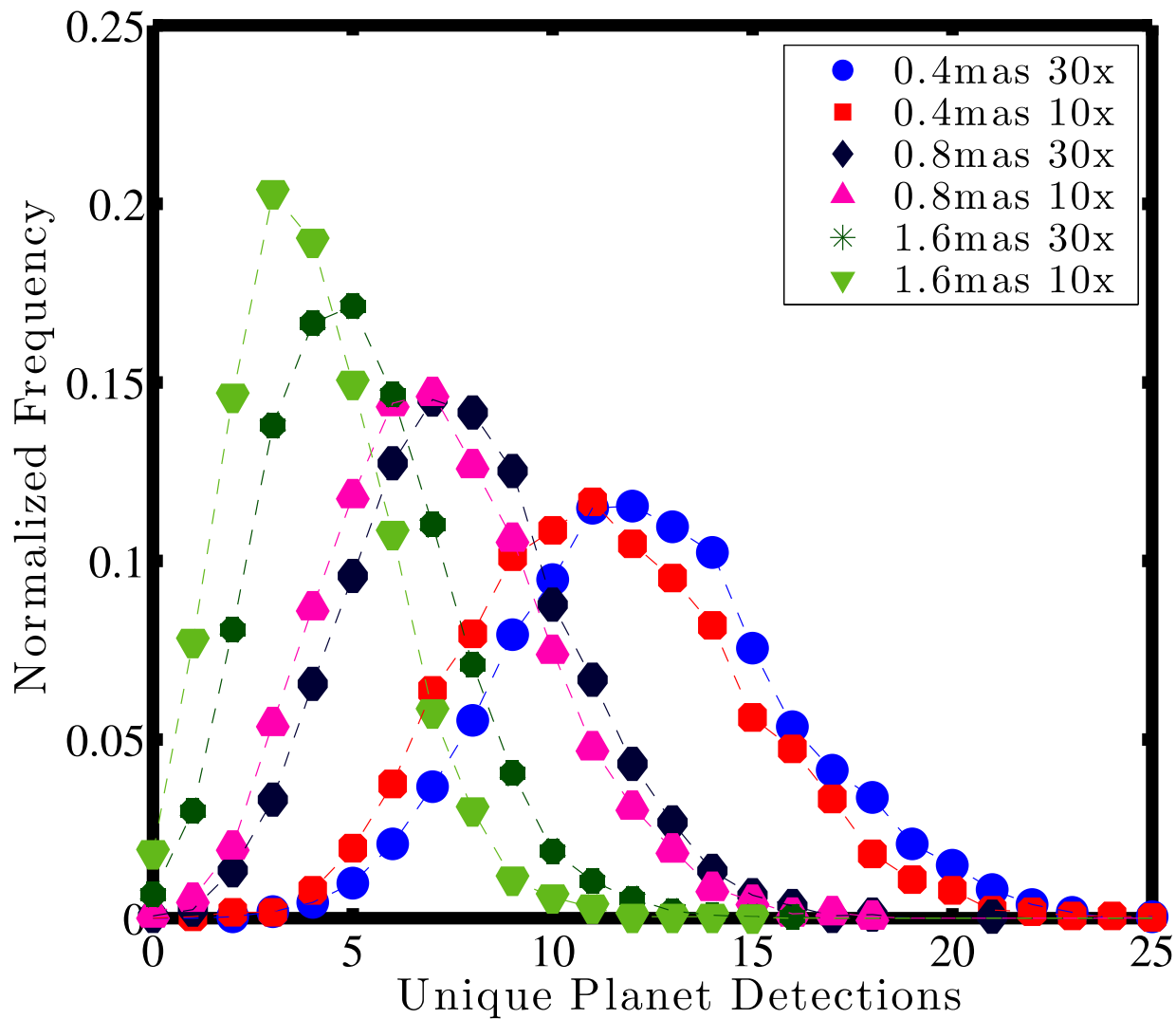
Two general approaches:

- Semi-analytical optimization (Stark, see talk)
- Monte-Carlo Mission Builder (ExoSim – Savransky)

Courtesy Dmitry Savransky

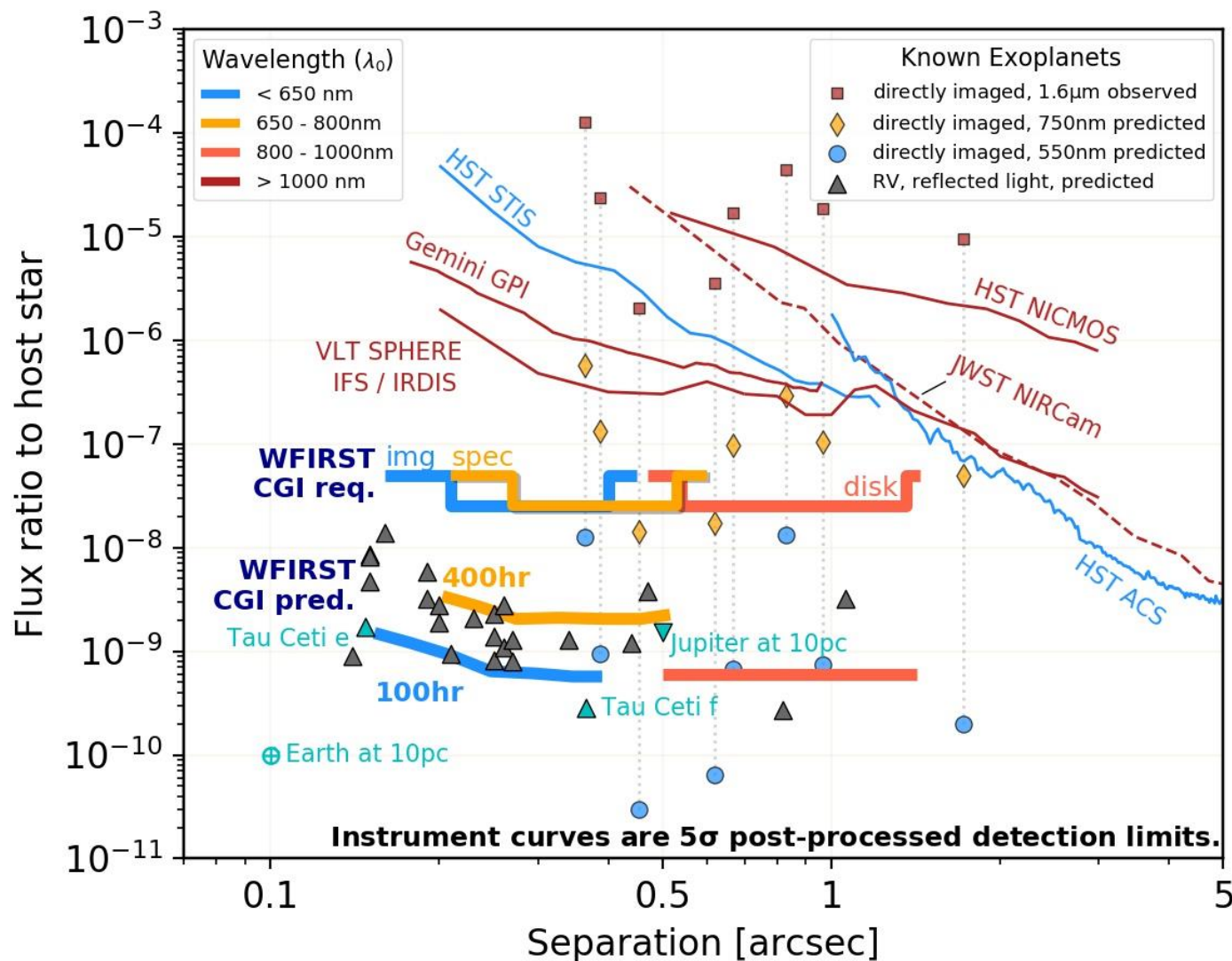


Courtesy Dmitry Savransky





All of these pieces then come together to produce estimates of capability and potential science yield.



