

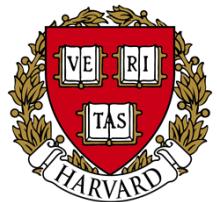
\*

# Everything You Always Wanted to Know About Differential Privacy\*



**Kobbi Nissim**

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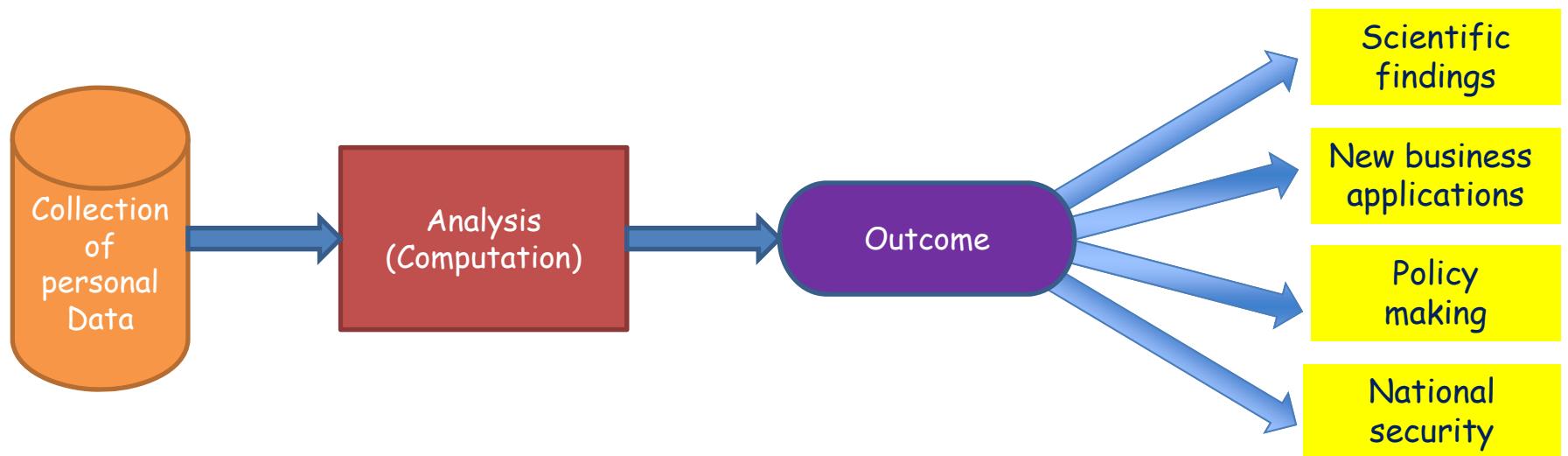
**Alexandra Wood**

Berkman Klein Center for Internet & Society  
Harvard University

Challenges and New Approaches for Protecting Privacy in Federal Statistical Programs  
National Academies of Sciences, June 6, 2019

(\*But Were Afraid to Ask)

# Data Privacy: The Problem



Given a dataset with sensitive personal information, how can one compute and release functions of the dataset while protecting individual privacy?

# Attacks on SLD Techniques

- Re-identification [Sweeney '00, ...]
  - GIC data, health data, clinical trial data, DNA, literacy data, text data, registration information ...
- Blatant non-privacy [Dwork, Nissim '03],
- Auditors [Kenthapadi, Nissim, Nissim '05]
- (C) Dabade '06
- General-Variable association studies (GVA) [Homer et al. '08]
- Netflix award [Narayanan, Shmatikov '09]
- Social networks [Backstrom, Dwork, Kleinberg '11]
- Genetic research studies [Gymrek, McGuire, Golan, Halperin, Erlich '11]
- Microtargeted advertising [Korolova '11]
- Recommendation Systems [Catalini, Tadelis, Naryanan, Feiten, Shmatikov '11]
- Israeli CBS [Mukatren, Nissim, Salman, Horie '14]
- Attack on statistical aggregates [Homer et al. '08] [Dwork, Smith, Steinke, Vadhan '15]
- Reconstruction attack on 2010 Census data

Slide idea stolen shamelessly from Or Sheffet

# Takeaways from Privacy Failures

In setting clear meaningful privacy goals

Lack of rigor leads to

unanticipated privacy failures.

In analyzing resilience to future attacks

In taking auxiliary knowledge into account

In accounting for privacy loss across multiple releases

In scrutiny of privacy technology

In understanding how normative and technical conceptions of privacy interact

# Takeaways from Privacy Failures

- Specific findings:

- Redaction of identifiers is insufficient for protecting privacy.
- Similarly: aggregation, noise addition\*, ...
- Auxiliary information needs to be taken into account.
- Regulation and technology only considered a limited scope of privacy failures.
  - New failure modes: whether an individual participated in study, inferences
- Any useful analysis of personal data must leak some information about individuals.
- Leakages accumulate with multiple analyses/releases.

Mathematical facts, not matters of policy

# A New Line of Work

Emerging from theoretical computer science (~2003).

Yields new concept: **Differential privacy** (2006):

- Rich theory and new privacy concepts.
- Mathematically provable privacy guarantees.
- In first stages of implementation and real-world use
  - US Census, Google, Apple, Uber, ...

Yeah, Yeah ...



To make you laugh,  
out loud!  
**TypeOL**

# **What is Differential Privacy?**

# Differential Privacy is ...

... not a specific technique or algorithm!

# Differential Privacy is ...

... a **definition** (i.e., a standard) of privacy\*

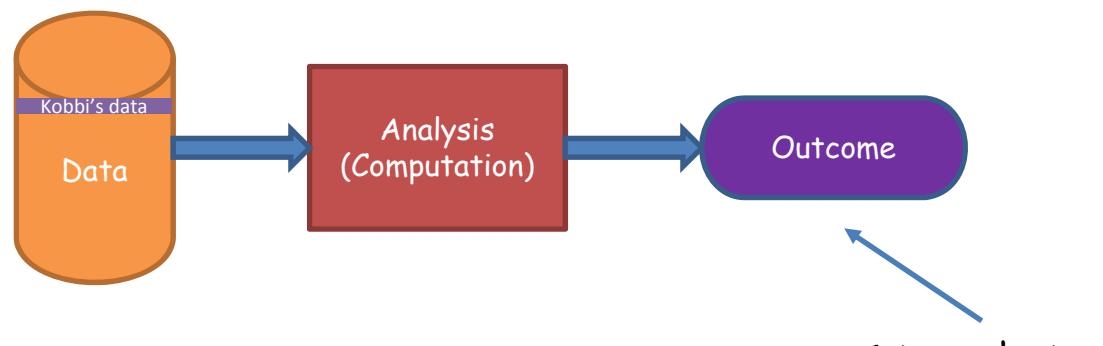
It expresses a specific desiderata of an analysis:

Any information-related risk to a person should not change significantly as a result of that person's information being included, or not, in the analysis.

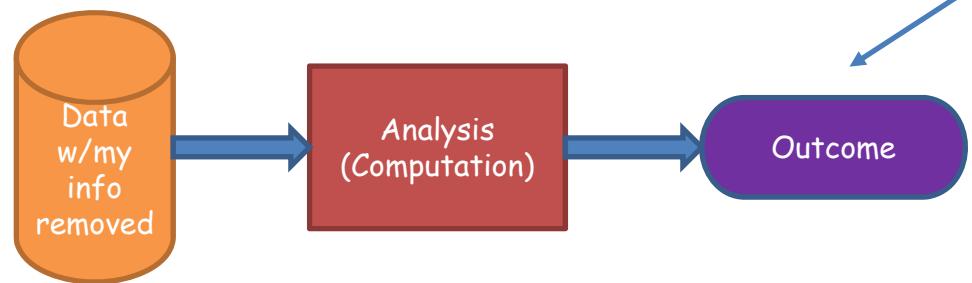
\*More precisely, a family of related mathematical definitions: pure DP, approximate DP, concentrated DP, ...