Giant Planet
Imaging
Photometry

Narrow-band
Spectroscopy of
Self-luminous &
RV Planets

New Planet
Discovery

Exozodiacal Disk
Imaging

Visible light
characterization
of Debris Disks

- R50 Spectra of ~ 2 young, self-luminous super-Jupiters
 - Beta Pic b, HR 8799 e, 51 Eri b
- Masses for ~ 10 Jupiter analogues
 - Imaging breaks $v \sin(i)$ degeneracy in mass of RV planets
- R50 Spectra of 1-2 Jupiter analogues
- Circumstellar disks
 - Image 2-4 bright, known debris & protoplanetary disks
 - More details of inner regions; new wavelengths
 - First images of 1-2 (faint) exozodi disks

➤ CGI Exoplanet Potential Science

- ~ double the number of planets with imaging and spectroscopy
- More than double the number of imaged disks
- ~ 3 months for a search for new planets
 - Could discover ~10 new Jupiter analogues
 - May discover a few Neptunes or mini-Neptunes
- “pre-imaging” of ~20 highest priority systems for exo-Earth missions
 - Exo-Earth imaging needs “clean” (low dust) systems
 - Detect / rule out Jupiter analogues in systems with poor RV constraints

➤ Expanded science areas & **possible GO program**

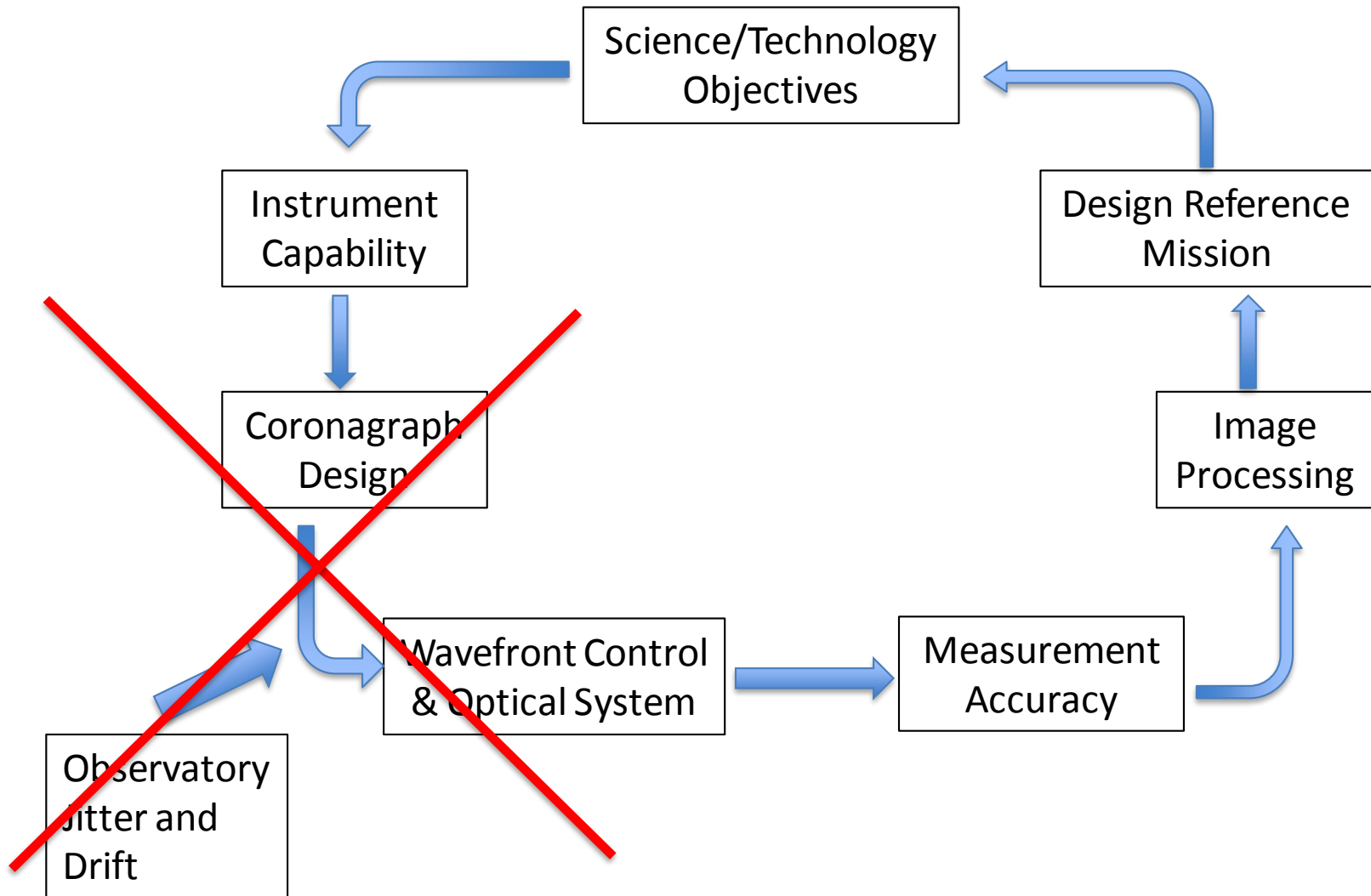
- new kinds of community-driven exoplanet & disk science
- evolved stars, quasars, Solar System objects, ...

➤ Possible **starshade rendezvous**

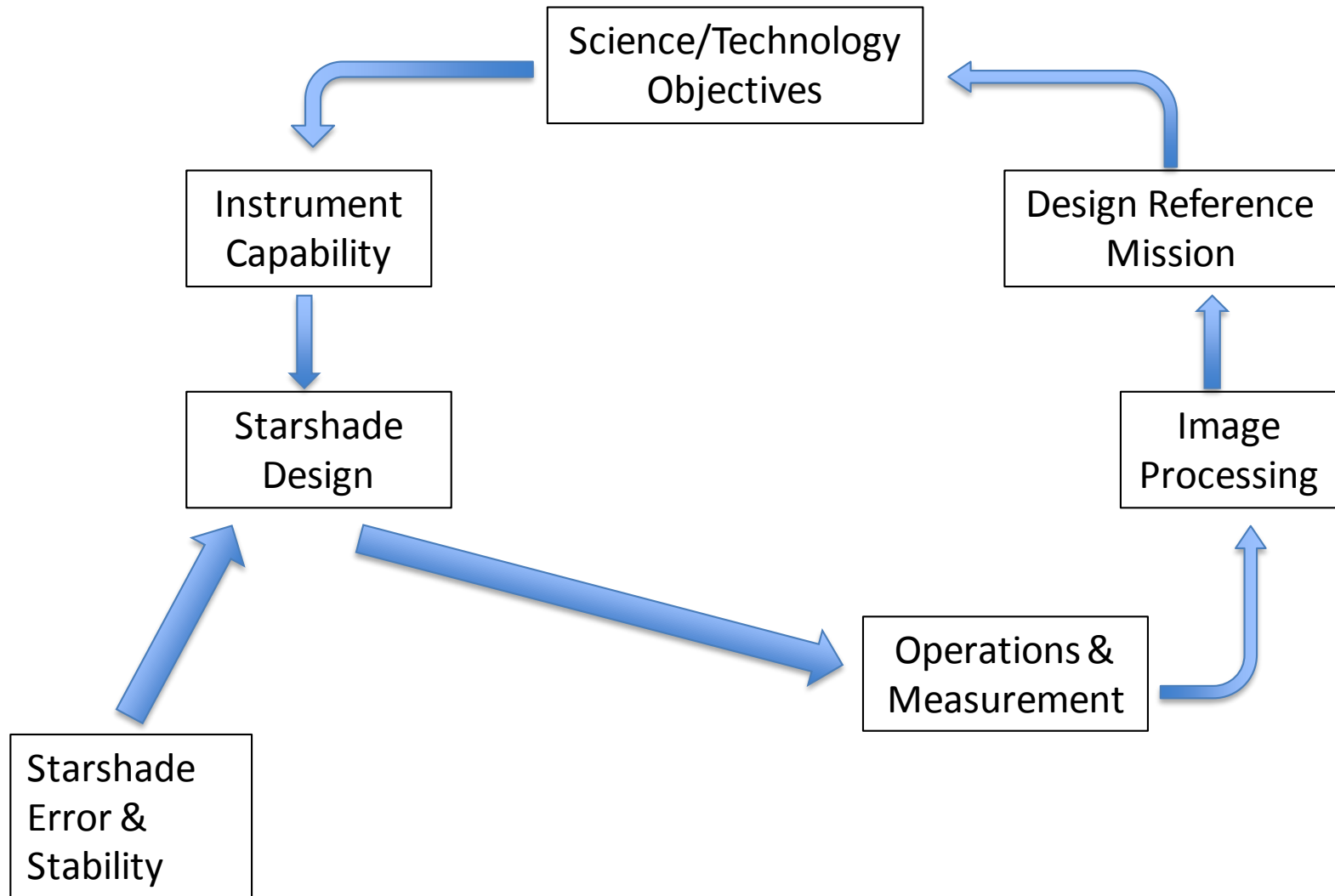
- CGI is pioneering all elements of an advanced coronagraph in space
- Designing and building CGI is reaping tremendous benefits for future missions
- Flying CGI will demonstrate full active coronagraph capability in space for first time.
- Flight characterization of entire system
- Potential for advances in science is significant.