# A Privacy Desiderata

Real world:

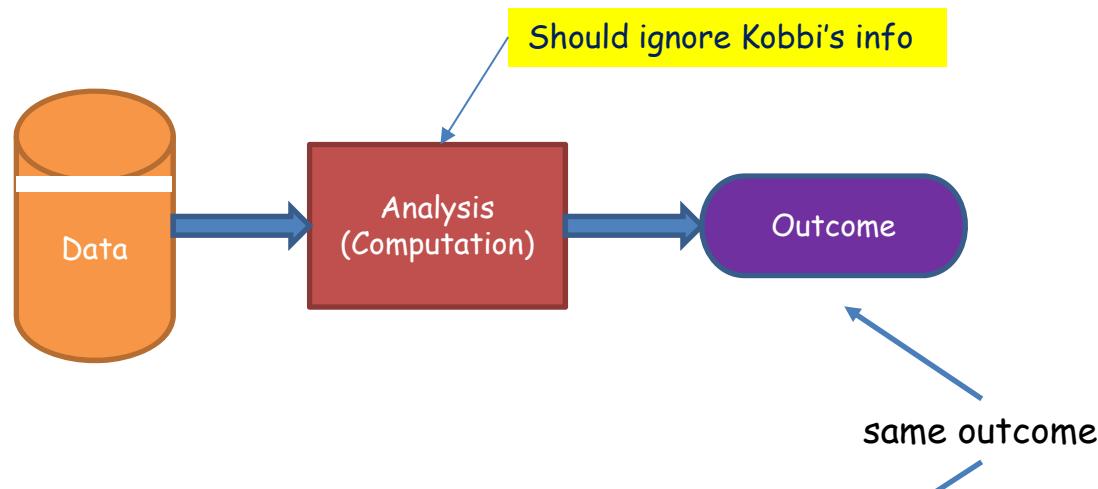


My ideal world:

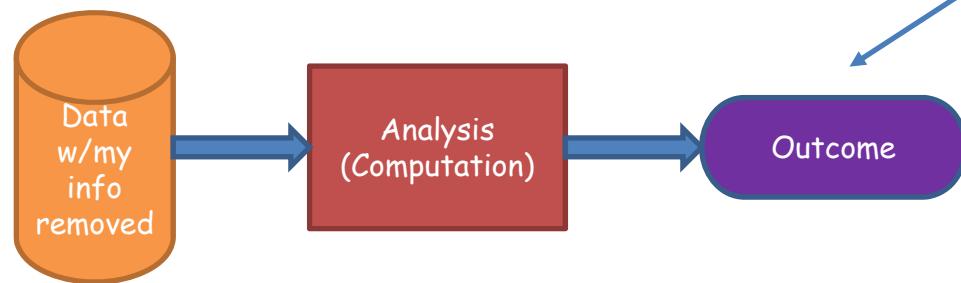


# A Privacy Desiderata

Real world:

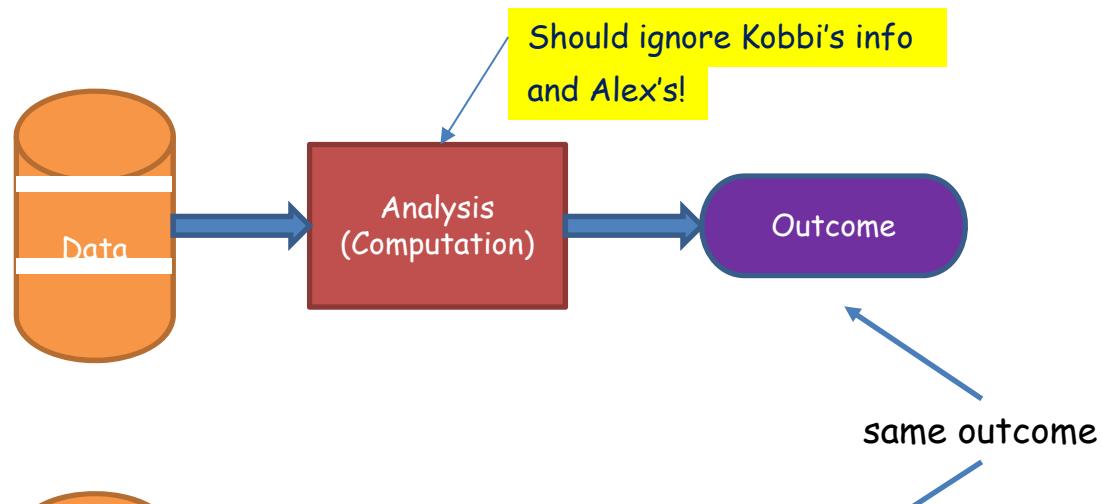


My ideal world:

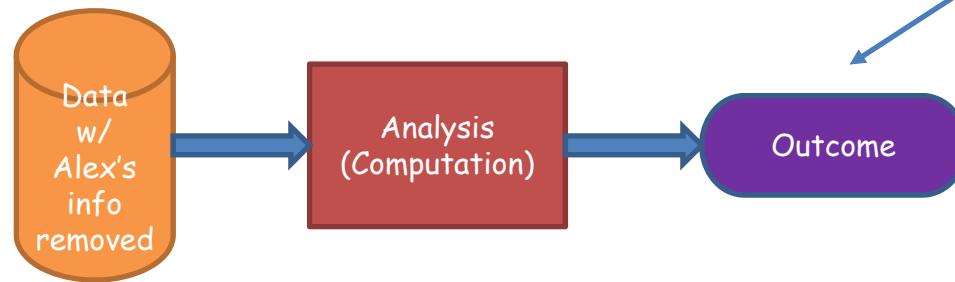


# A Privacy Desiderata

Real world:



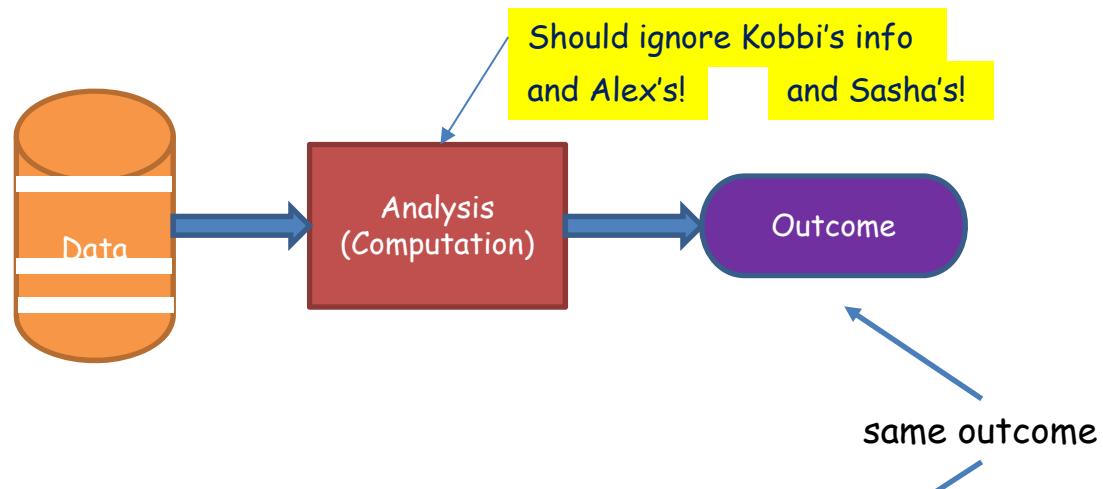
Alex's ideal world:



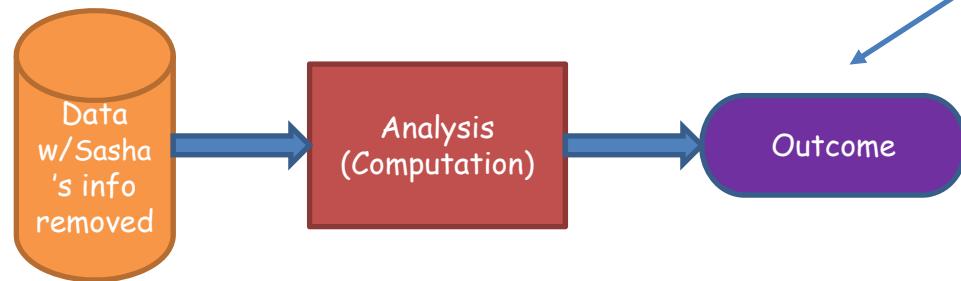
AW2

# A Privacy Desiderata

Real world:



Sasha's ideal world:



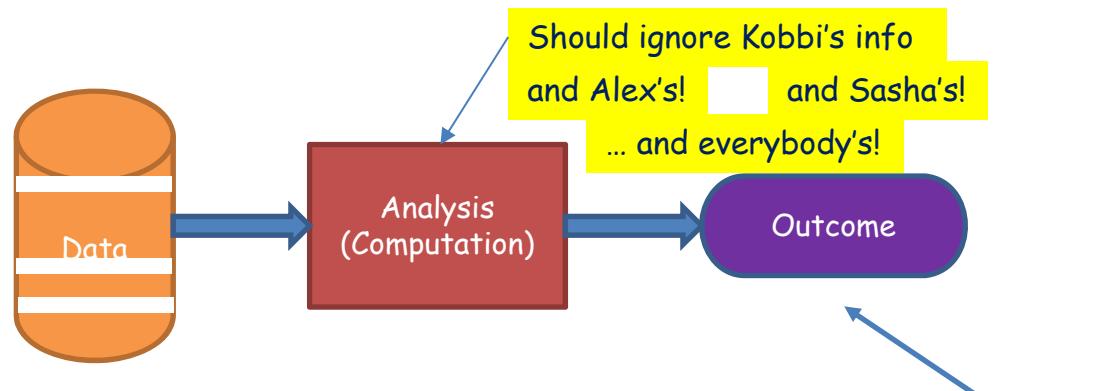
**AW2**

**JULES**

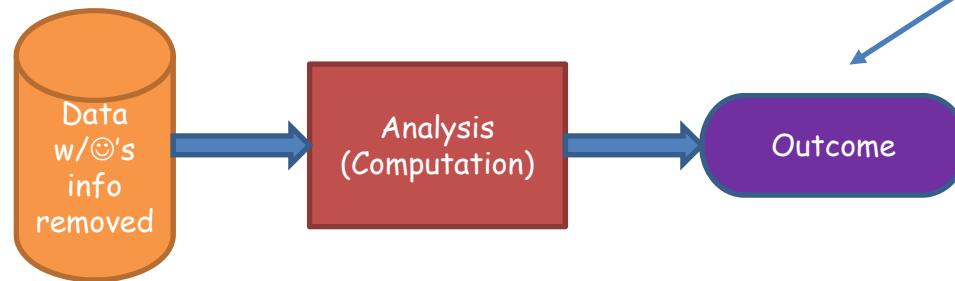
Alexandra Wood, 5/15/2018

# A Privacy Desiderata

Real world:



☺'s ideal world:

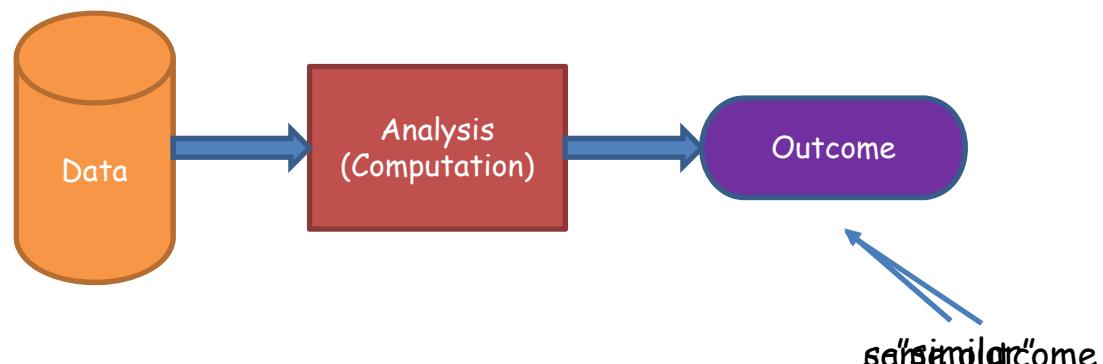


# **Oops!**

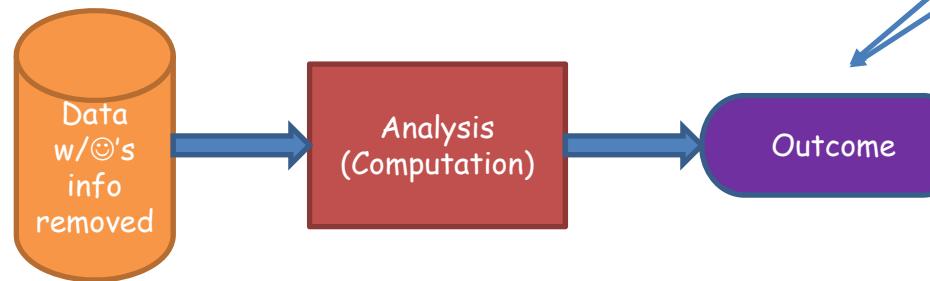
That did not go so well ...

# A More Realistic Privacy Desiderata

Real world:

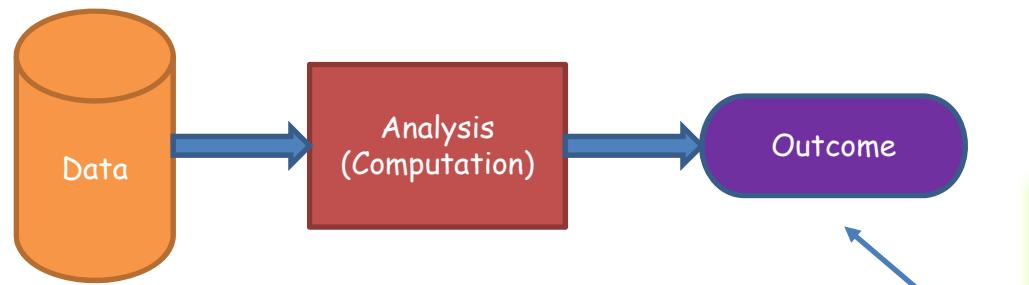


☺'s ideal world:



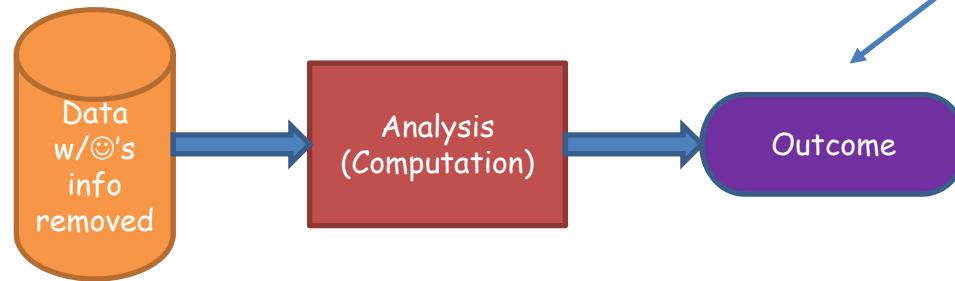
# Differential Privacy [Dwork McSherry Nissim Smith '06]

Real world:



smaller  $\epsilon$  – better privacy

☺'s ideal world:



Chance of bad event almost the same in everybody's ideal and real worlds

$\epsilon$ -“similar”

# Understanding Differential Privacy

- “Automatic” opt-out: I am protected (almost) as if my info was not used at all.
- I incur limited risk: Contributing my real info can increase the probability I will be denied insurance by at most 1%.
  - When compared with not participating, or contributing fake info.
- These privacy guarantees are provided independent of the methods used by a potential attacker and in presence of arbitrary auxiliary information.
- Future proof: Avoids the “penetrate and patch” cycle.