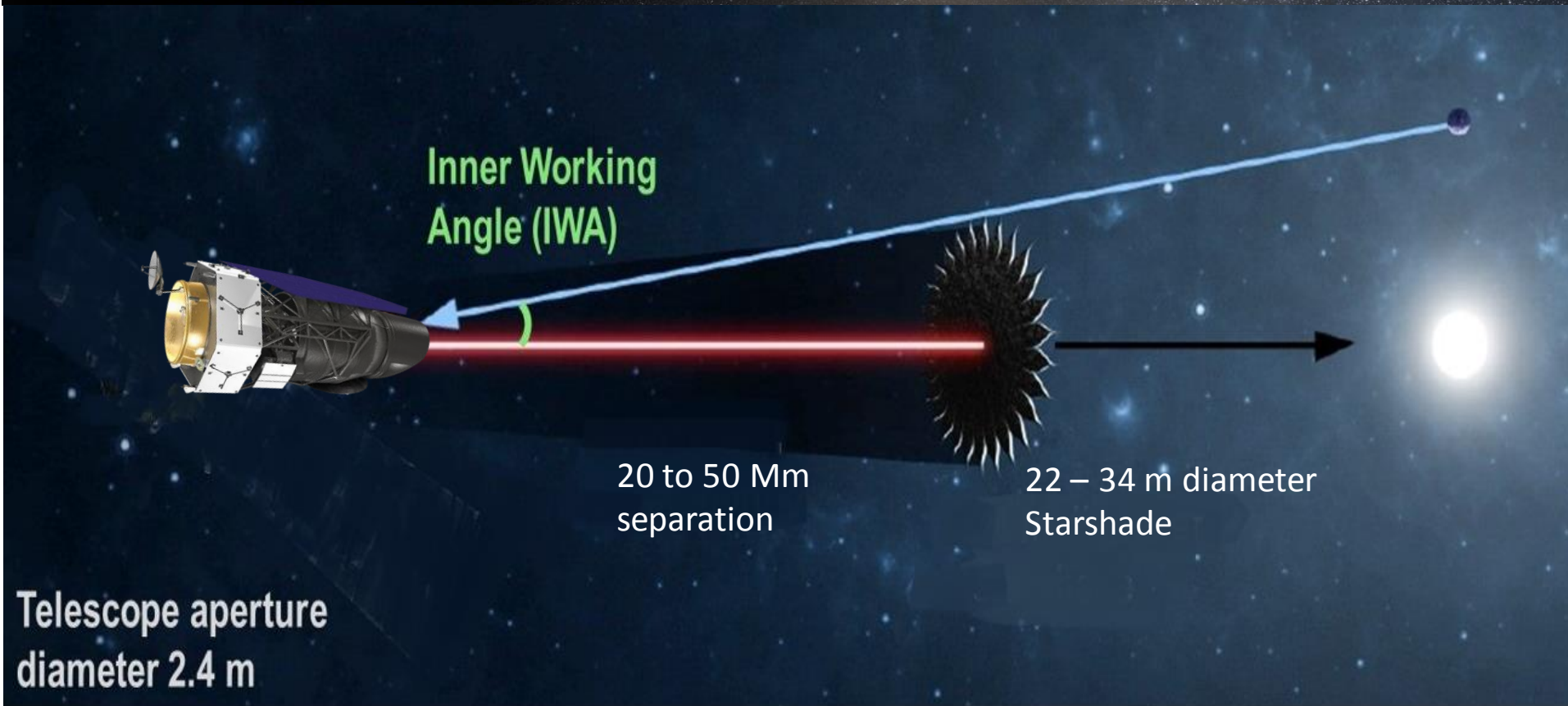
A Starshade Mission



A Starshade Mission

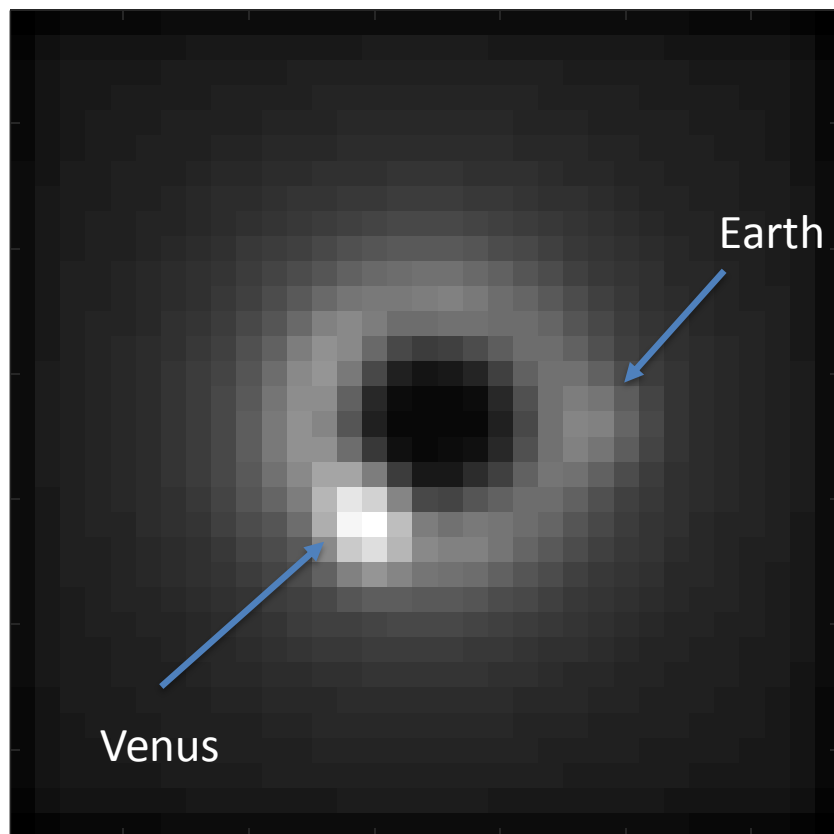


Starshades for Exo-Earth Imaging

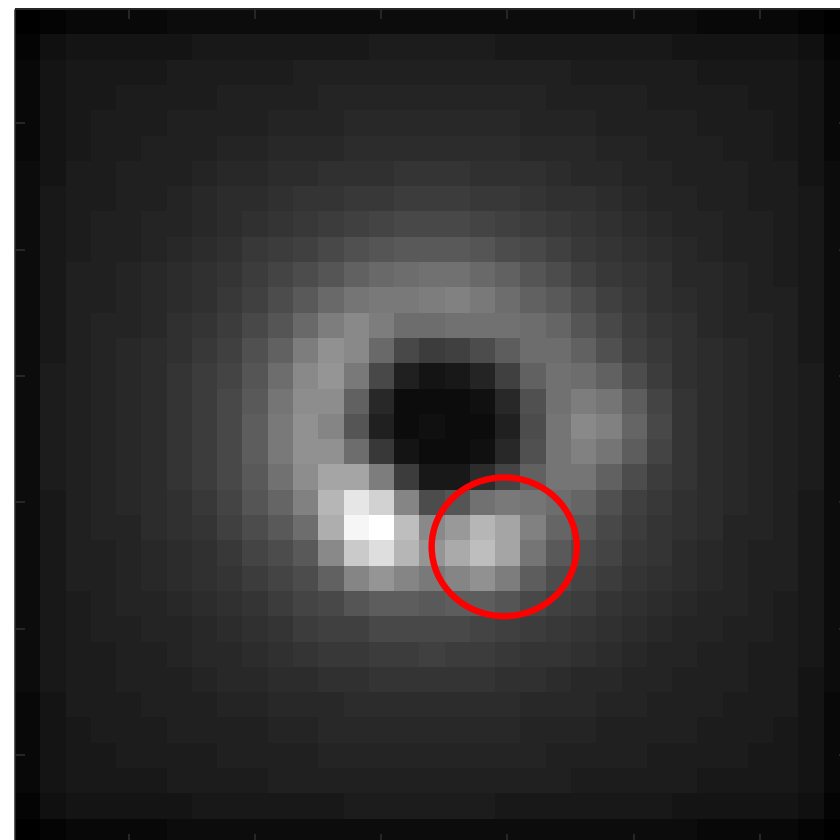


With small impact to WFIRST and CGI, we can give the 2020 Decadal Survey the option to recommend a starshade for enhanced science and technology demonstration.

Perfect starshade



Truncated Tip



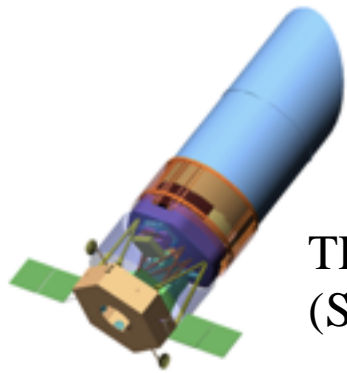
Starshade Basics

- Contrast and IWA independent of telescope aperture size
 - Enables small inner working angle with 2.4 m telescope and access to habitable zone
 - Enables detection of smaller, close-in planets
- No outer working angle – Large FOV
 - Enables imaging of entire planetary systems, mosaicing from within dark shadow
- High throughput, broad wavelength bandpass
 - Enables spectral characterization of smaller planets in feasible time
- Can work in tandem with coronagraph
 - Coronagraph: orbits of brighter planets, Starshade: spectra of smaller planets
 - Potentially enables work on binaries like alpha Cen
- Wavefront correction unnecessary
 - Adds robustness to exoplanet program
- Retargeting requires long starshade slews (days to weeks)
 - Long down times compatible with interleaved observations
 - Starshade revisits are challenging but CPM confirmation is possible for high priority targets within single observation epoch (~2 weeks)

Modern Mission History

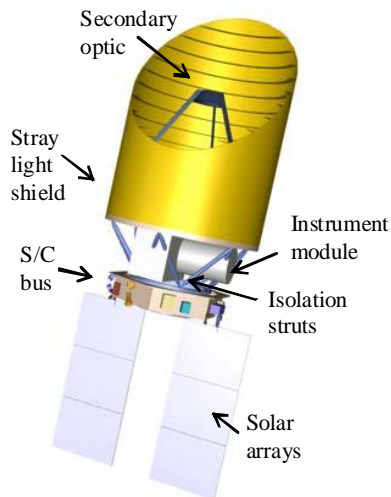
First suggested by Lyman Spitzer in 1962. Later, BOSS in 2000 & UMBRA in 2003.

2010 Decadal Survey



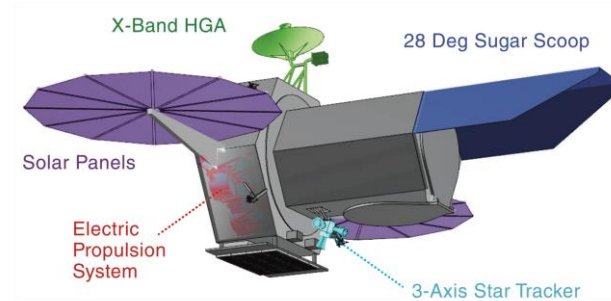
THEIA
(Spergel & Kasdin)

4 m
Telescopes
with Large
Starshade



NWO
(Cash)

2015 Probe Studies



Exo-S
(Seager)

1.1 m Telescope,
30 m Starshade
3-5 Earths in HZ

Also recommended was a rendezvous w/ WFIRST

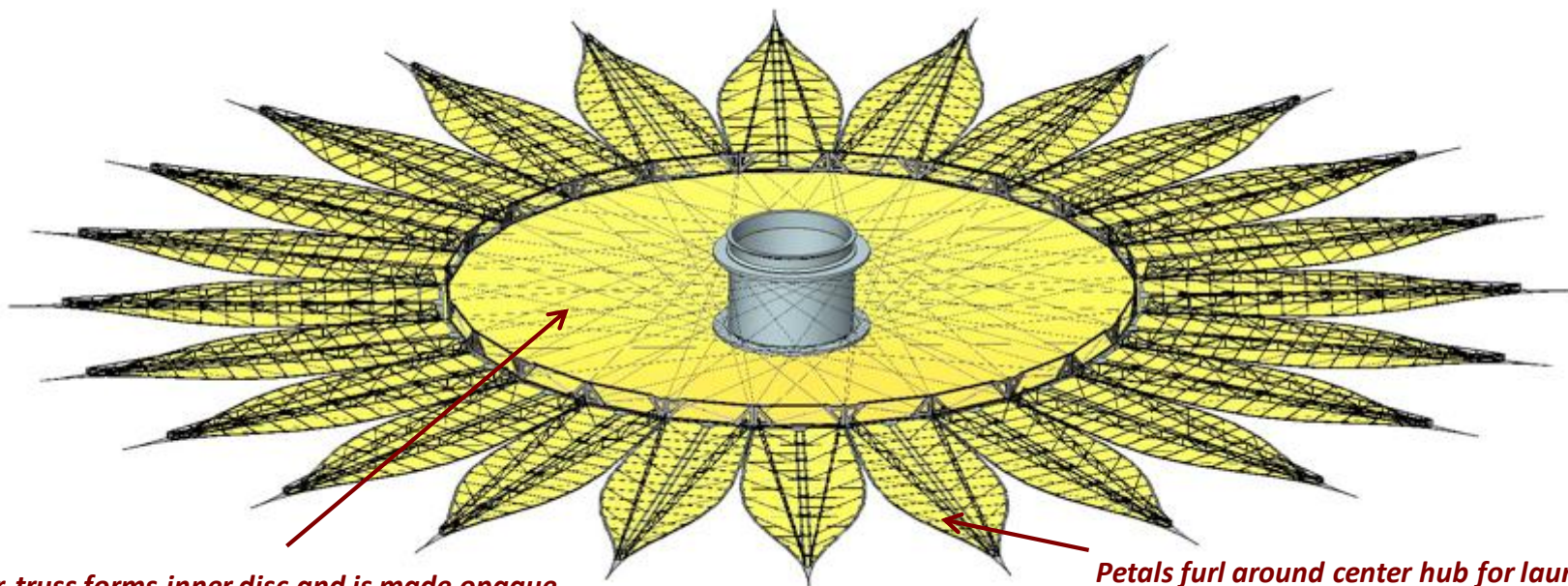
2020 Decadal Probe Studies



WFIRST Rendezvous
(Seager and Kasdin)

Rendezvous Mission Concept

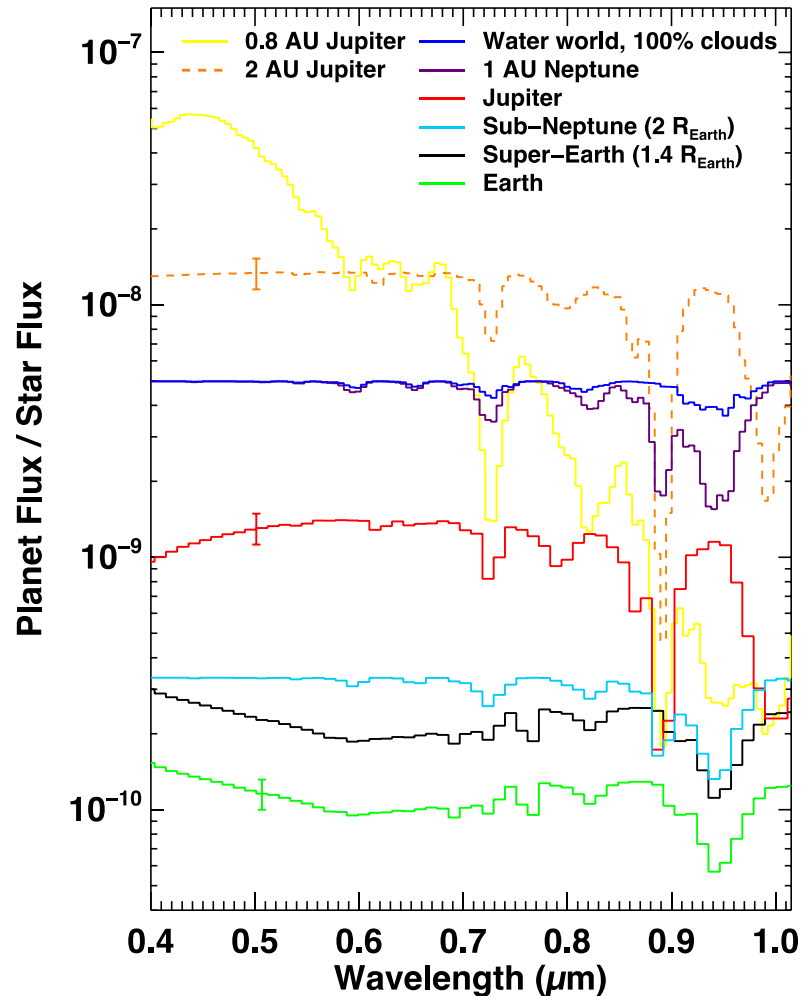
- Starshade launches separately to rendezvous with WFIRST already operating at E-S L2
- Starshade is sized to provide access to habitable zones around nearby stars and create a dark shadow with diameter 2-m larger than the telescope (22 – 34 m)
- Perform "Deep Dive" on systems around a dozen of the nearest sun-like stars
- Starshade performs large translation maneuvers to line up on target stars and fine lateral control maneuvers to keep the dark shadow on the telescope
- WFIRST provides instrumentation and fine formation sensing via the CGI



Perimeter truss forms inner disc and is made opaque with an origami folded optical shield