# A Privacy “Budget”

DP provides provable privacy guarantees with respect to the cumulative risk from successive data releases.

- Combination of  $\epsilon$ -differentially private computations results in differential privacy (with larger  $\epsilon$ ).
- Can manage accumulated privacy loss.
  - Whereas other known definitions of privacy do not measure the cumulative risk from multiple analyses/releases.
- **This is an important feature, not a bug!**
  - Consider how ignoring the fuel gauge would not make your car run indefinitely without refueling.



# Transparency

DP has the benefit of transparency.

- It is not necessary to maintain secrecy around a differentially private computation or its parameters.
  - Whereas some traditional techniques relied on secret algorithms or parameters.
- Benefits of transparency include:
  - Knowledge accumulation.
  - Scrutiny by the scientific community.
  - Possibility of accounting for DP in statistical inference.

# Application for Public Access to Data

DP can be used to provide broad, public access to data or data summaries in a privacy-preserving way.

- Can consider data publications that were otherwise impossible.
  - Whereas traditional techniques would require (more often) to apply controls in addition to de-identification.

# Differential Privacy and Concepts from Privacy Law and Policy \*

- **PII:** Differential privacy can be interpreted as ensuring that using an individual's data will (essentially) not reveal any personally identifiable information that is specific to her.
  - Here, specific refers to information that cannot be inferred unless the individual's information is used in the analysis.

# Differential Privacy and Concepts from Privacy Law and Policy \*

✓ PII

- Singling out:
  - This can be formalized mathematically.
    - DP protects against a specific notion of singling out (“predicate singling out”).
    - Note: rigorous argument also wrt FERPA’s concept of de-identification.

**AW3**

**Singling out text**

Alexandra Wood, 5/15/2018

# Differential Privacy and Concepts from Privacy Law and Policy \*

- ✓ PII
- ✓ Singling out
- **Linkage:** Microdata or contingency tables that allow the identification of population uniques cannot be created using statistics produced by a differentially private tool.
  - This can be formalized and proved mathematically.

# Differential Privacy and Concepts from Privacy Law and Policy\*

- ✓ PII
- ✓ Singling out
- ✓ Linkage

- **Inference:** Differential privacy masks the contribution of any single individual, (essentially) making it impossible to infer any information specific to an individual, including whether an individual's information was used at all.
  - But DP does not protect against all inferences.

# Differential Privacy and Concepts from Privacy Law and Policy \*

- ✓ PII
- ✓ Singling out
- ✓ Linkage
- ✓ Inference

Differential privacy provides protection (far) beyond “identifiability.”

## Example: Reasoning About Risk Gertrude's Life Insurance



- Gertrude:
  - Age: 65
  - She has a \$100,000 life insurance policy.
  - She is considering participating in a medical study but is concerned it may affect her insurance premium.

# Example: Reasoning About Risk Gertrude's Life Insurance



- Based on her age and sex, she has a 1% chance of dying next year. Her life insurance premium is set at  $0.01 \times \$100,000 = \$1,000$ .
- Gertrude is a coffee drinker. If the medical study finds that 65-year-old female coffee drinkers have a 2% chance of dying next year, her premium would be set at \$2,000.
  - This would be her **baseline risk**: Her premium would be set at \$2,000 even if she were not to participate in the study.
- **Can Gertrude's premium increase beyond her baseline risk?**
  - She is worried that the study may reveal more about her, such as that she *specifically* has a 50% chance of dying next year. This can increase her premium from \$2,000 to \$50,000!

# Example: Reasoning About Risk Gertrude's Life Insurance



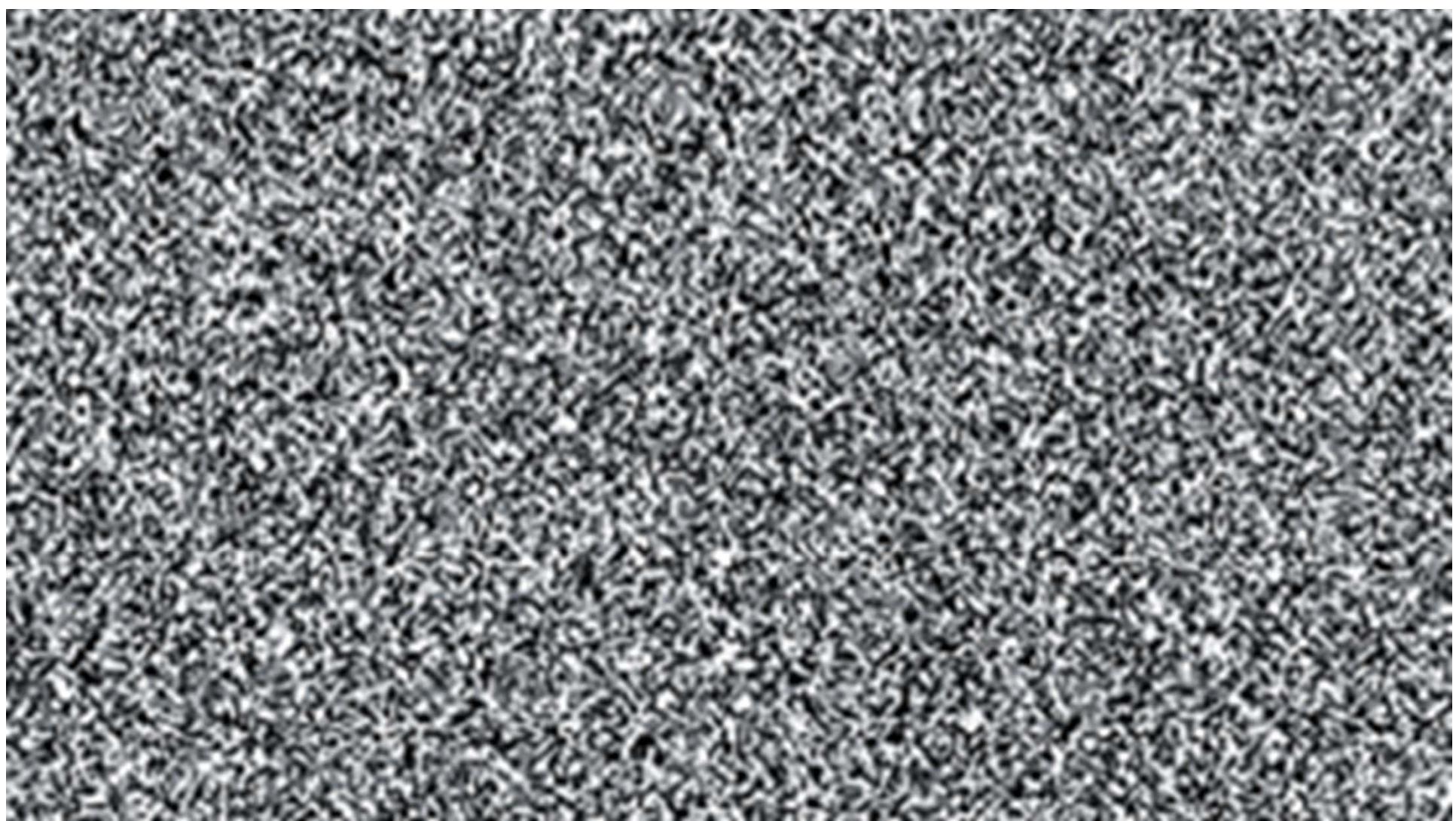
- Reasoning about Gertrude's risk
  - Imagine instead the study is performed using differential privacy with  $\epsilon = 0.01$ .
  - The insurance company's estimate of Gertrude's risk of dying in the next year can increase to at most
$$(1 + \epsilon) \cdot 2\% = 2.02\%.$$
  - Her premium would increase to at most \$2,020. Therefore, Gertrude's risk would be  $\leq \$2020 - \$2000 = \$20$ .