Petals furl around center hub for launch and become rigid with pop-up ribs

Rendezvous Science

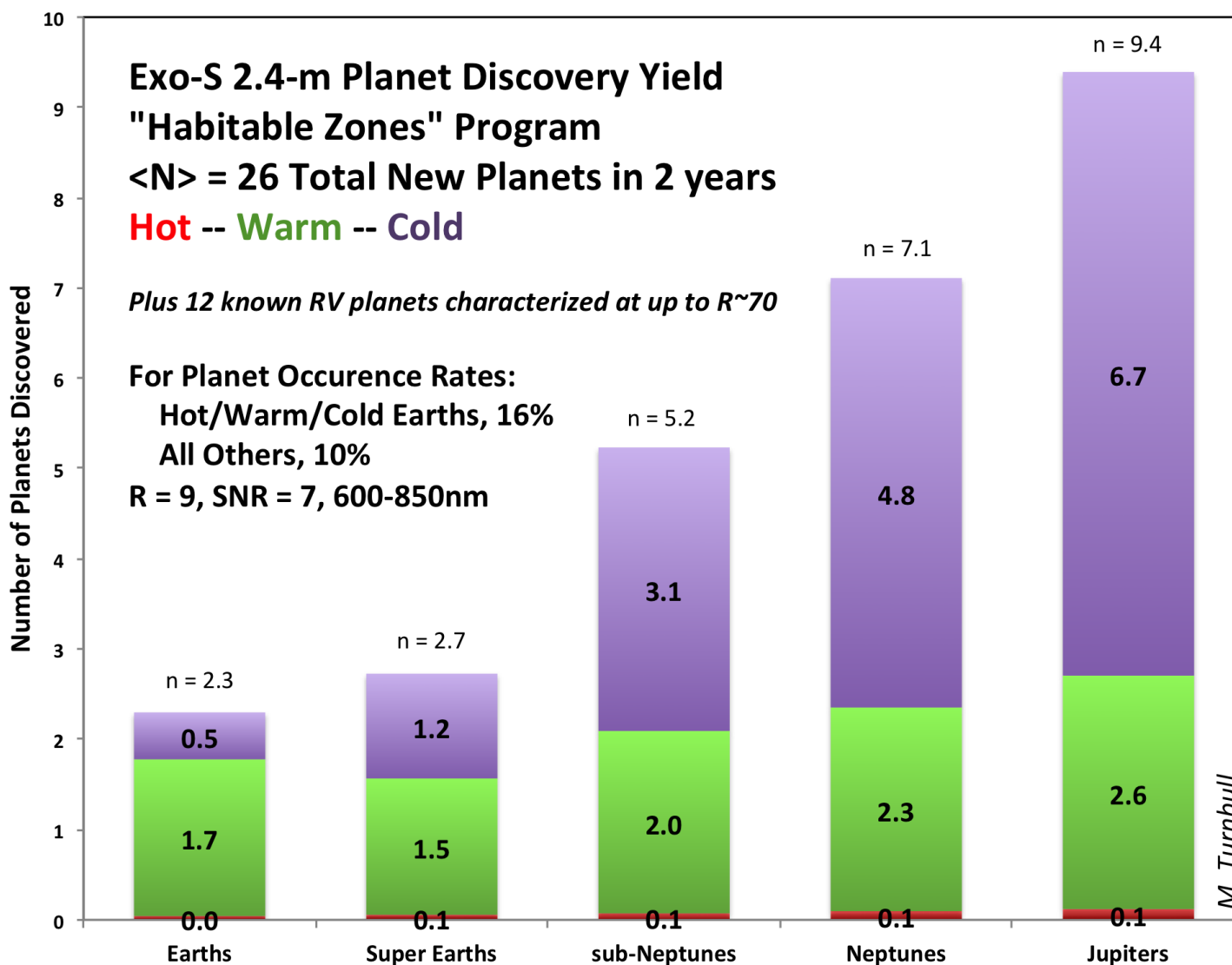


Simulated spectra for the Rendezvous mission, with three representative 10% error bars for SNR=10.

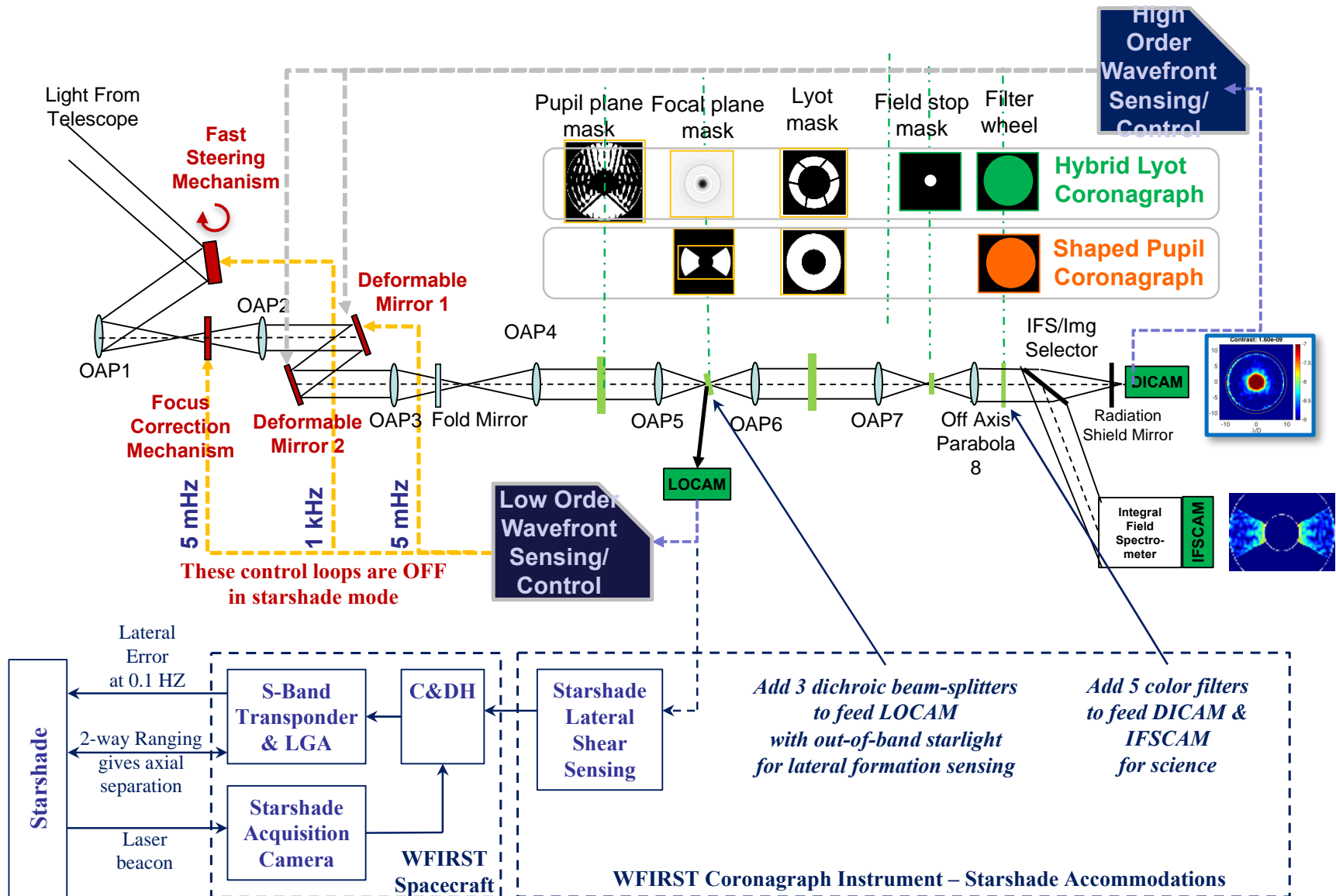
- 1) Discover new exoplanets from giant planet down to Earth size
- 2) Characterize new planets by spectra ($R=10$ to 70)
 - Wavelength range from 400–1,000 nm, in three bands
- 3) Characterize known giant planets by spectra ($R=70$) and constrain masses
 - detectable by virtue of extrapolated position in mid-to-late 2020 timeframe
- 4) Study planetary systems including circumstellar dust in the context of known planets
 - dust-generating parent bodies
 - possible detection of unseen planets
 - assessment of exozodi for future missions

A DRM proof of concept is in process.

Example Yield



WFIRST Starshade Accommodation

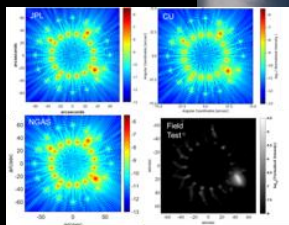


S5 Starshade Technology Gaps

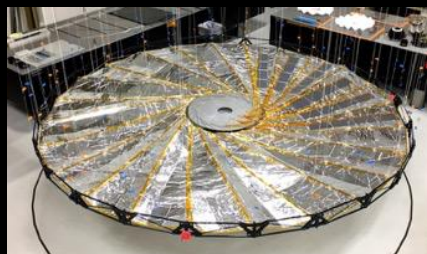
(1) Starlight Suppression



Suppressing scattered light off petal edges from off-axis Sunlight (S-1)

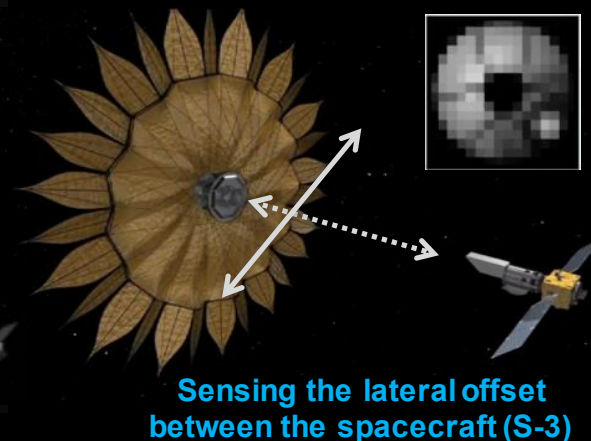


Suppressing diffracted light from on-axis starlight and optical modeling (S-2)



Positioning the petals to high accuracy, blocking on-axis starlight, maintaining overall shape on a highly stable structure (S-5)

(2) Formation Sensing



Sensing the lateral offset between the spacecraft (S-3)

(3) Deployment Accuracy and Shape Stability

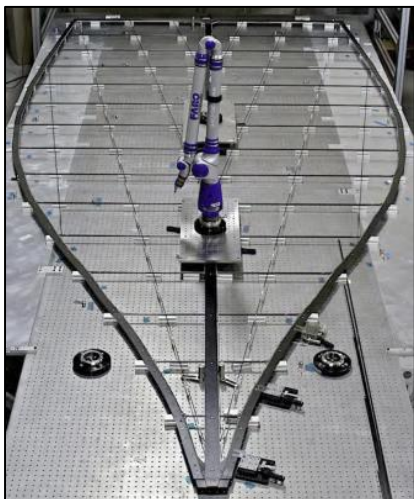


Fabricating the petals to high accuracy (S-4)

Starshade Mechanical Progress

Past efforts demo tolerances for:

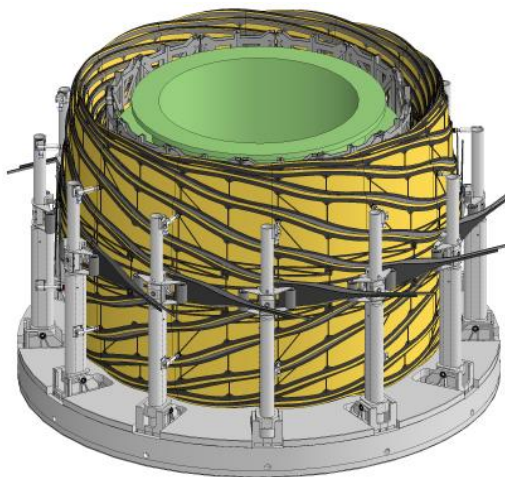
Petal Manufactured Shape



TDEM-09: J. Kasdin, PI

Ongoing efforts demo how to:

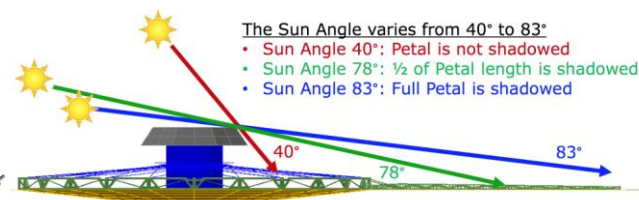
Unfurl Petals



Jettisoned rotating carousel

Future efforts need to demo:

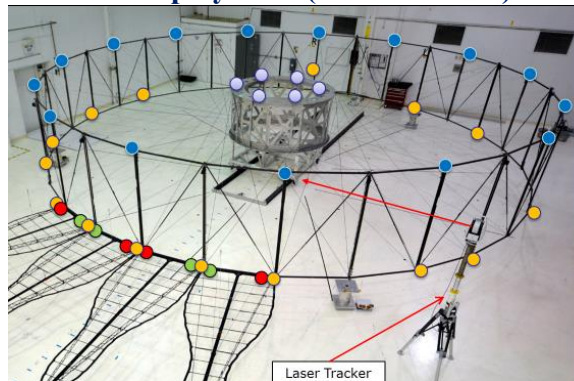
On-orbit stability over temperature



Performance is fortunately insensitive to uniform shape change.

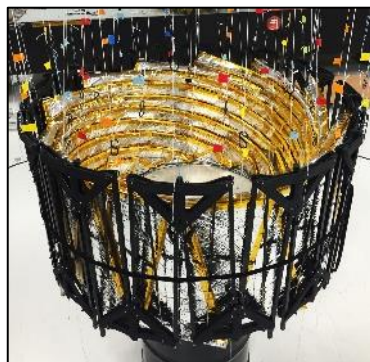
Non-uniform thermal shape changes contribute less than 10% of the total max expected instrument contrast.