# Example: Reasoning About Risk Gertrude's Life Insurance



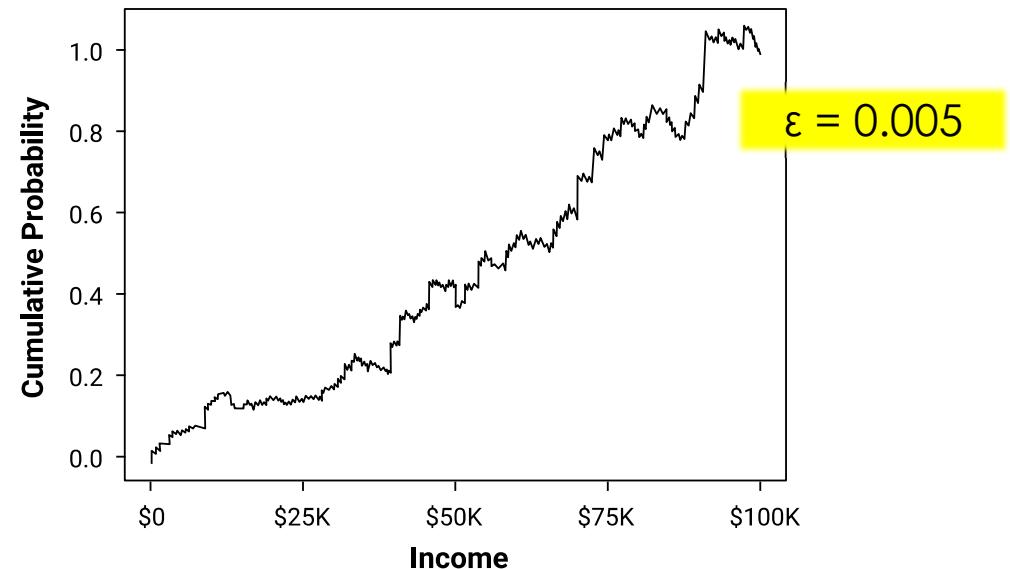
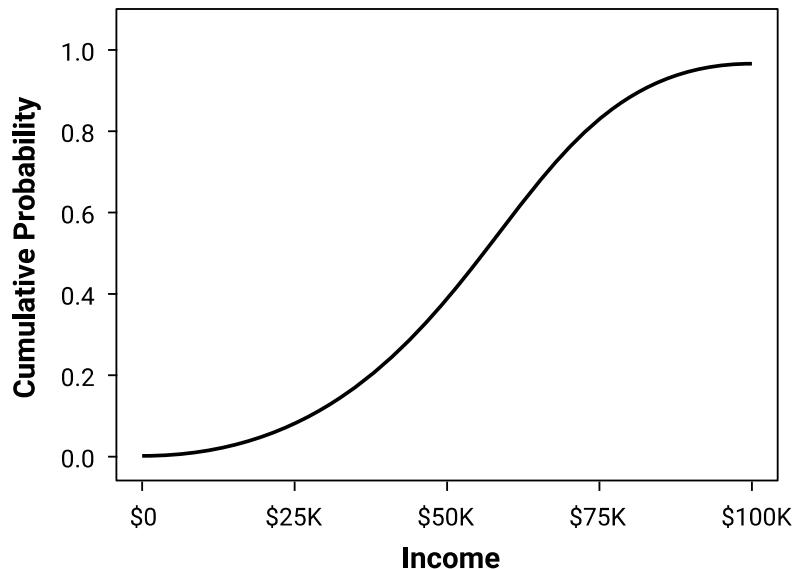
- Generally, calculating one's baseline is very complex (if possible at all).
  - In particular, in our example the 2% baseline depends on the potential outcome of the study.
  - The baseline may also depend on many other factors Gertrude does not know.
- However, differential privacy provides simultaneous guarantees for every possible baseline value.
  - The guarantee covers not only changes in Gertrude's life insurance premiums, but also her health insurance and more.

# **How is differential privacy achieved?**



# Differentially Private Computations

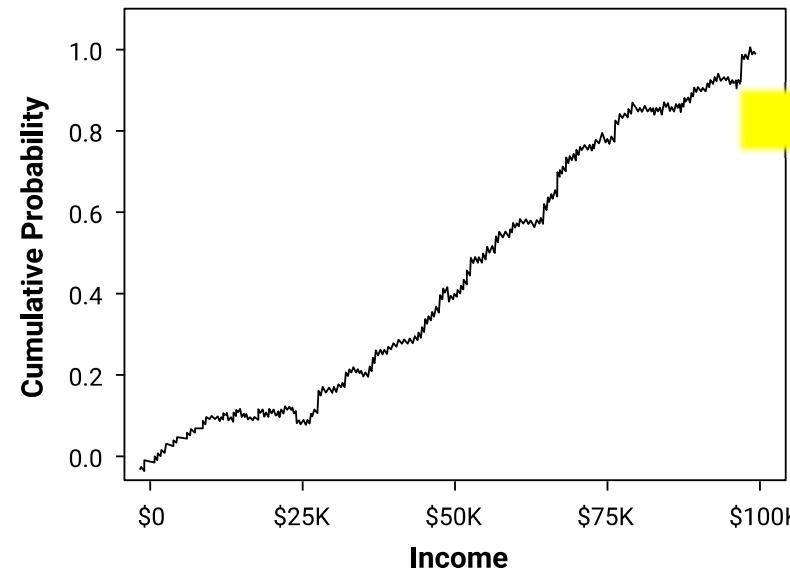
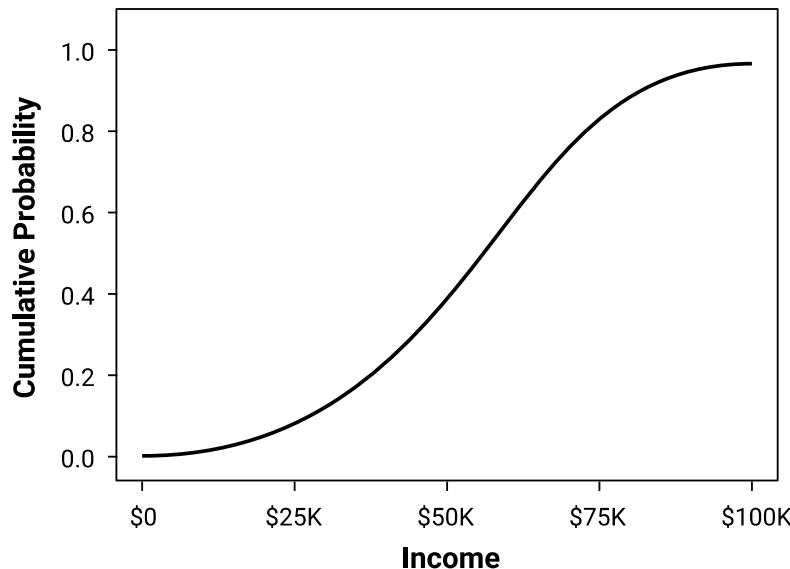
Algorithms maintain differential privacy via the introduction of *carefully crafted* random noise into the computation.



(These CDFs are stylized examples.)

# Differentially Private Computations

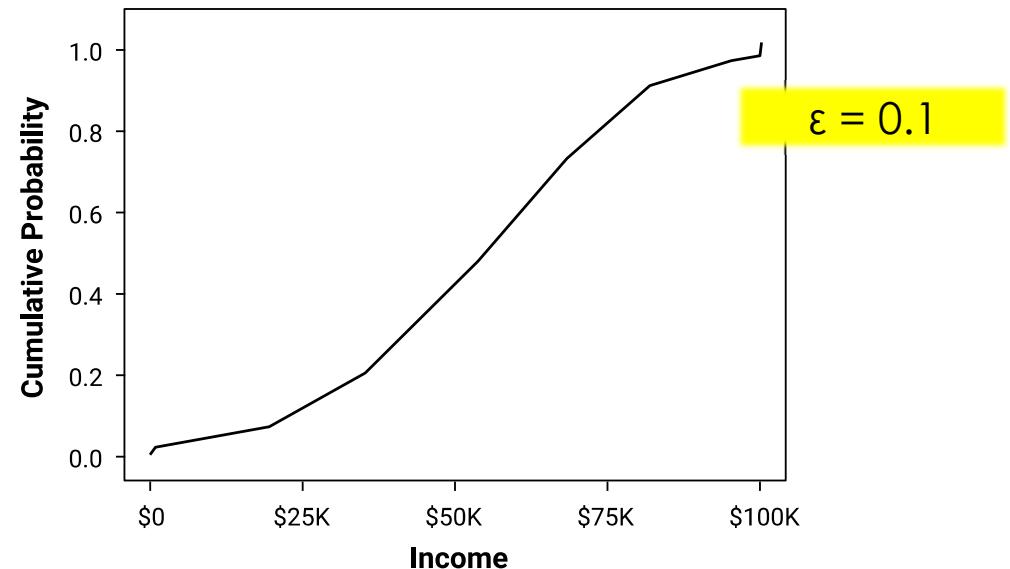
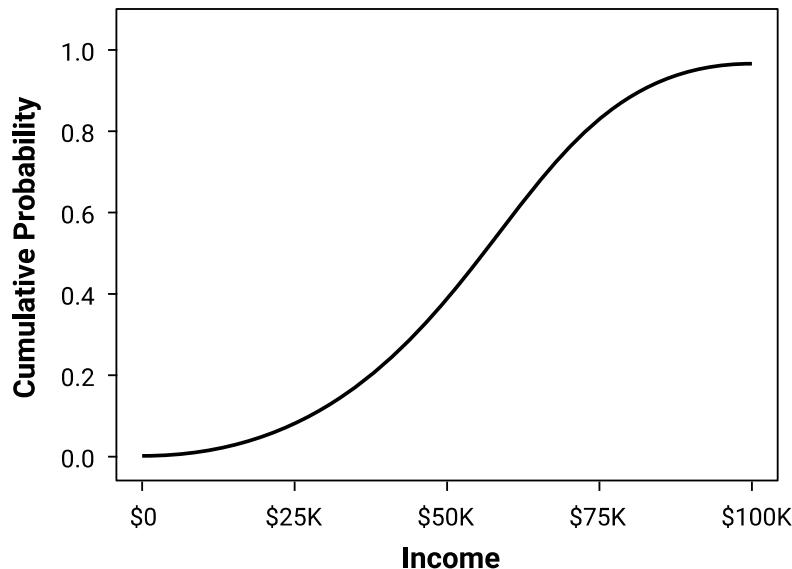
Algorithms maintain differential privacy via the introduction of *carefully crafted* random noise into the computation.



(These CDFs are stylized examples.)

# Differentially Private Computations

Algorithms maintain differential privacy via the introduction of *carefully crafted* random noise into the computation.



(These CDFs are stylized examples.)

# What can be Computed with Differential Privacy?

- **Descriptive statistics:** counts, mean, median, histograms, boxplots, etc.
- **Supervised and unsupervised ML tasks:** classification, regression, clustering, distribution learning, etc.
- **Generation of synthetic data**

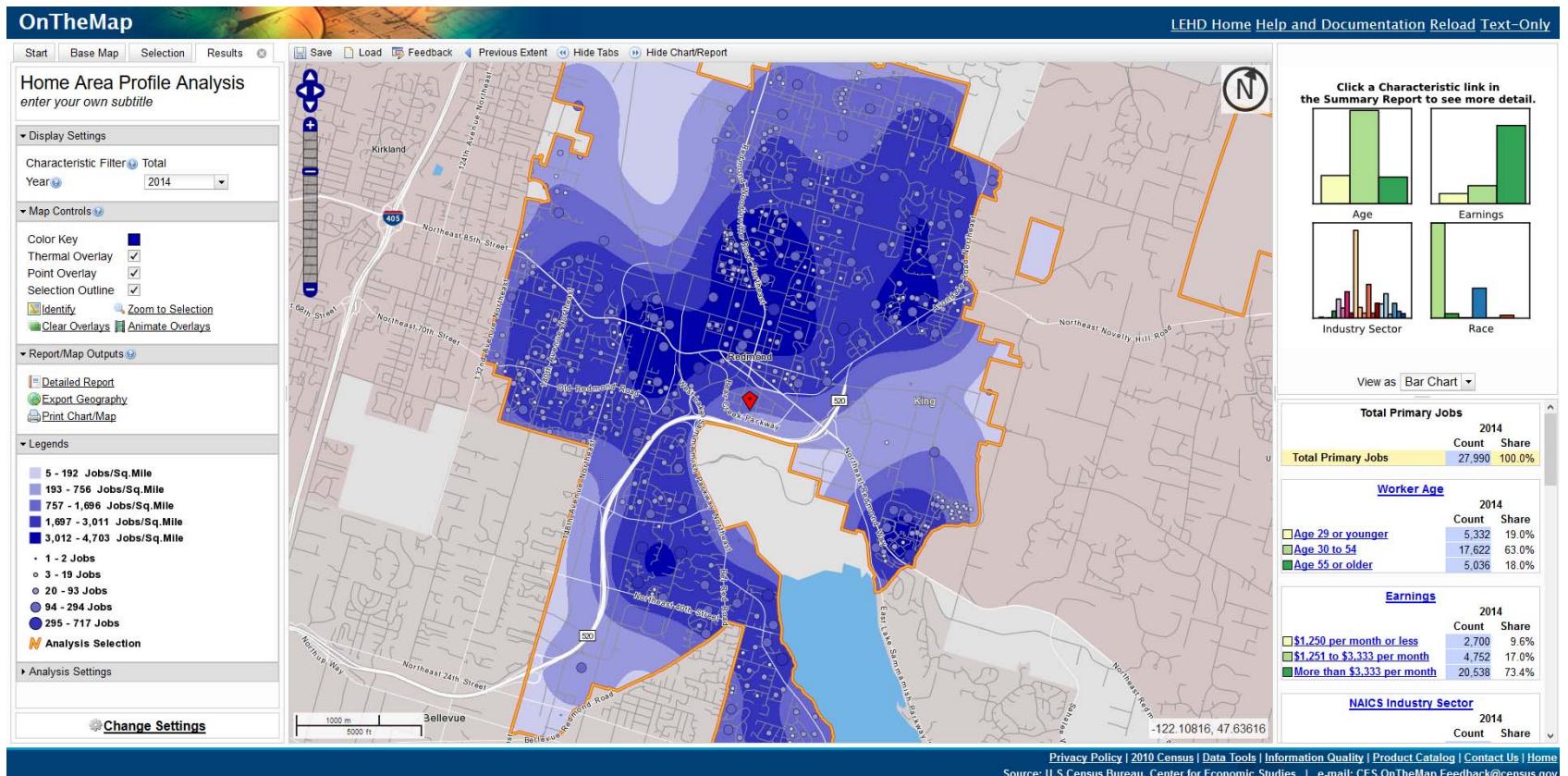
Because of noise addition, differentially private algorithms work best when the number of data records is large.

\*

# Applications

# U.S. Census Bureau

<http://onthemap.ces.census.gov>



2008 AD

# GOOGLE

## RAPPOR: Randomized Aggregatable Privacy-Preserving Ordinal Response

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### ABSTRACT

Randomized Aggregatable Privacy-Preserving Ordinal Response, or RAPPOR, is a technology for crowdsourcing statistics from end-user client software, anonymously, with strong privacy guarantees. In short, RAPPORs allow the forest of client data to be studied, without permitting the possibility of looking at individual trees. By applying randomized response in a novel manner, RAPPOR provides the mechanisms for such collection as well as for efficient, high-utility analysis of the collected data. In particular, RAPPOR permits statistics to be collected on the population of client-side strings with strong privacy guarantees for each client, and without linkability of their reports.

This paper describes and motivates RAPPOR, details its differential-privacy and utility guarantees, discusses its practical deployment and properties in the face of different attack models, and, finally, gives results of its application to both synthetic and real-world data.