Disk Deployment (Petal Position)



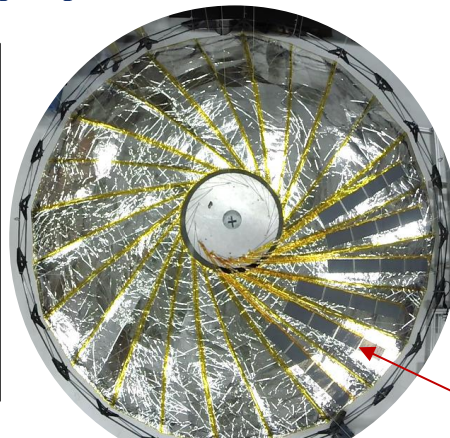
TDEM-10: J. Kasdin, PI

Co-deploy an opaque optical shield

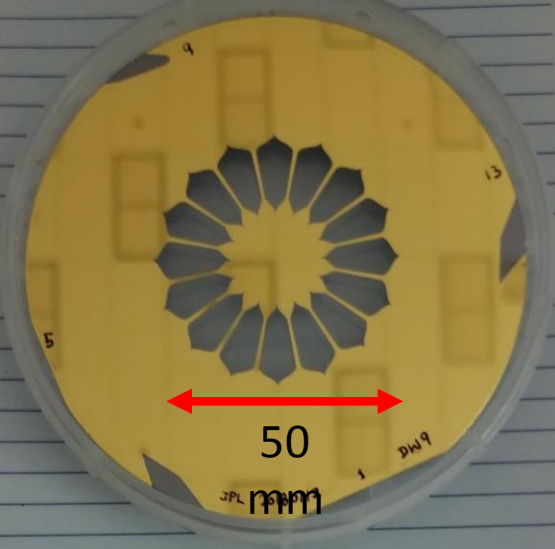


Wrapped spiral gores

Disk deploy tolerances with optical shield installed.



Thin-film solar cells could power SEP



Lack of full-scale starshade test before launch places **strong** reliance on optical models

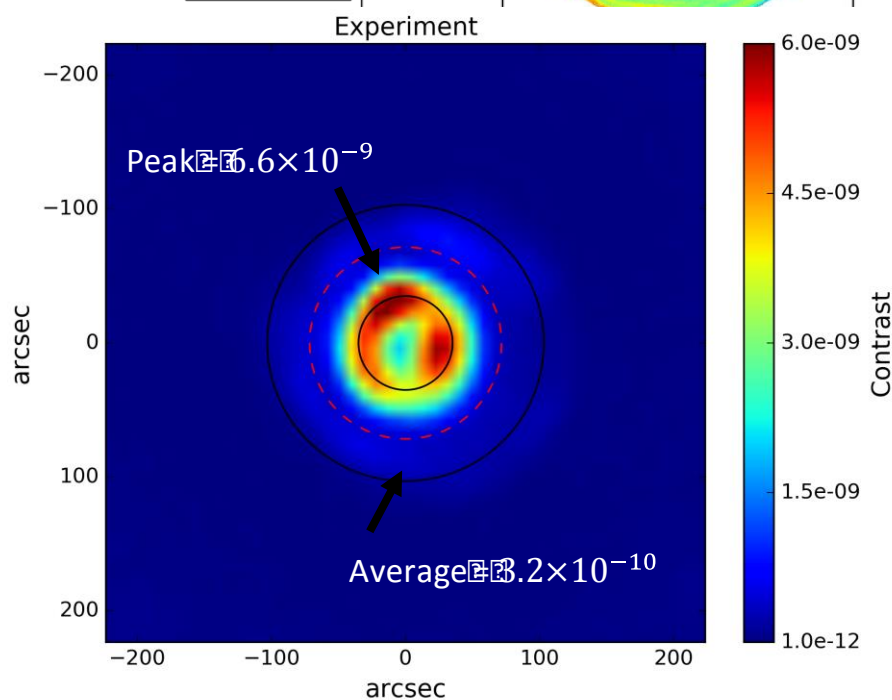
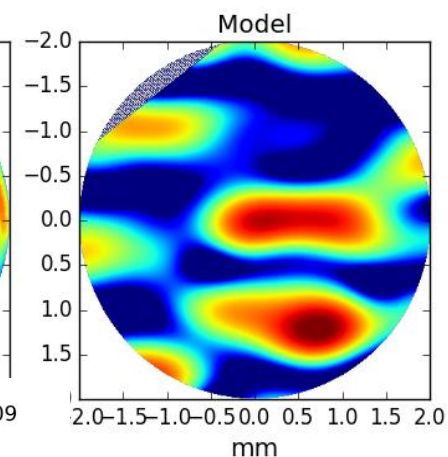
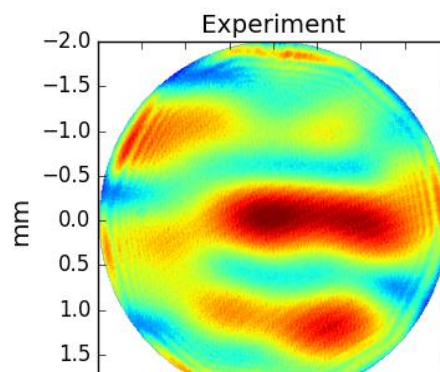
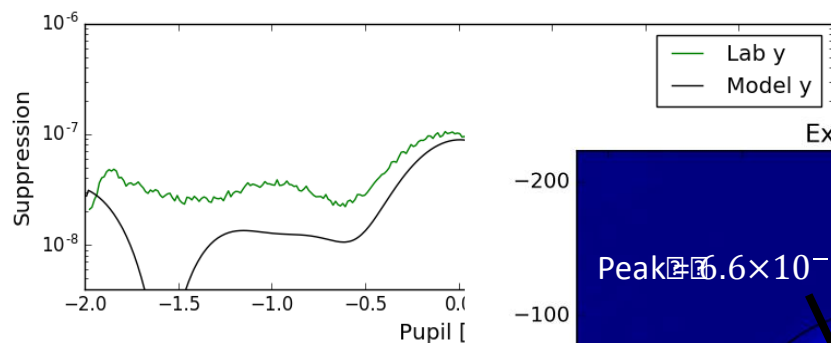
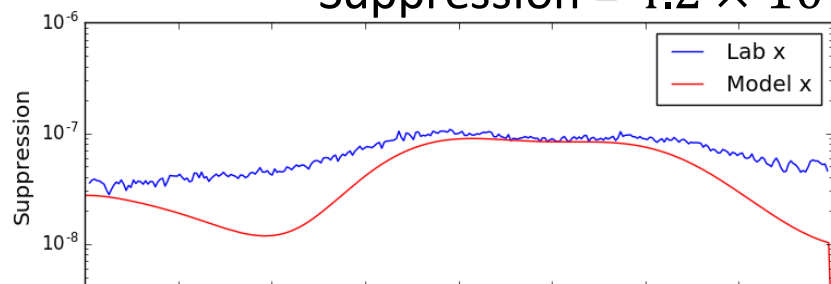


Princeton
Starshade
Testbed

Goal to
Achieve $1e-9$
Suppression
and $1e-10$
Contrast

Current Status

Suppression = 4.2×10^{-8}





Thank You.