### 1 Introduction

Crowdsourcing data to make better, more informed decisions is becoming increasingly commonplace. For any such crowdsourcing, privacy-preservation mechanisms should be

asked to flip a fair coin, in secret, and answer “Yes” if it comes up heads, but tell the truth otherwise (if the coin comes up tails). Using this procedure, each respondent retains very strong deniability for any “Yes” answers, since such answers are most likely attributable to the coin coming up heads; as a refinement, respondents can also choose the untruthful answer by flipping another coin in secret, and get strong deniability for both “Yes” and “No” answers.

Surveys relying on randomized response enable easy computations of accurate population statistics while preserving the privacy of the individuals. Assuming absolute compliance with the randomization protocol (an assumption that may not hold for human subjects, and can even be non-trivial for algorithmic implementations [23]), it is easy to see that in a case where both “Yes” and “No” answers can be denied (flipping two fair coins), the true number of “Yes” answers can be accurately estimated by  $2(Y - 0.25)$ , where  $Y$  is the proportion of “Yes” responses. In expectation, respondents will provide the true answer 75% of the time, as is easy to see by a case analysis of the two fair coin flips.

Importantly, for one-time collection, the above randomized survey mechanism will protect the privacy of any specific respondent, irrespective of any attacker’s prior knowl-

2014 AD

# Apple

Apple will not  
see your data

ANDY GREENBERG SECURITY 06.13.16 07:02 PM

**APPLE'S 'DIFFERENTIAL  
PRIVACY' IS ABOUT COLLECTING  
YOUR DATA—BUT NOT YOUR  
DATA**



2016 AD



## Harvard University Privacy Tools Project

[Home](#) [Research ▾](#) [News](#) [People ▾](#) [Publications](#) [Software ▾](#) [Outreach ▾](#)



The Privacy Tools Project is a broad effort to advance a multidisciplinary understanding of data privacy issues and build computational, statistical, legal, and policy tools to help address these issues in a variety of contexts. It is a collaborative effort between Harvard's [Center for Research on Computation and](#)

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### LATEST NEWS & BLOG POSTS

Graduate Student Michael Bar-Sinai Presented at the 8th Annual ESPAnet Israel 2017

PI Salil Vadhan, PI Kobbi Nissim, and Senior Researcher Marco Gaboardi Presented at the Third Biennial Secure and Trustworthy CyberSpace Principal Investigators' Meeting (SaTC PI Meeting '17)

Berkman Klein Center Seeks Applications for 2017 Summer Internship Program

Harvard Magazine Highlights Privacy Tools Project in Article on Privacy and Security

George Kellaris Featured on CRCS Blog

Privacy Tools Project Featured in Harvard Law Review

Berkman Klein Center Seeks Fellow for Privacy

2018 AD

# **DP in Practice: Challenges**

# Transitioning to Practice

- A relatively new concept:
  - How to communicate its strengths and limitations?
  - What are the “right” use cases for implementation at this stage?
- Access to data:
  - Via a mechanism; Noise added
  - Limited by the “privacy budget”
    - Setting the budget is a policy question
- Matching guarantees with privacy law & regulation

\*

# Conclusion

# Main Takeaways

- **Accumulating failures:** anonymization & traditional SDL techniques
- **Differential privacy:**
  - A standard providing a rigorous framework for developing privacy technologies with provable quantifiable guarantees
  - Rich theoretical work, now transitioning to practice
    - First real-world applications and use
  - Not a panacea; to be combined (wisely!) with other technical and policy tools

\*

# Resources

# Learning More About Differential Privacy

- [Page et al, 2018] [Differential Privacy: An Introduction For Statistical Agencies](#), UK ONS.
- [Wood et al, 2019] [Differential Privacy: A Primer for a Non-technical Audience](#), Vanderbilt JETLaw.
- [Nissim et al, 2018] [Bridging the gap between computer science and legal approaches to privacy](#), Harvard JOLT.
- [Dwork 2011] [A Firm Foundation for Private Data Analysis](#), CACM January 2011.
- [Heffetz & Ligett, 2014] [Privacy and Data-Based Research](#), Journal of Economic Perspectives.
- [Dwork & Roth, 2014] [The Algorithmic Foundations of Differential Privacy](#), Now publishers.
- + [Vadhan, 2017] [The Complexity of Differential Privacy](#)

less  
technical

technical

# Projects, Software Tools [Partial List]

[Microsoft Research] [PINQ](#)

[UT Austin] [Airavat: Security & Privacy for MapReduce](#)

[UC Berkeley] [GUPT](#)

[CMU-Cornell-PennState] [Integrating Statistical and Computational Approaches to Privacy](#)

[US Census] [OnTheMap](#)

[Google] [Rappor, TensorFlow Privacy](#)

[UCSD] [Integrating Data for Analysis, Anonymization, and Sharing \(iDash\)](#)

[UPenn] [Putting Differential Privacy to Work](#)

[Stanford-Berkeley-Microsoft] [Towards Practicing Privacy](#)

[Duke-NISS] [Triangle Census Research Network](#)

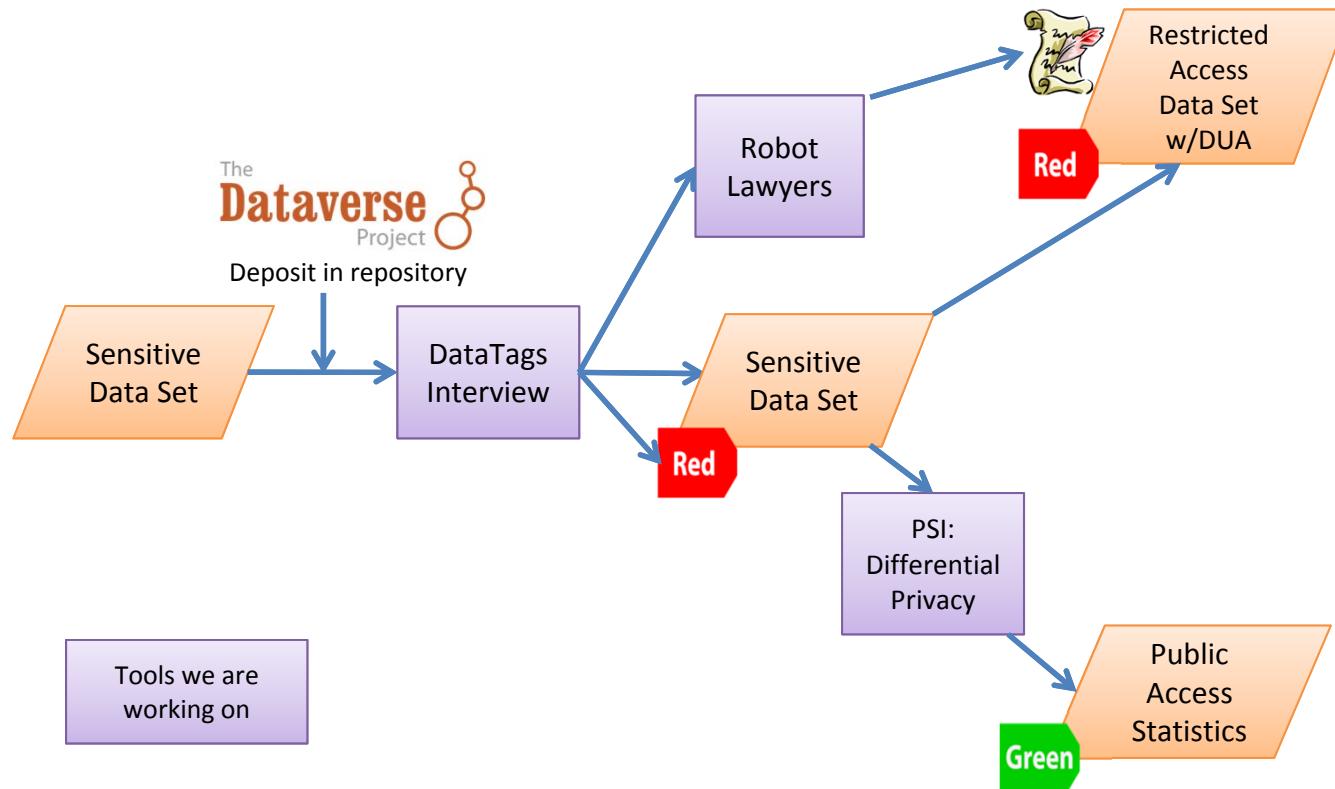
[Harvard] [Privacy Tools](#)

[Georgetown-Harvard-BU] [Formal Privacy Models and Title 13](#)

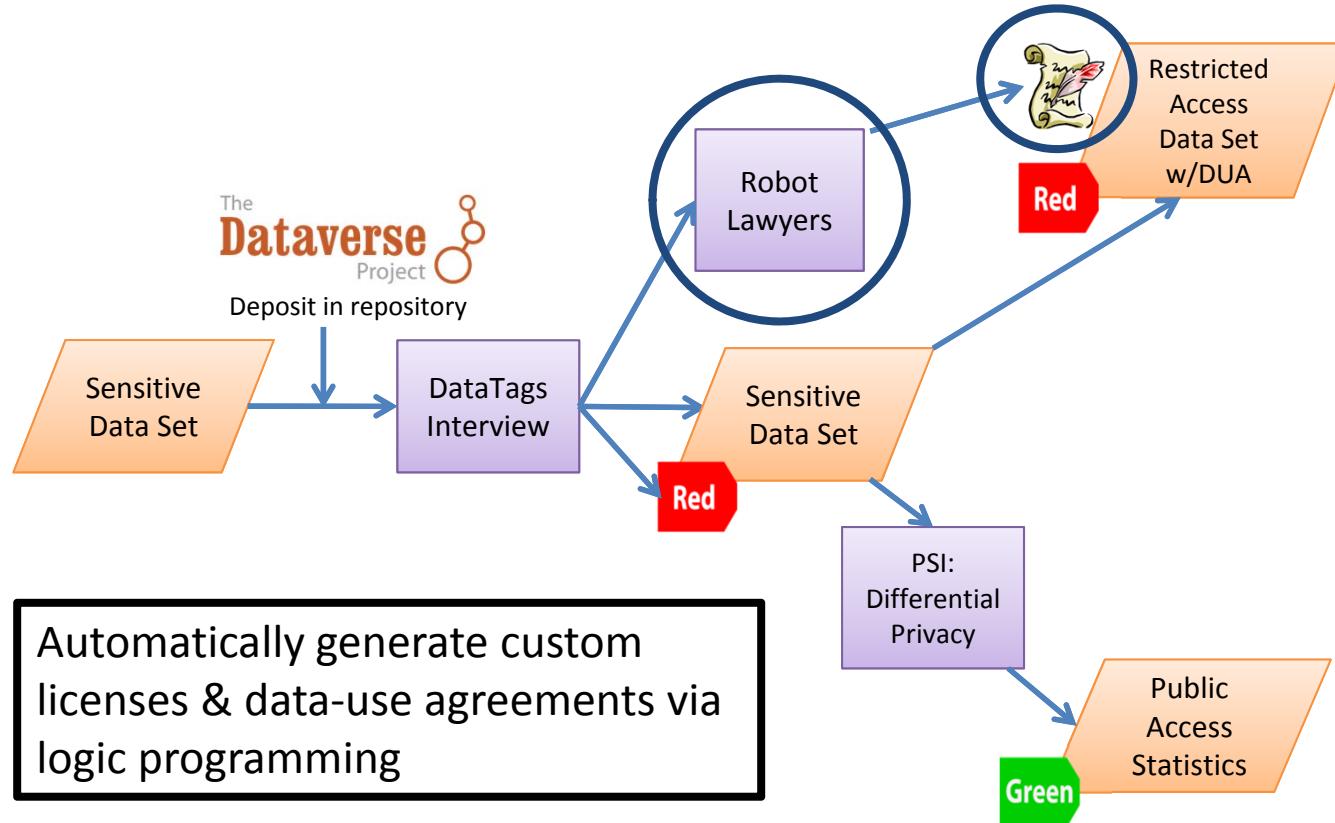
[Harvard-Georgetown-Buffalo] [Computing over Distributed Sensitive Data](#)

# **Backup Slides**

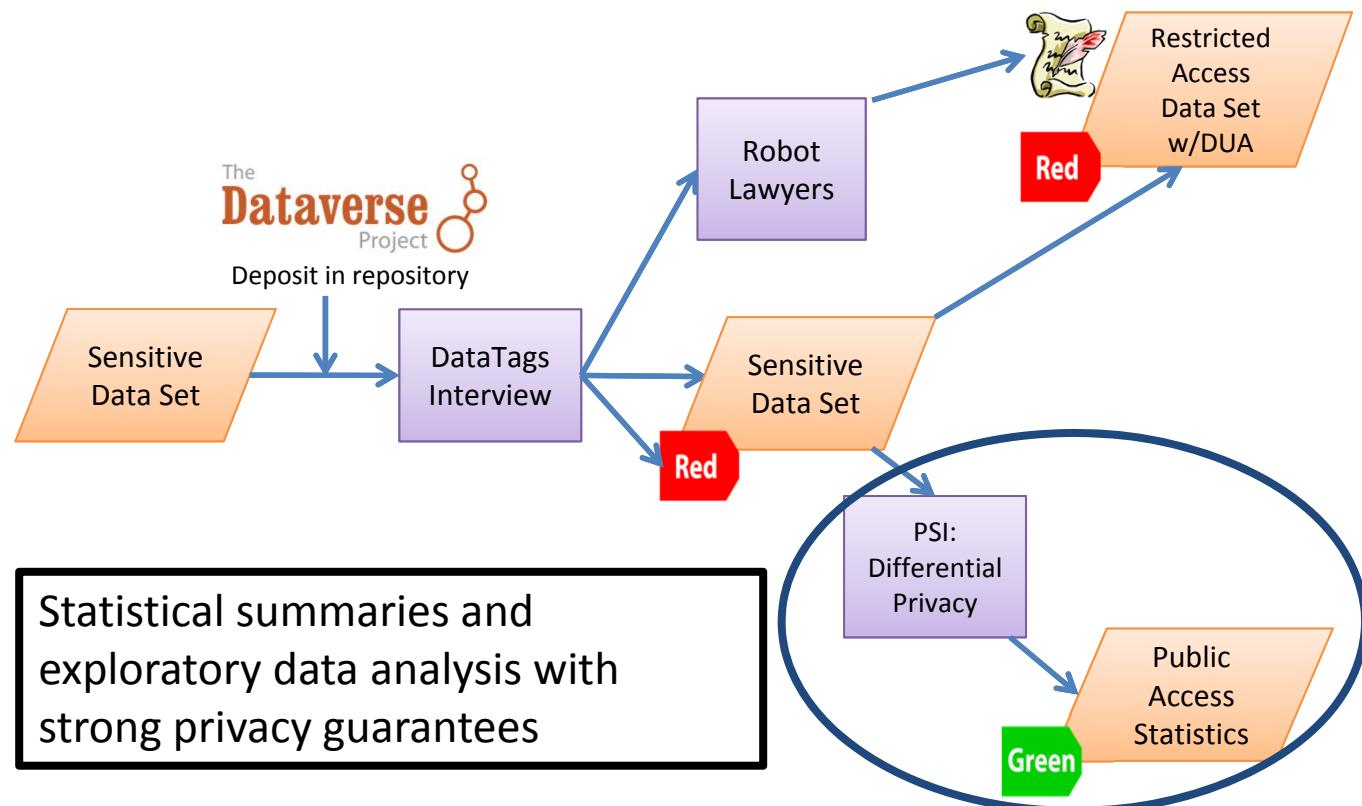
# The Privacy Tools Project



# The Privacy Tools Project: Robot Lawyers



# The Privacy Tools Project: PSI



# The Privacy Tools Project: Bridging Defs

